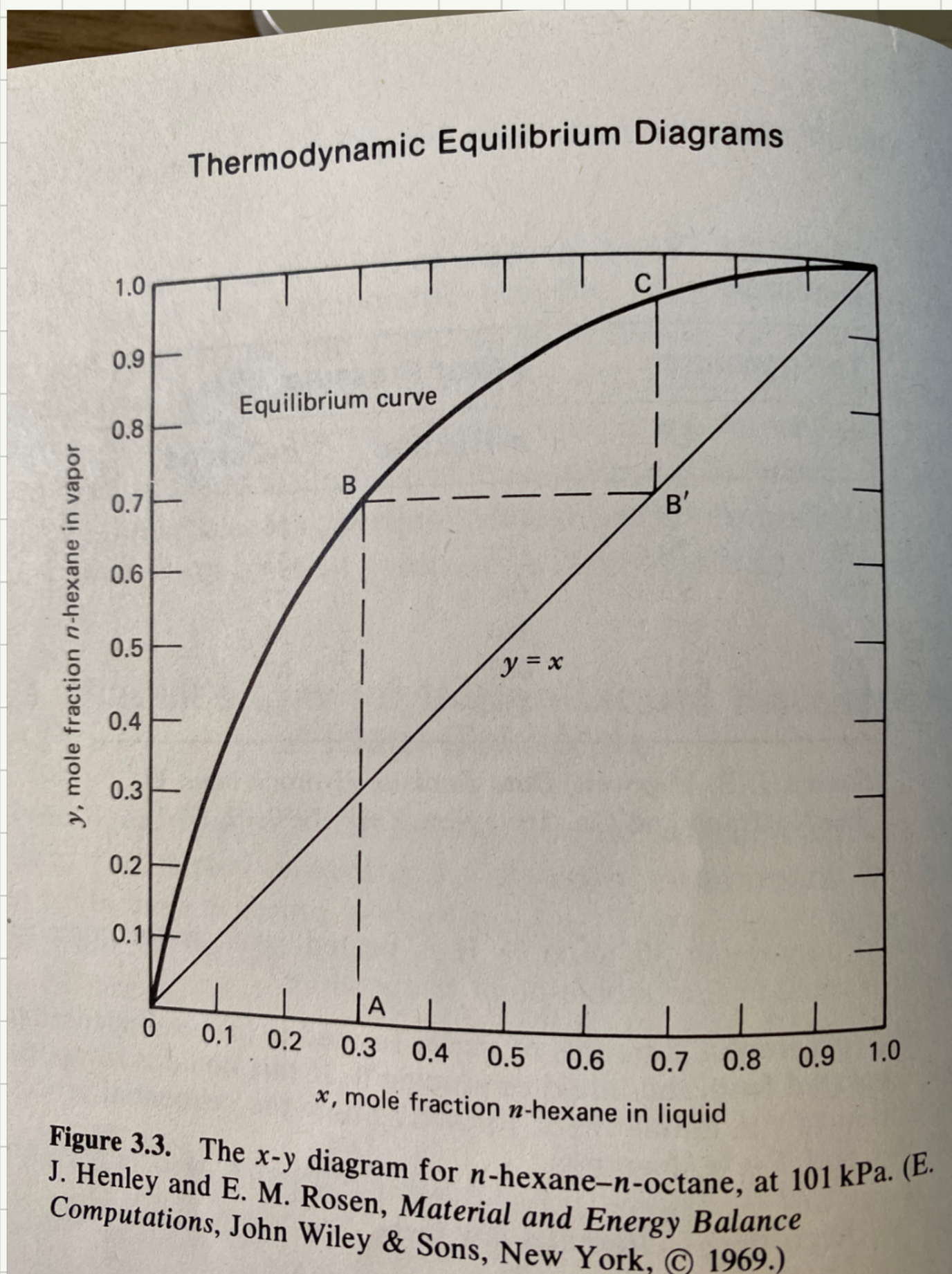


CBE 34487

6/25/20

MULTI STAGE OPERATIONS

CONSIDER A LIQUID MIXTURE



SUPPOSE $x = .3$

$y = .7$

IT IS DESIRED
TO GET HEXANE
AT ~ 0.99
PURITY?

WHAT CAN YOU
DO.?

Thermodynamic Equilibrium Diagrams

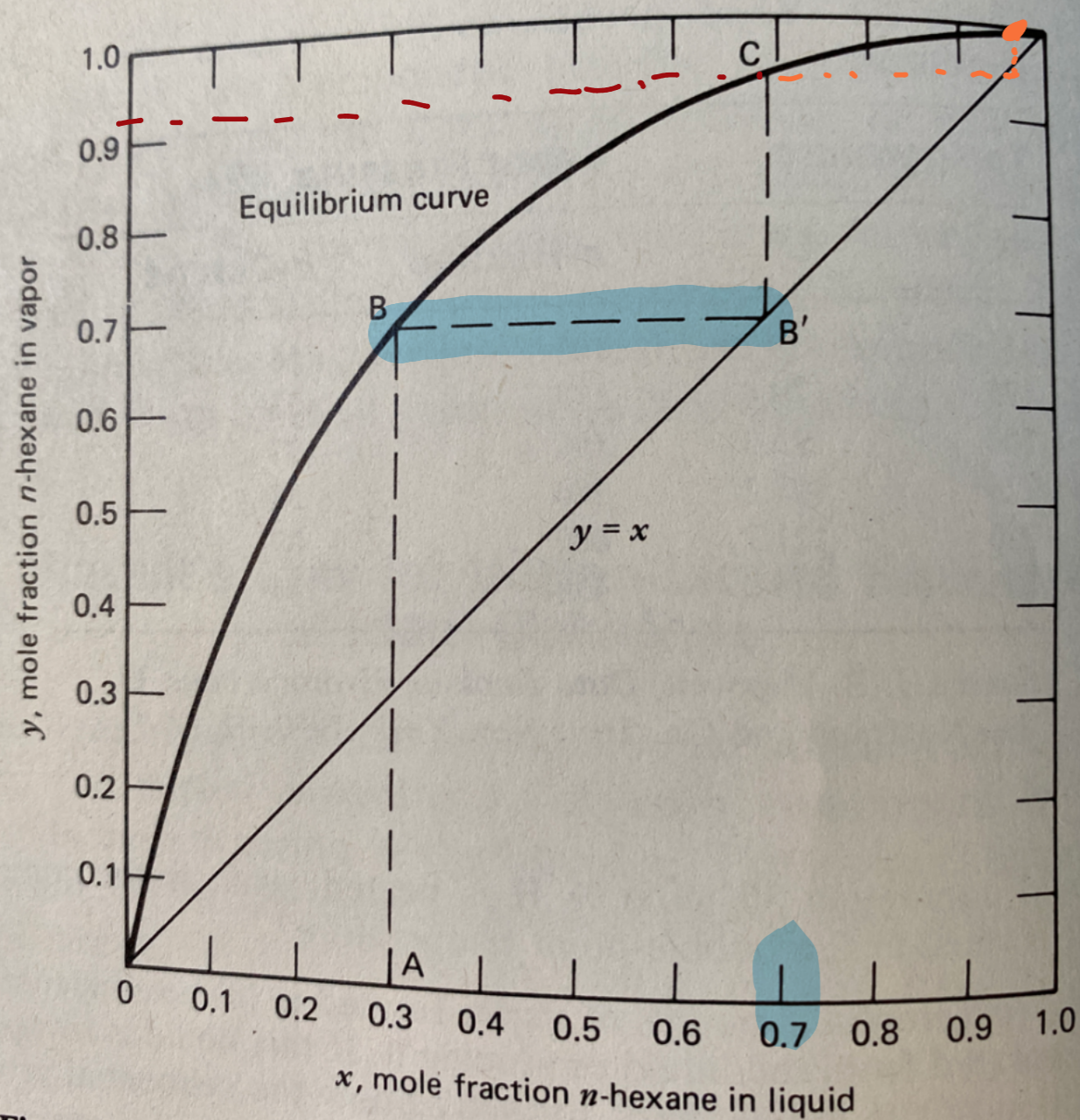


Figure 3.3. The x-y diagram for n-hexane-n-octane, at 101 kPa. (E. J. Henley and E. M. Rosen, *Material and Energy Balance Computations*, John Wiley & Sons, New York, © 1969.)

WE COULD COLLECT
SOME OF THE
VAPOR AND
CONDENSE.
OF COURSE, IF
WE PICKED A
SIGNIFICANT
FRACTION,
THE CONCENTRATION
WOULD DROP.

NOW WE HAVE VAPOR AT $y = .93$

NOW CONDENSE THIS AND $x = .93$

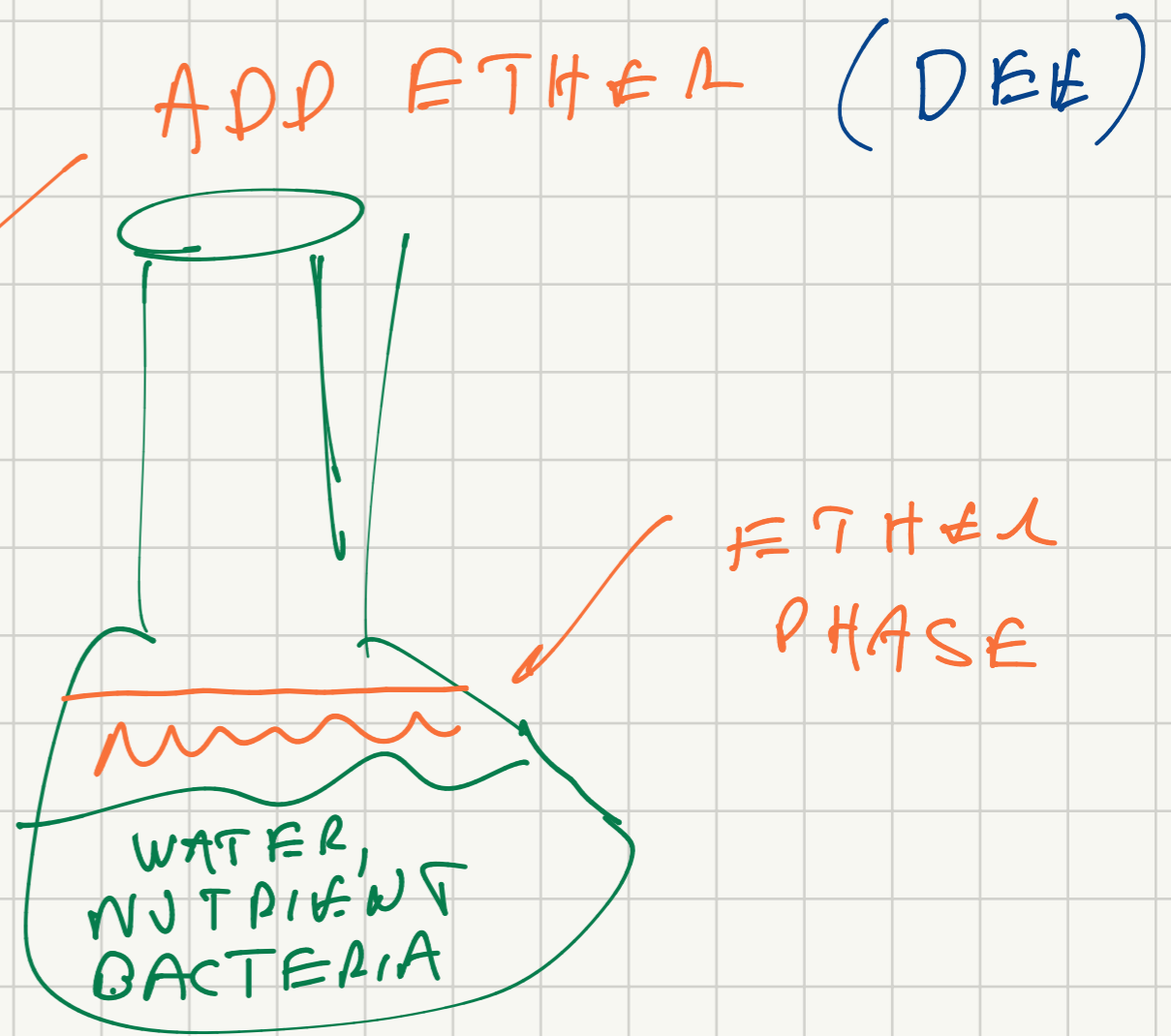
IF WE VAPORIZE AGAIN, WE

WOULD BE CLOSE TO $.99$

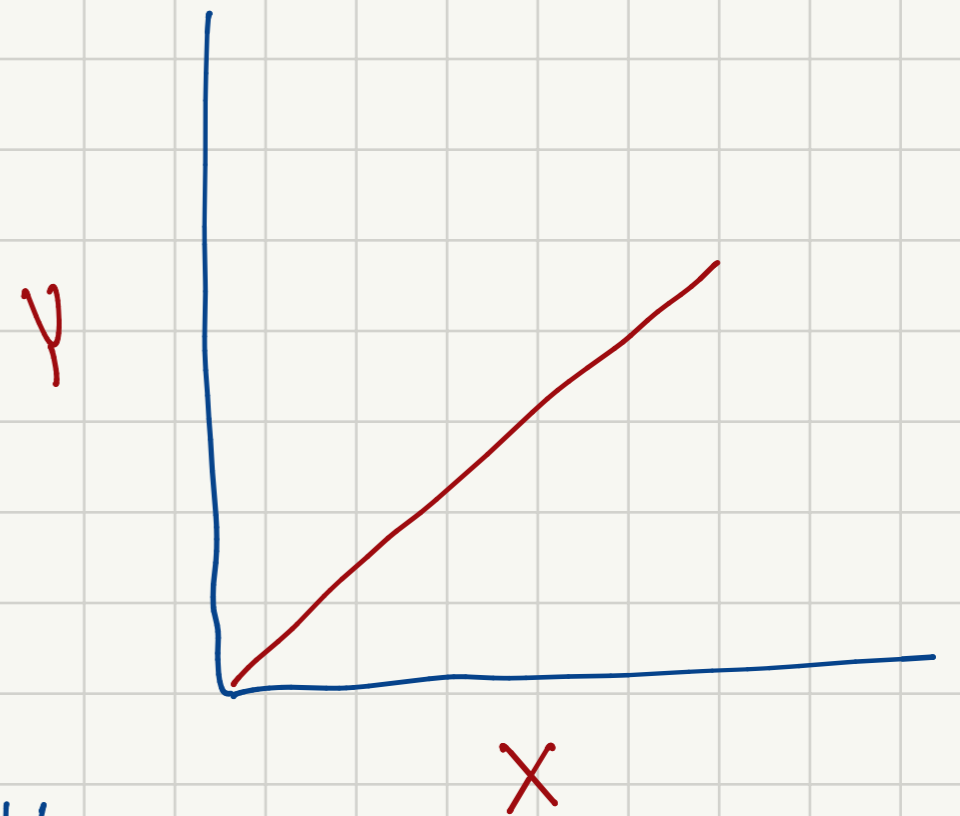
OF COURSE WE WOULD HAVE
ONLY A SMALL AMOUNT OF PRODUCT.

WE SEE THE PRINCIPLE !!

HOW ABOUT EXTRACTION.



THE BACTERIA
HAVE PRODUCED
DESIRED
COMPOUND
IT IS AT LEAST
A LITTLE
HYDROPHOBIC

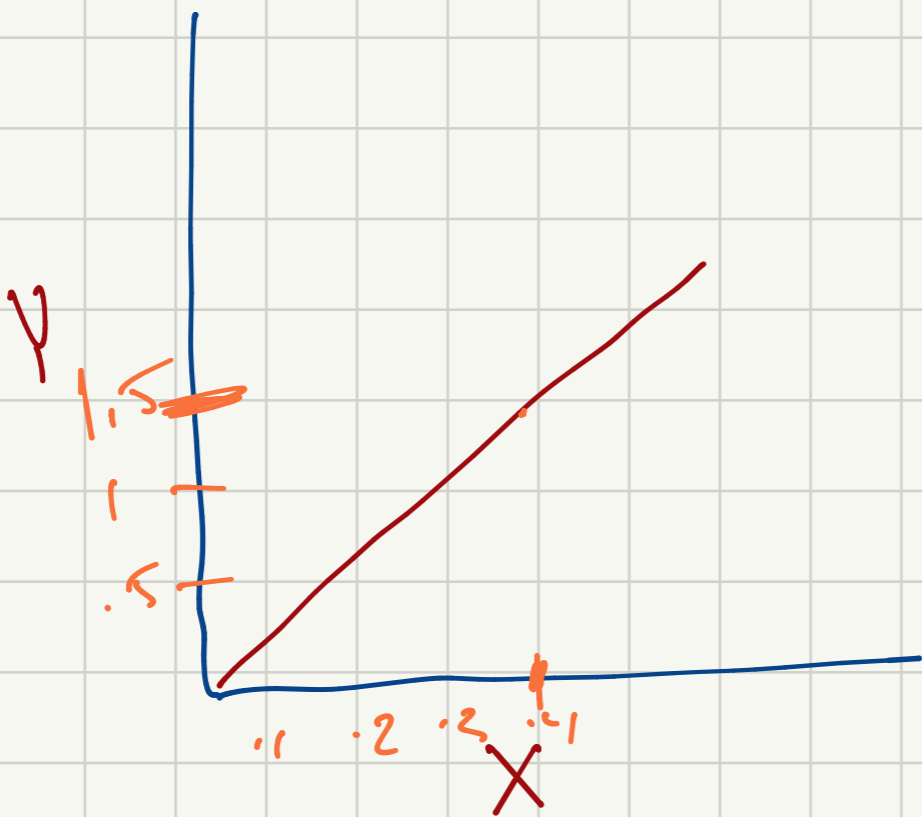


EQUILIBRIUM PARTITIONING

$$Y = m X$$

$$X = \frac{\text{MASS OF P.C.}}{\text{MASS H}_2\text{O}}$$

$$Y = \frac{\text{MASS OF P.C.}}{\text{MASS DEE}}$$

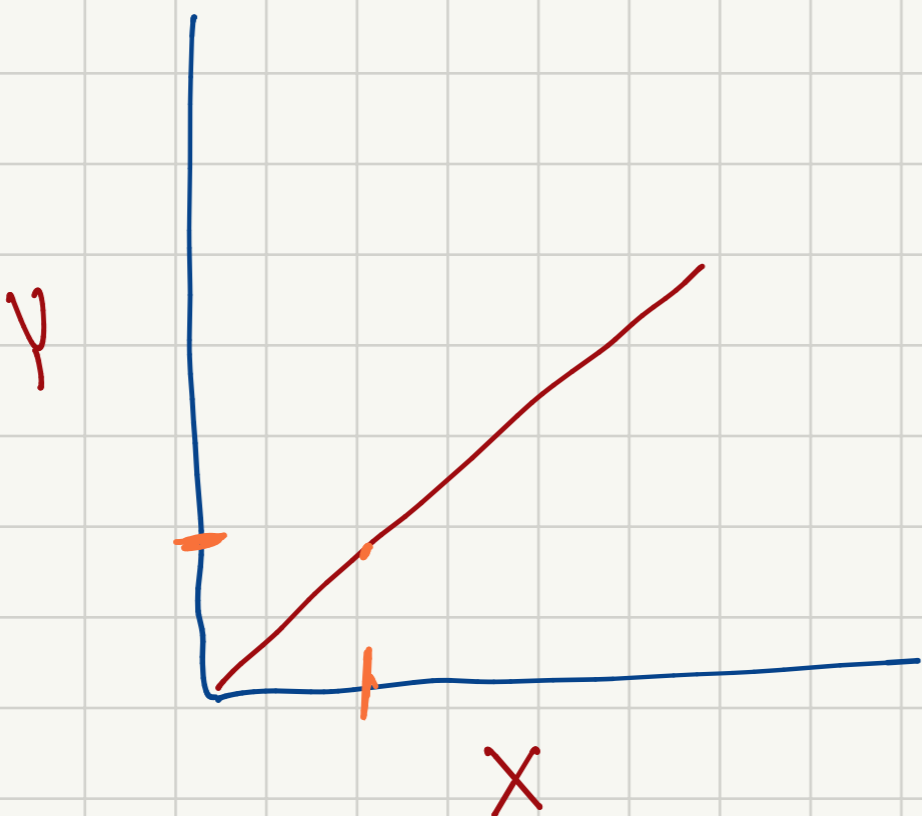


SUPPOSE WE ADD
500 ML OF DFE TO
500 BR

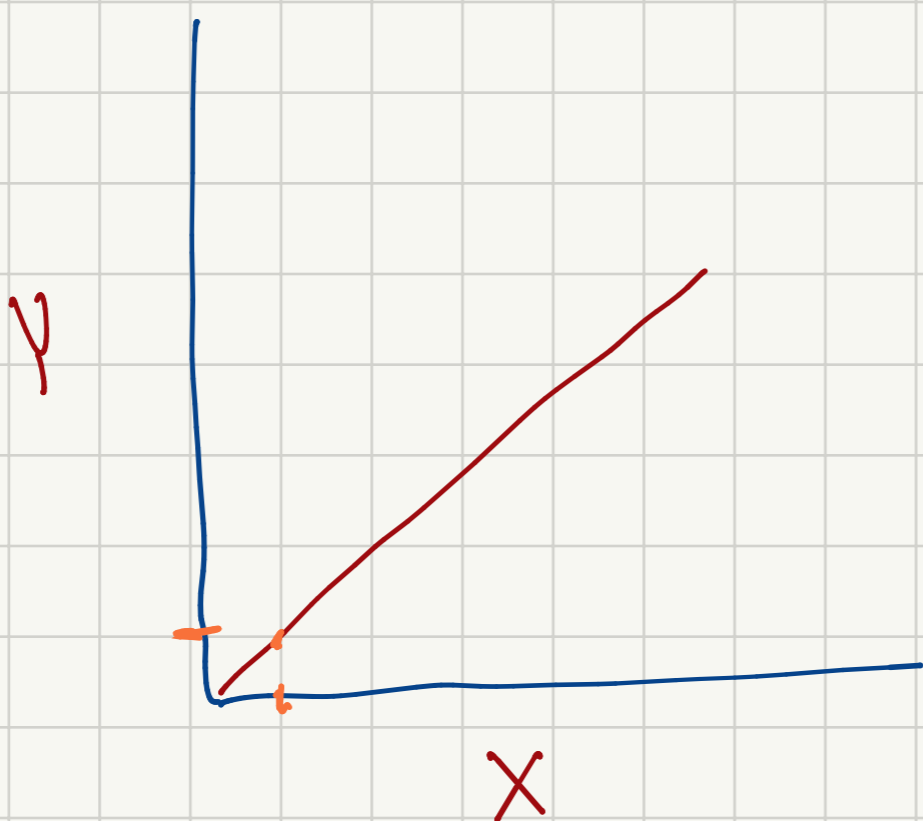
$$X = 0.4$$

$$Y = 1.5$$

WE COULD ADD
MORE



OR MORE



THIS ACCOMPLISHED

THE GOAL OF

REMOVING

VALUABLE DRUG

FROM BOTH BUT

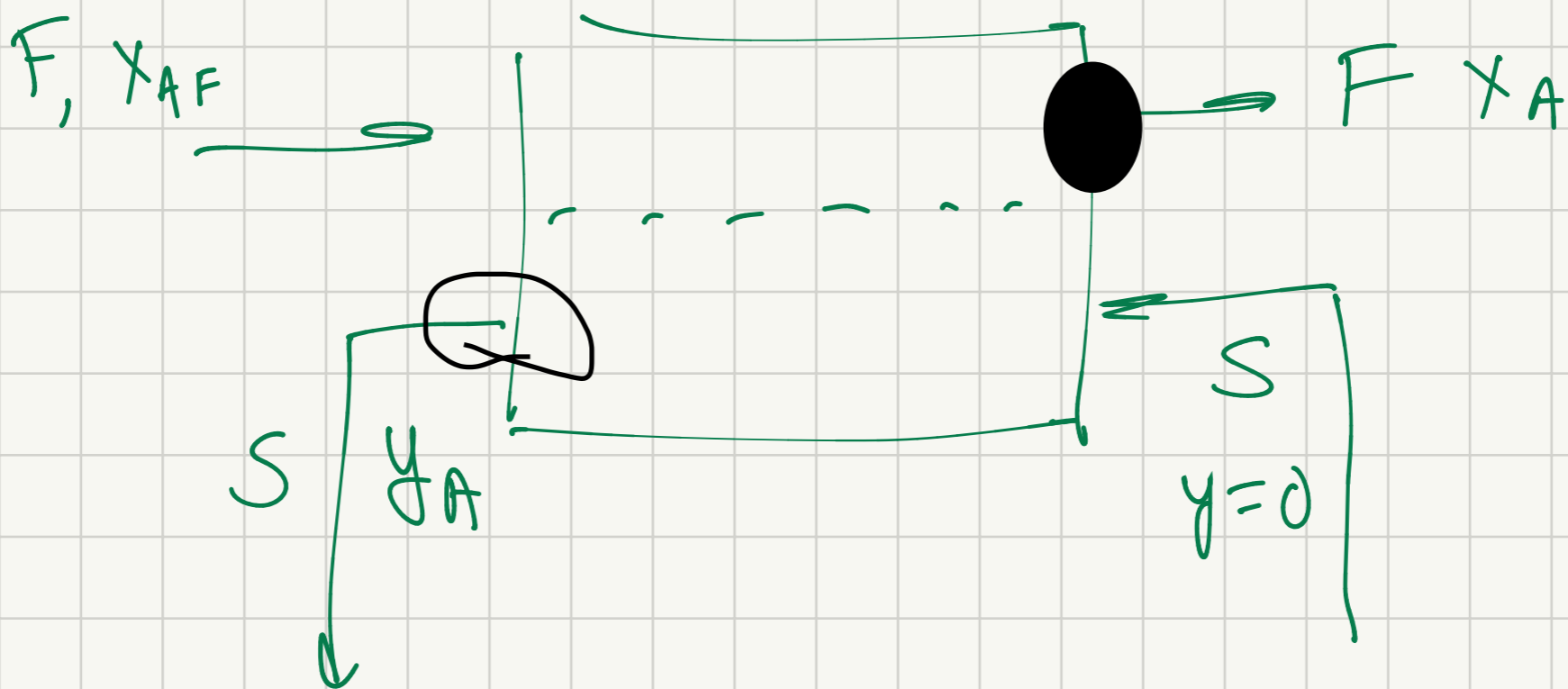
IT IS INCREASINGLY DILUTE!

CONSIDER EXTRACTION

$$Y = m X$$

FEED STREAM, $F (=) \frac{\text{MASS}}{\text{TIME}}$

SOLVENT STREAM $S (=) \frac{\text{MASS}}{\text{TIME}}$



$$\cancel{y_s} S + X_{AF} F = F X_A + S y_A$$

(IN) (OUT)

$$y_A = m X_A$$

AMOUNT
REMAINING
IN
FEED
STREAM

$$X_{AF} F = F X_A + S m X_A$$

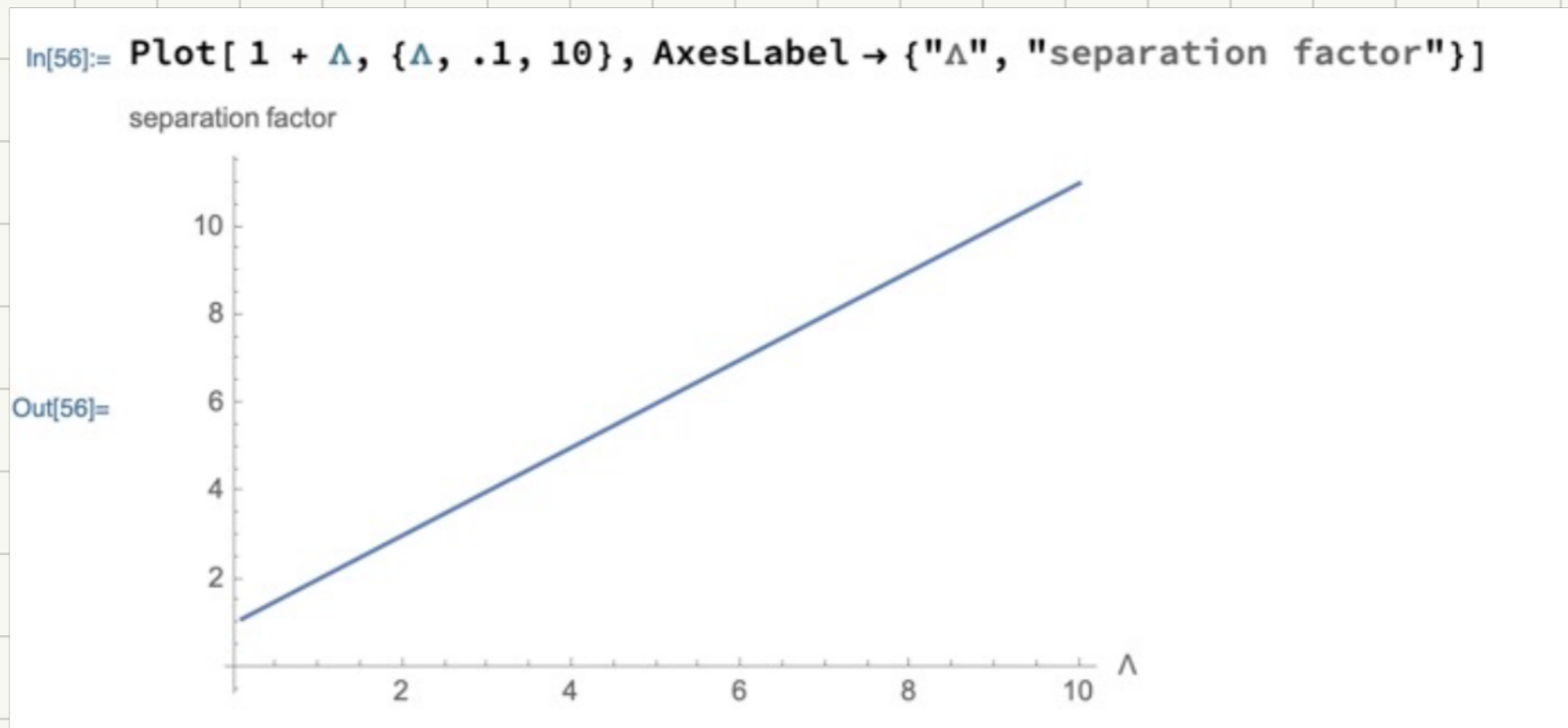
$$\frac{X_A}{X_{AF}} = \frac{1}{1 + \frac{mS}{F}}$$

$$\frac{X_A}{X_{AF}} = \frac{1}{1 + \frac{mS}{F}}$$

PICK, $\Lambda \equiv \frac{mS}{F}$, $\xi \equiv \frac{X_{AF}}{X_A}$

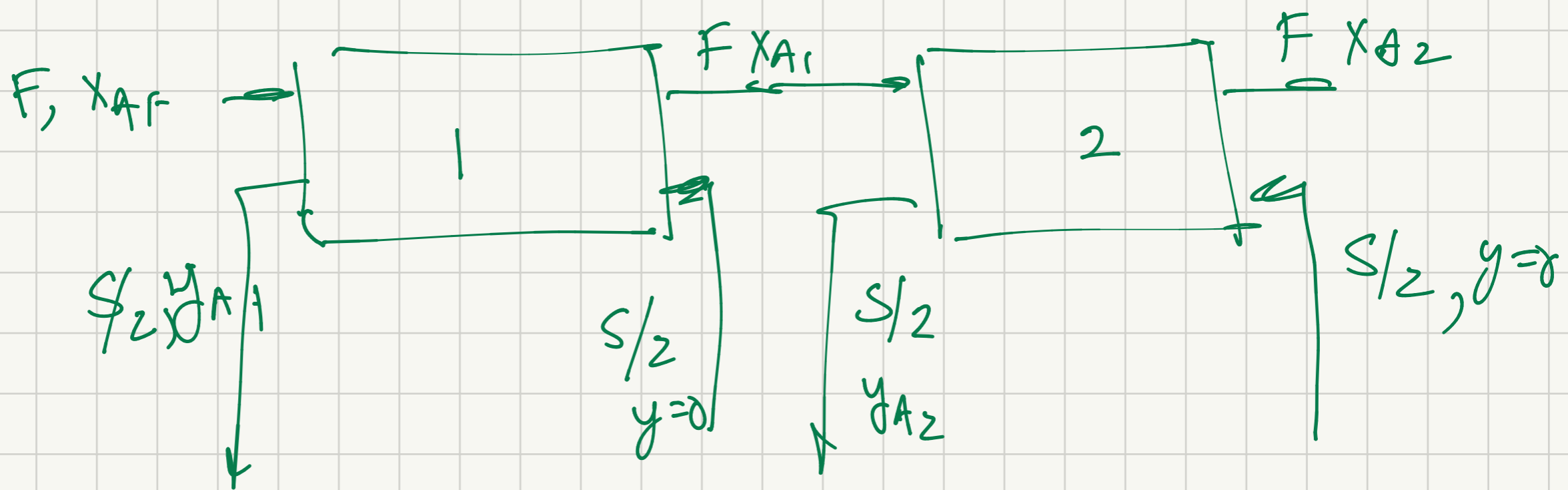
'BIGGER' IS BETTER

$$\xi = 1 + \Lambda$$



m MAY BE FIXED BY CHEMISTRY
OTHER WISE MUST INCREASE S.!!

SUPPOSE



①

$$F x_{AF} = F x_{A1} + \frac{S}{2} y_{A1}$$

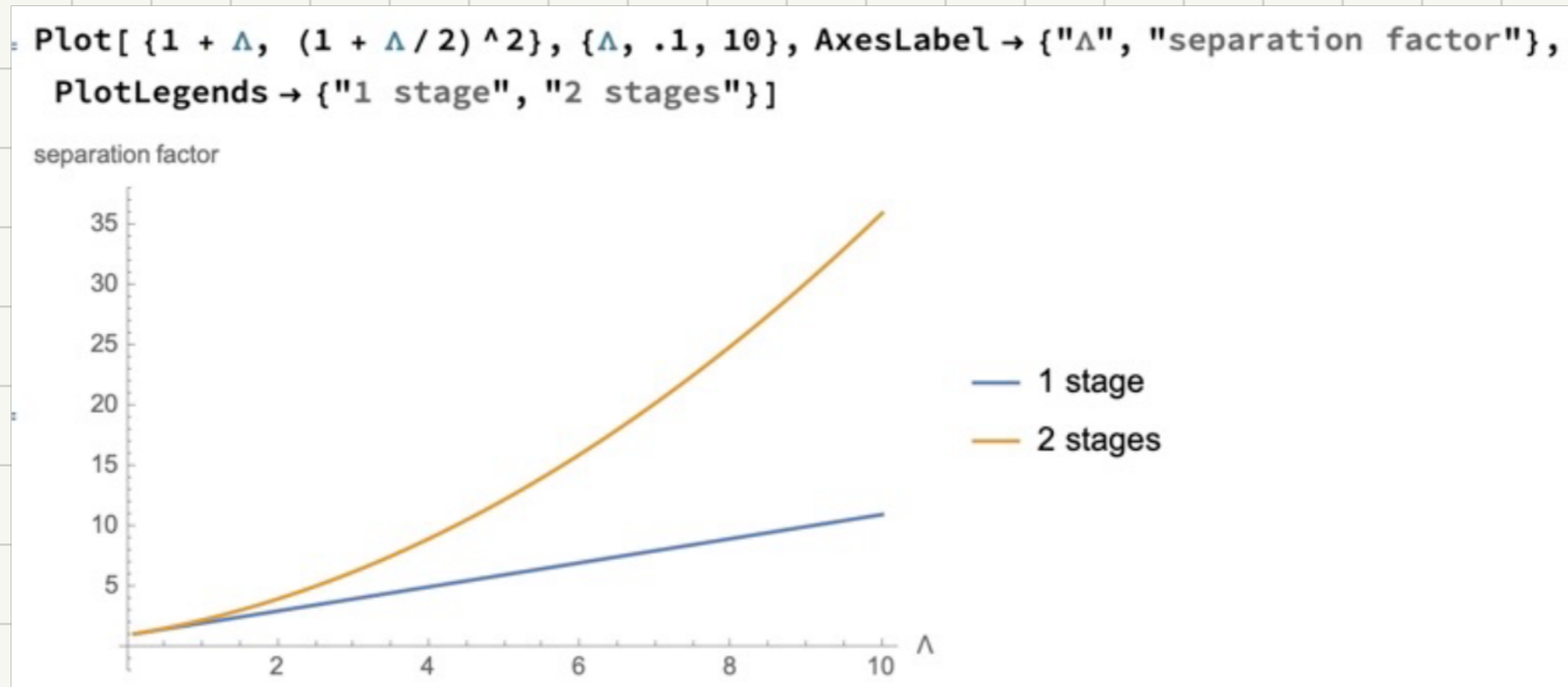
$$y = m x$$

②

$$F x_{A1} = F x_{A2} + \frac{S}{2} y_{A2}$$

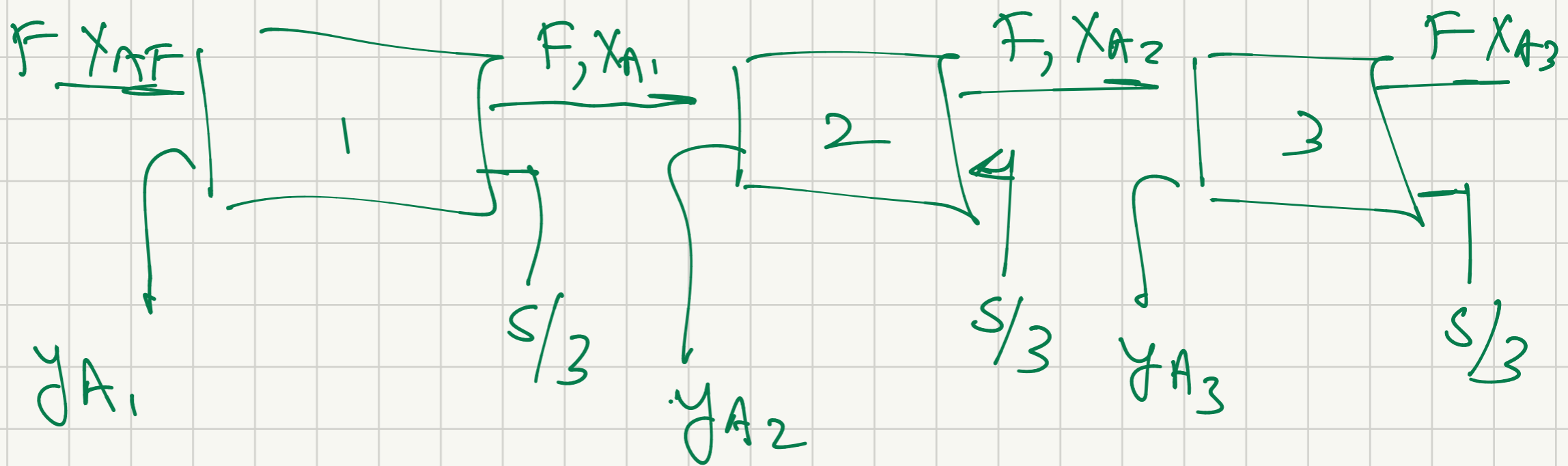
$$\xi_2 = \left(1 + \frac{\Delta}{2}\right)^2$$

TWO STAGES IS BETTER



HOW ABOUT 3...

CROSS
CURRENT



$$F_{X_{AF}} = F_{X_{A_1}} + y_{A_1} \frac{S}{3}$$

$$F_{X_{A_1}} = F_{X_{A_2}} + y_{A_2} \frac{S}{3}$$

$$F_{X_{A_2}} = F_{X_{A_3}} + y_{A_3} \frac{S}{3}$$

$$\xi_3 = \frac{X_{AF}}{X_{A_3}} = \left(1 + \frac{1}{3}\right)^3$$

WE CAN NOW GUESS...

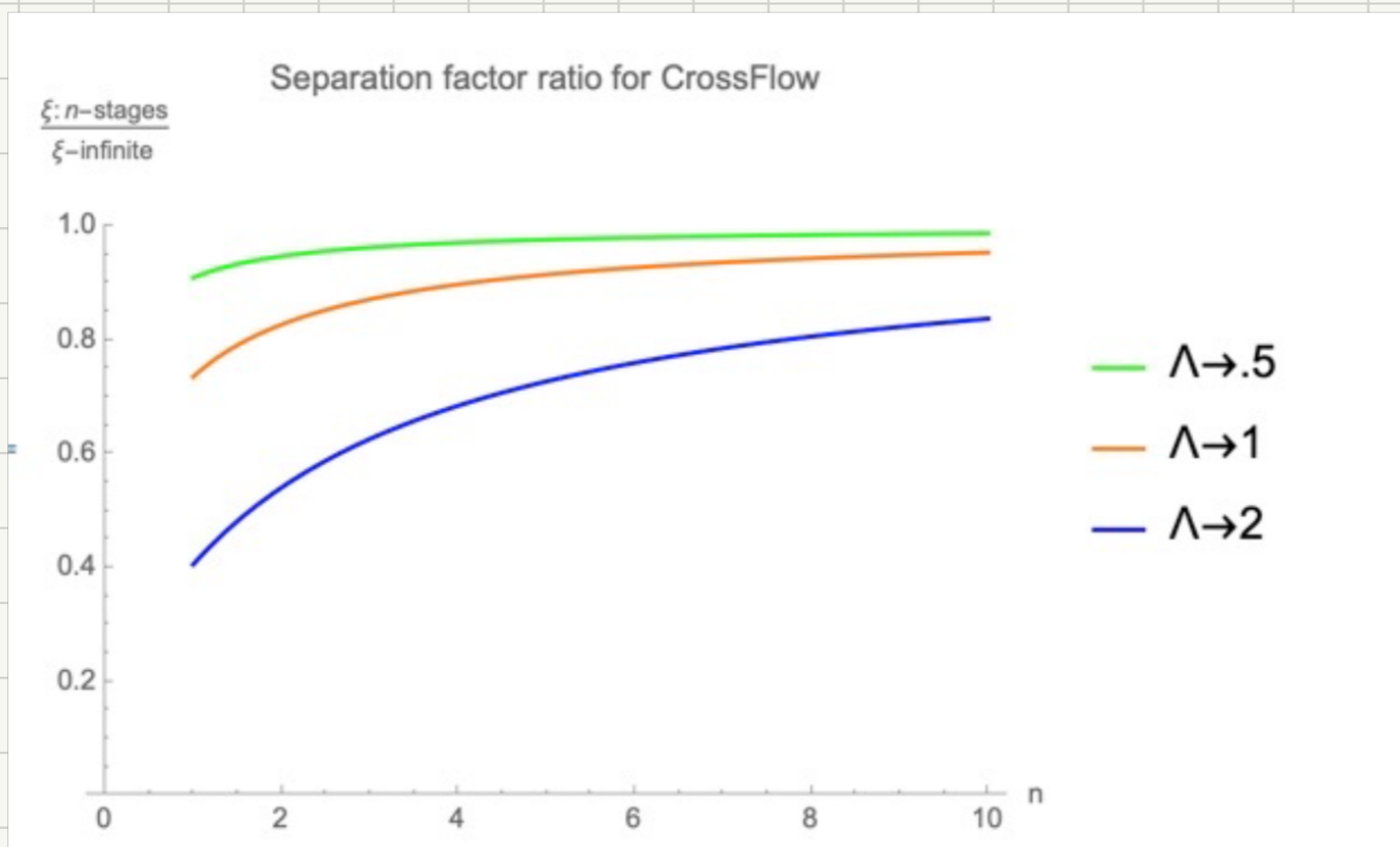
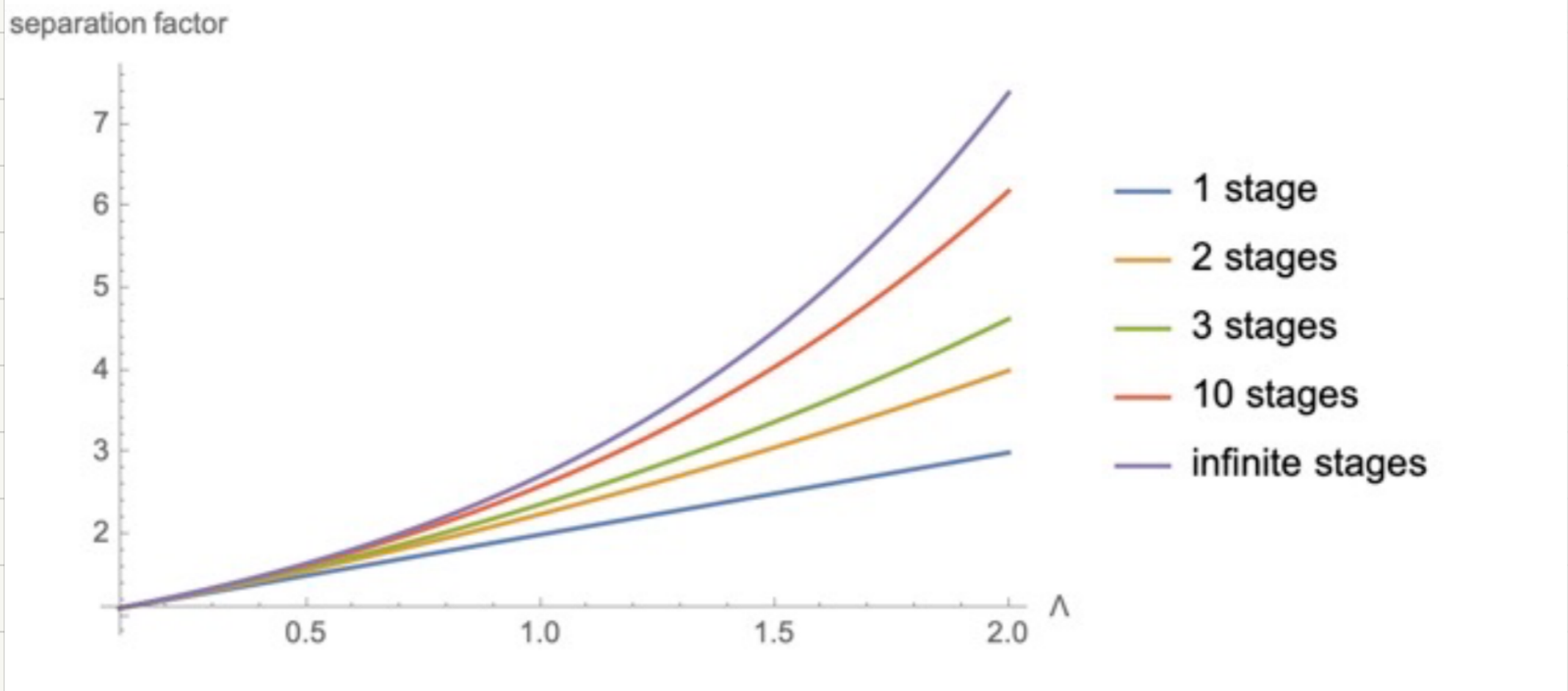
$$\xi_m = \left(1 + \frac{1}{n}\right)^m$$

As $n \rightarrow \infty$...

$$\xi_{\infty} = \text{Exp}(\Lambda)$$

WHICH SEEMS REALLY GOOD!!

```
Plot[ {1 + Δ, (1 + Δ/2)^2, (1 + Δ/3)^3, (1 + Δ/10)^10, Exp[Δ]}, {Δ}
AxesLabel -> {"Δ", "separation factor"},
PlotLegends -> {"1 stage", "2 stages", "3 stages", "10 stages", "infi
```

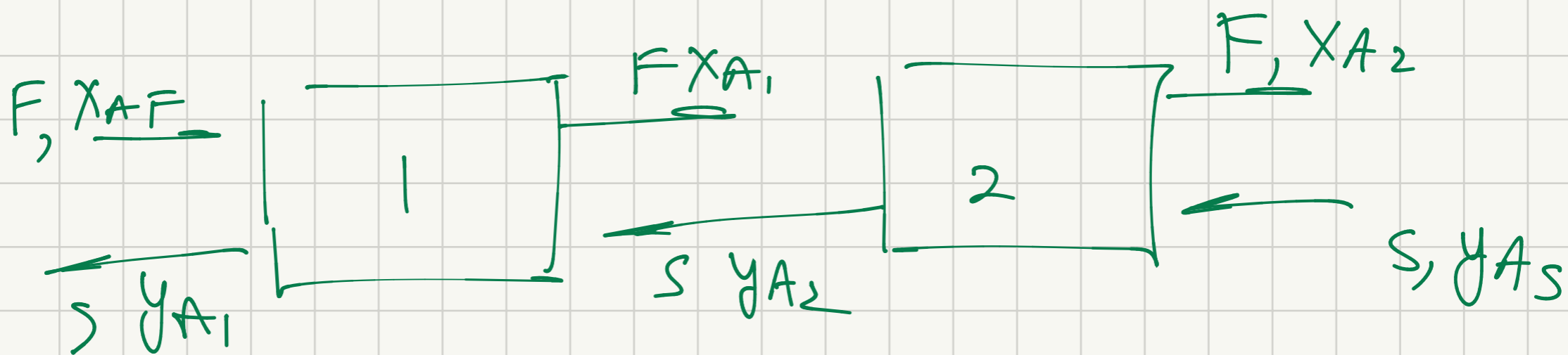


IF $\Lambda > 1$
 MORE
 STAGES
 HELPS
 FOR QUITE
 A LOT OF
 STAGES
 IF YOU NEED
 IT!!

HOWEVER... WE CAN DO
EVEN BETTER !!

(CAN AN EXPONENTIAL BE BEAT?)

COUNTER CURRENT



①

$$F X_{AF} + S y_{A2} = F X_{A1} + S y_{A1}$$

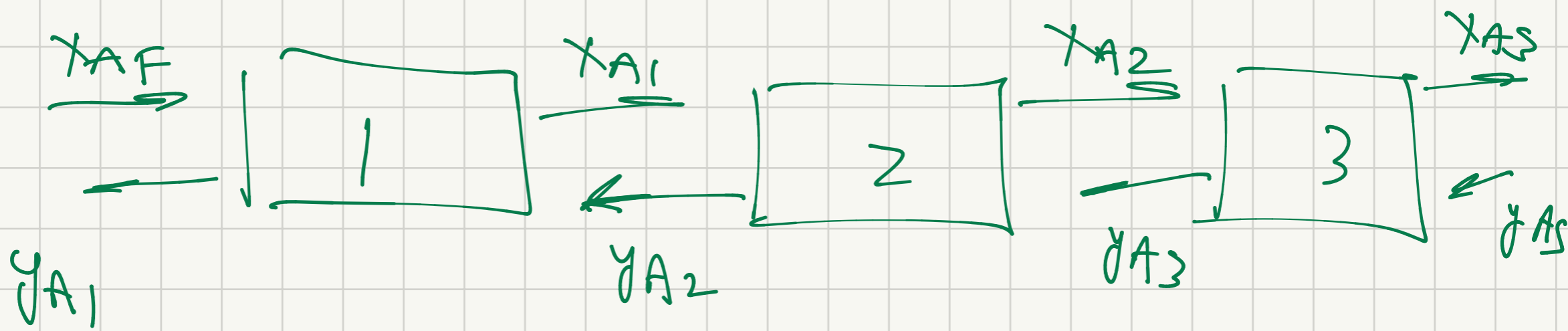
②

$$F X_{A1} + S y_{AS} = F X_{A2} + S y_{A2}$$

$$X_{A2} = \frac{X_{AF}}{1 + \Lambda + \Lambda^2}$$

$$y_{A2} = \frac{y_{AS}}{1 + \Lambda + \Lambda^2}$$

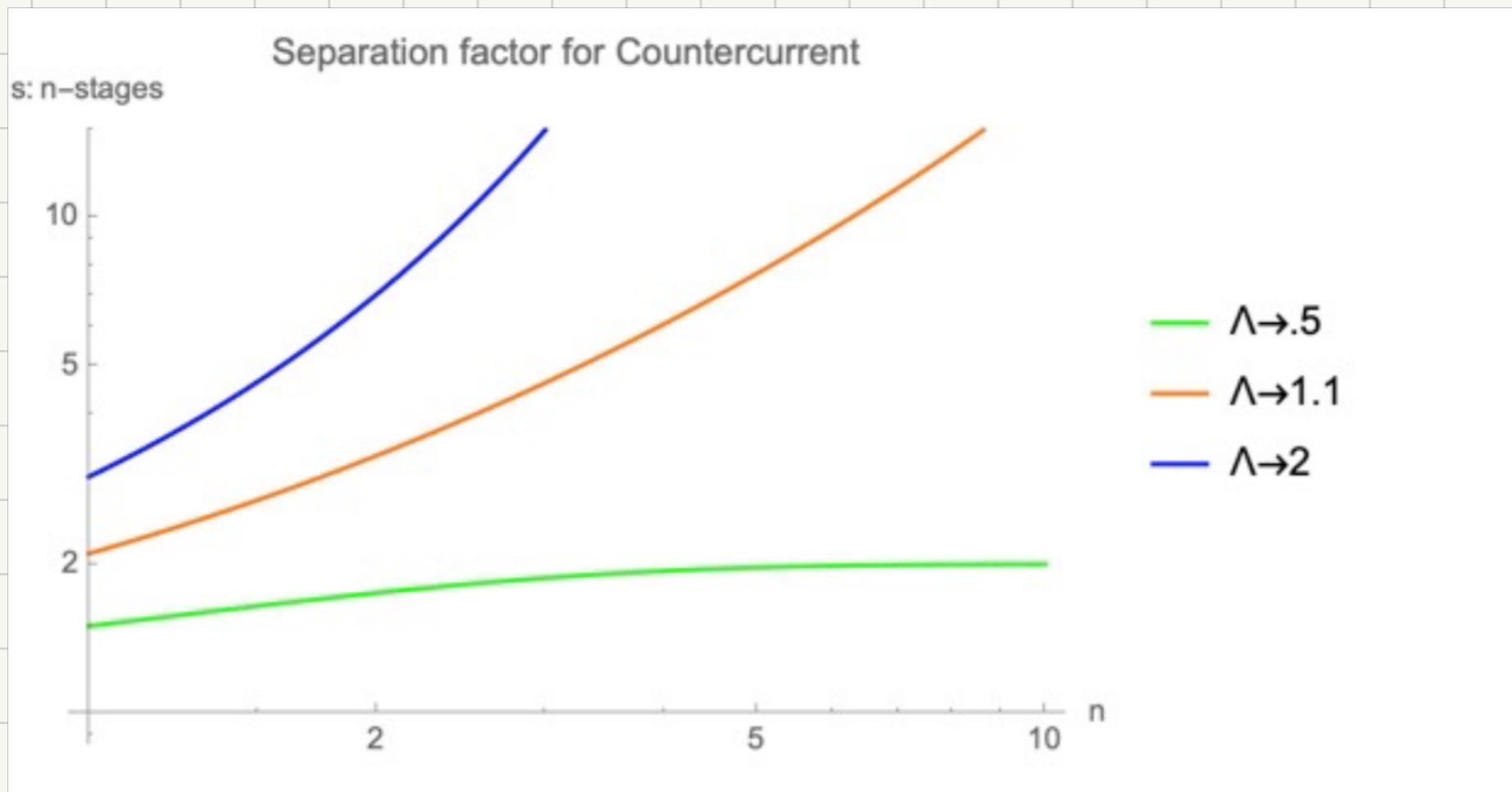
LET'S CHECK 3



$$\frac{X_{A3}}{X_{AF}} = \frac{1}{1 + \Lambda + \Lambda^2 + \Lambda^3}$$

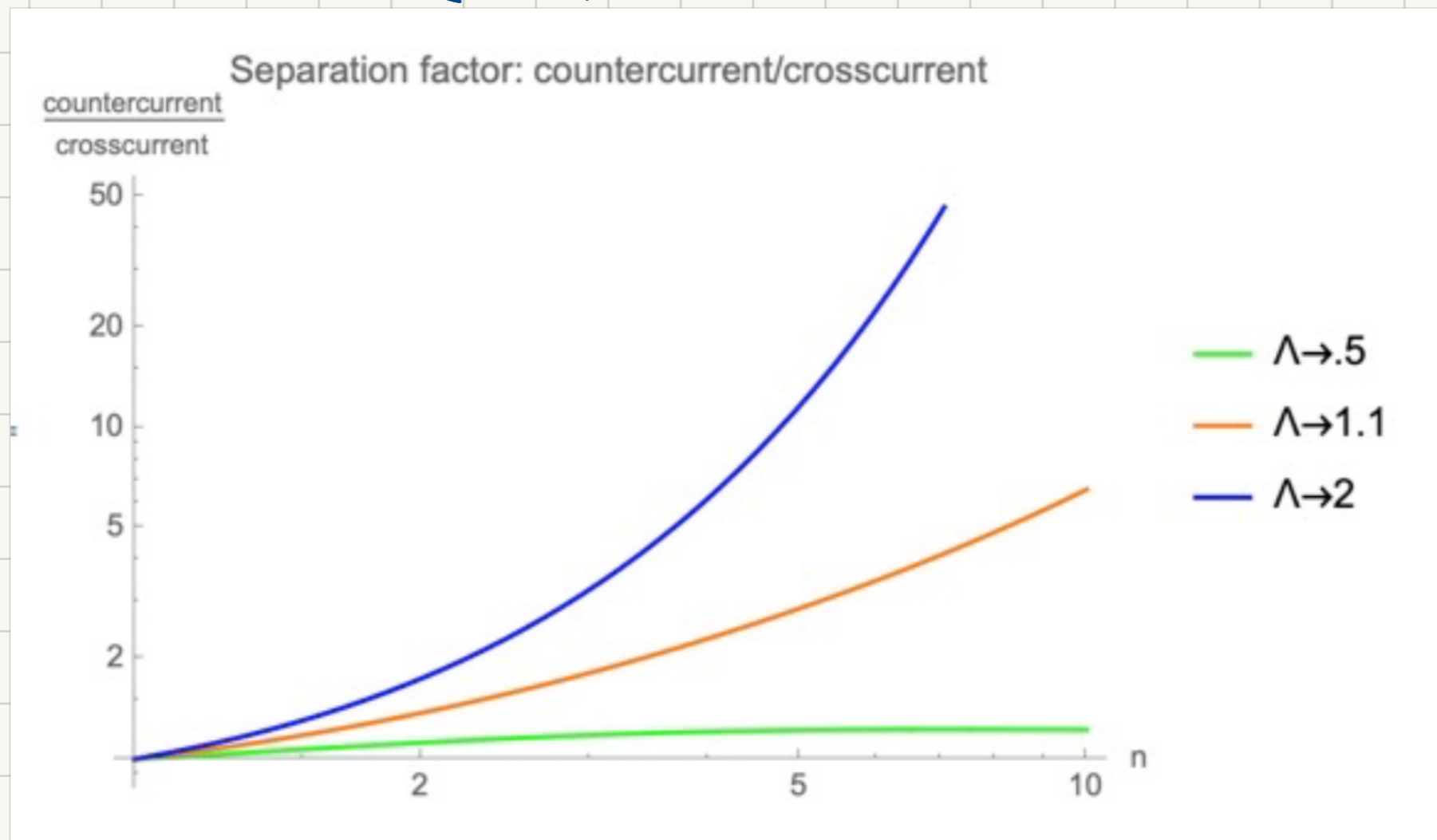
SO WE HAVE

$$\xi_m = \sum_{i=0}^m \Lambda^i$$



IF $\Lambda > 0$
CAN GET
AS LARGE
OF ξ
AS YOU
NEED

WE COMPARE CROSS CURRENT TO COUNTERCURRENT...



IF $\Lambda > 1$, SUBSTANTIAL BENEFIT

CROSS CURRENT $\xi_{\infty} = \exp(\Lambda)$

IF Λ IS LIMITED, ξ IS LIMITED

COUNTERCURRENT

$$\xi_{\infty} = \sum_{i=0}^{\infty} \Lambda^i$$

IF $\Lambda > 1$

ξ IS UNLIMITED.

SO ALMOST ALWAYS... COUNTERCURRENT.

KEY DIMENSIONLESS PARAMETER:

$$\Lambda \equiv \frac{mS}{F}$$

$$\xi_n = \sum_{i=0}^n \Lambda^i$$

$$\xi_n = \frac{\Lambda^{n+1} - 1}{\Lambda - 1}$$

$$n = \frac{\ln(1 + (\Lambda - 1)\xi_n)}{\ln(\Lambda)} - 1$$

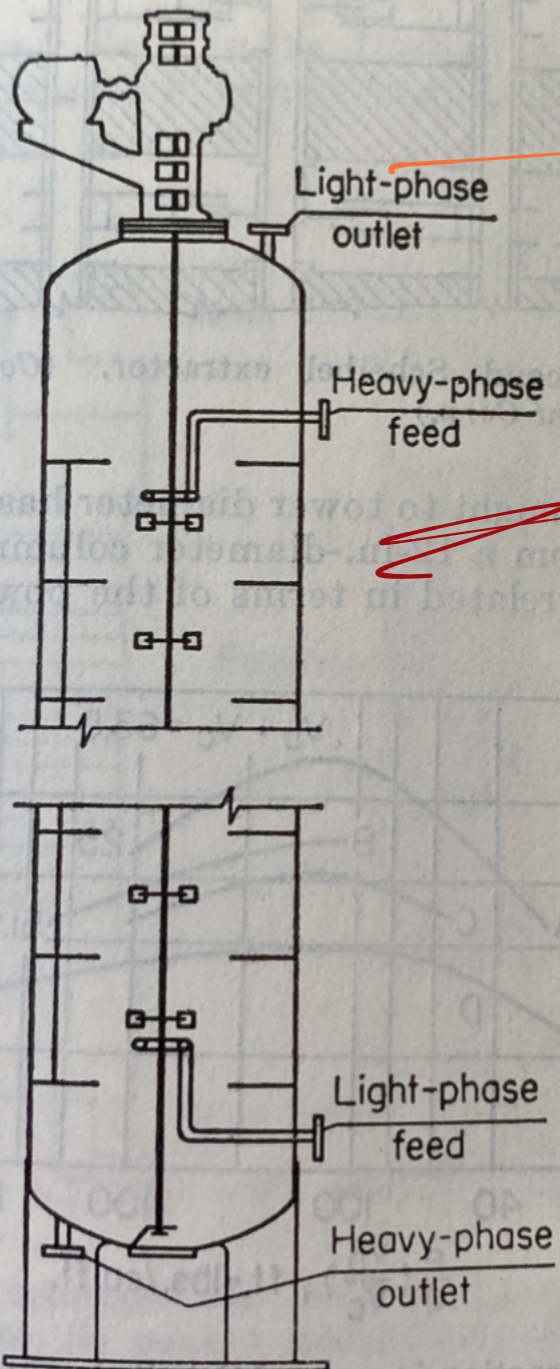
KREMSER EQ

EXTRACTION COLUMN

Mixco (Lightnin CMContactor) (Oldshue-Rushton) Column.

REFERENCES: Oldshue and Rushton, *Chem. Eng. Progress*, 48, 297 (1952). Dykstra, Thompson, and Clouse, *Ind. Eng. Chem.*, 50, 161 (1958). Gustison, Treybal, and Capps, *Chem. Eng. Progress, Symp. Ser.*, in press.

Refer to Fig. 21-47. The extractor is an extension of the simple baffled mixing vessel into a multistage column.



H.E.T.S., ft.
0.9
0.8
0.7
0.6
0.5
0.4
0.3
0.2
0.1

Fig. 21-4
ketone-ac
X = floo

[Data of C

A som
Eguchi,
20, 2 (1
(1957);
is chara
between
centric
column,
($V_c =$
fraction

Sche

REFER
1958; Br
771 (194
Eng. Ch

MAYBE,
EVAPORATE
SOLVENT
CRYSTALLIZE
PRODUCT

PROBABLY
NEVER
ACCUMULATION
IN EQ.

PLUS NEVER
ALLOWED
TO
SEPARATE
INTO
PHASES

Fig. 21-47. Mixco (Oldshue-Rushton) extractor.

Although commercial application has been made, data are scarce and limited to towers of small diameter. The preferred proportions are $Z = 0.5T$, $d_c > d_i$.

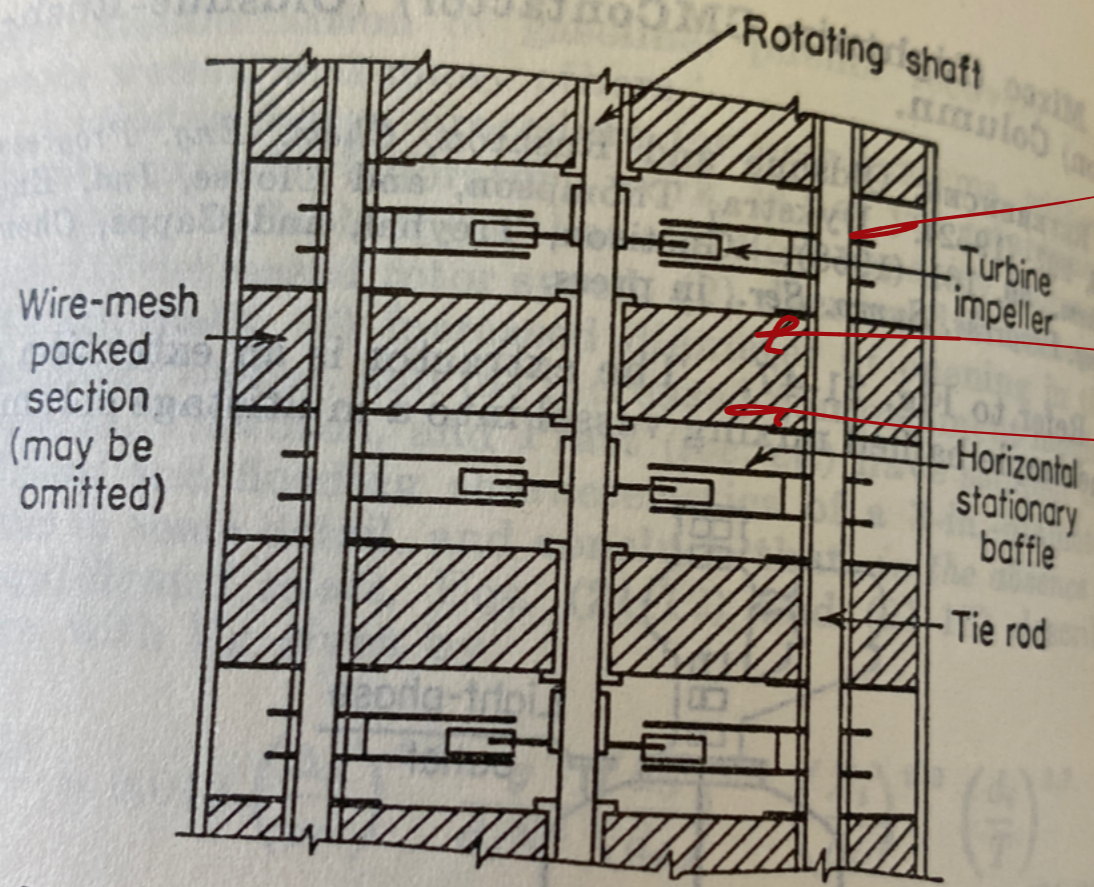
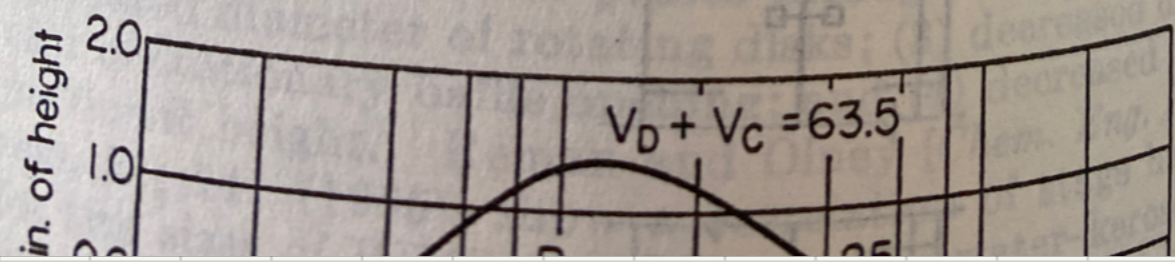


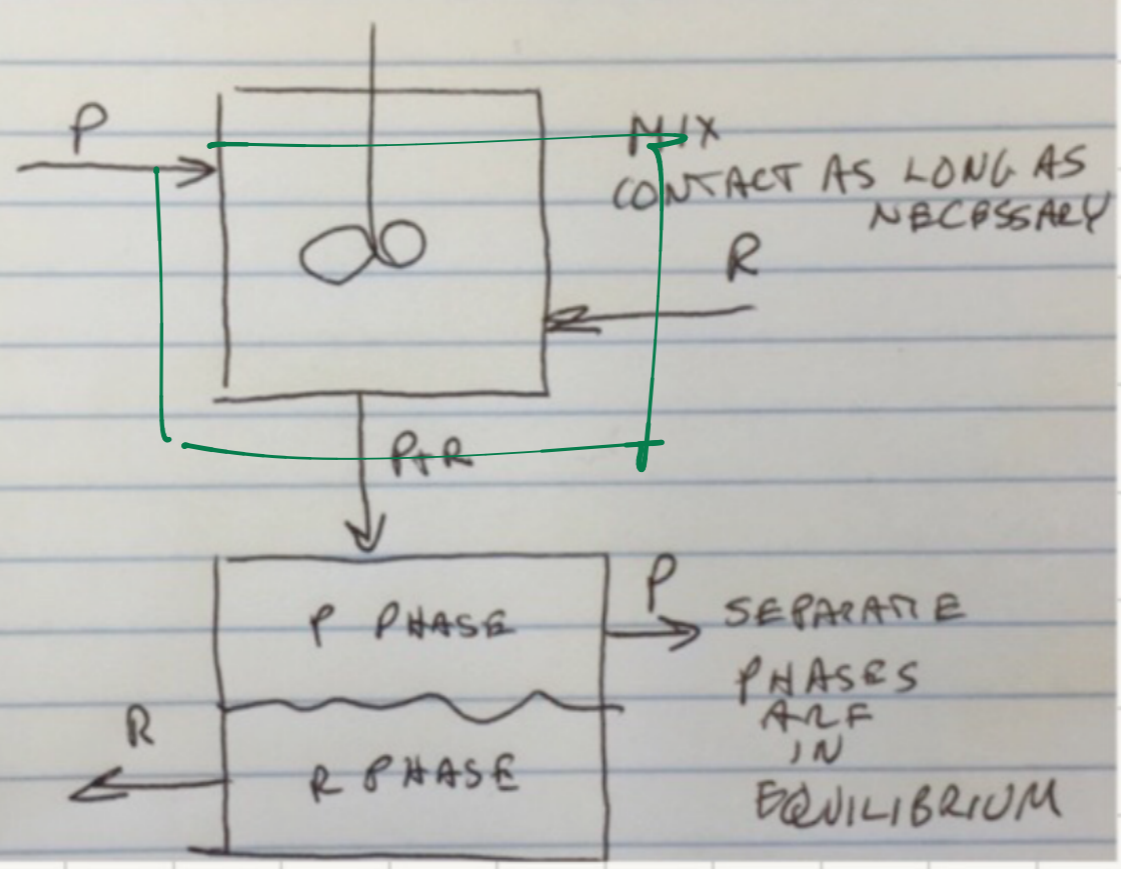
FIG. 21-51. Second Scheibel extractor. (Courtesy of York Process Equipment Corp.)

compartment height to tower diameter has been reduced. Data taken from a 12-in.-diameter column are shown in Fig. 21-52, correlated in terms of the power applied per



MIXING
SETTLING

SCHEMATIC OF EQUILIBRIUM STAGE



IDEALLY AN EXTRACTOR LOOKS MORE LIKE THIS...

FOR DISTILLATION

EACH TRAY COULD BE CLOSE TO EQUILIBRIUM

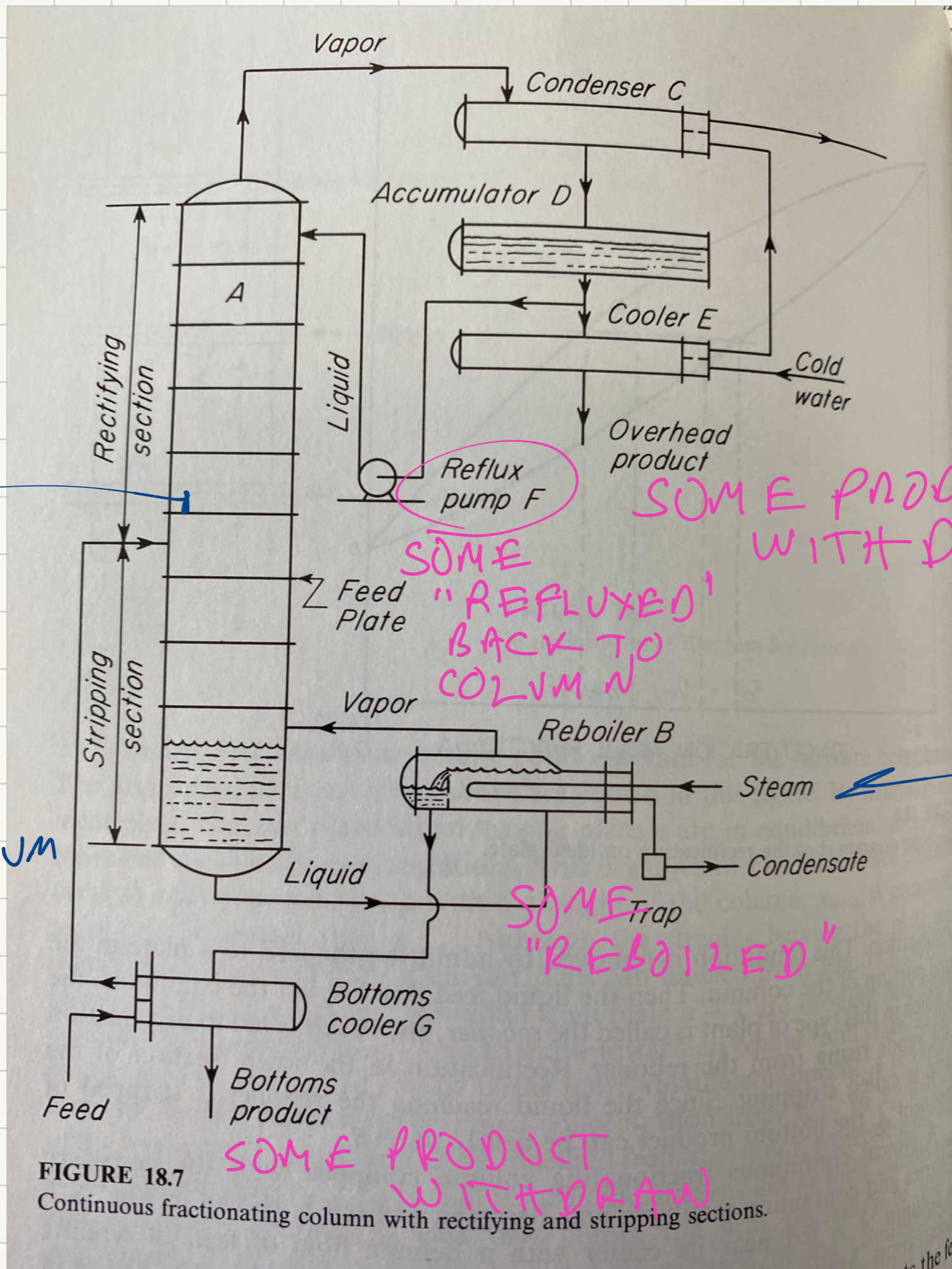


FIGURE 18.7 Continuous fractionating column with rectifying and stripping sections.

SOME PRODUCT WITHDRAWN

SOME "REFLUXED" BACK TO COLUMN

SOME "REBOILED"

SOME PRODUCT WITHDRAWN

HEAT IN PROVIDES ENERGY TO ALLOW SEPARATION

INNERENT TRADE OFF BETWEEN # TRAYS & RATE OF HEATING

CAPITAL COSTS

OPERATING COSTS

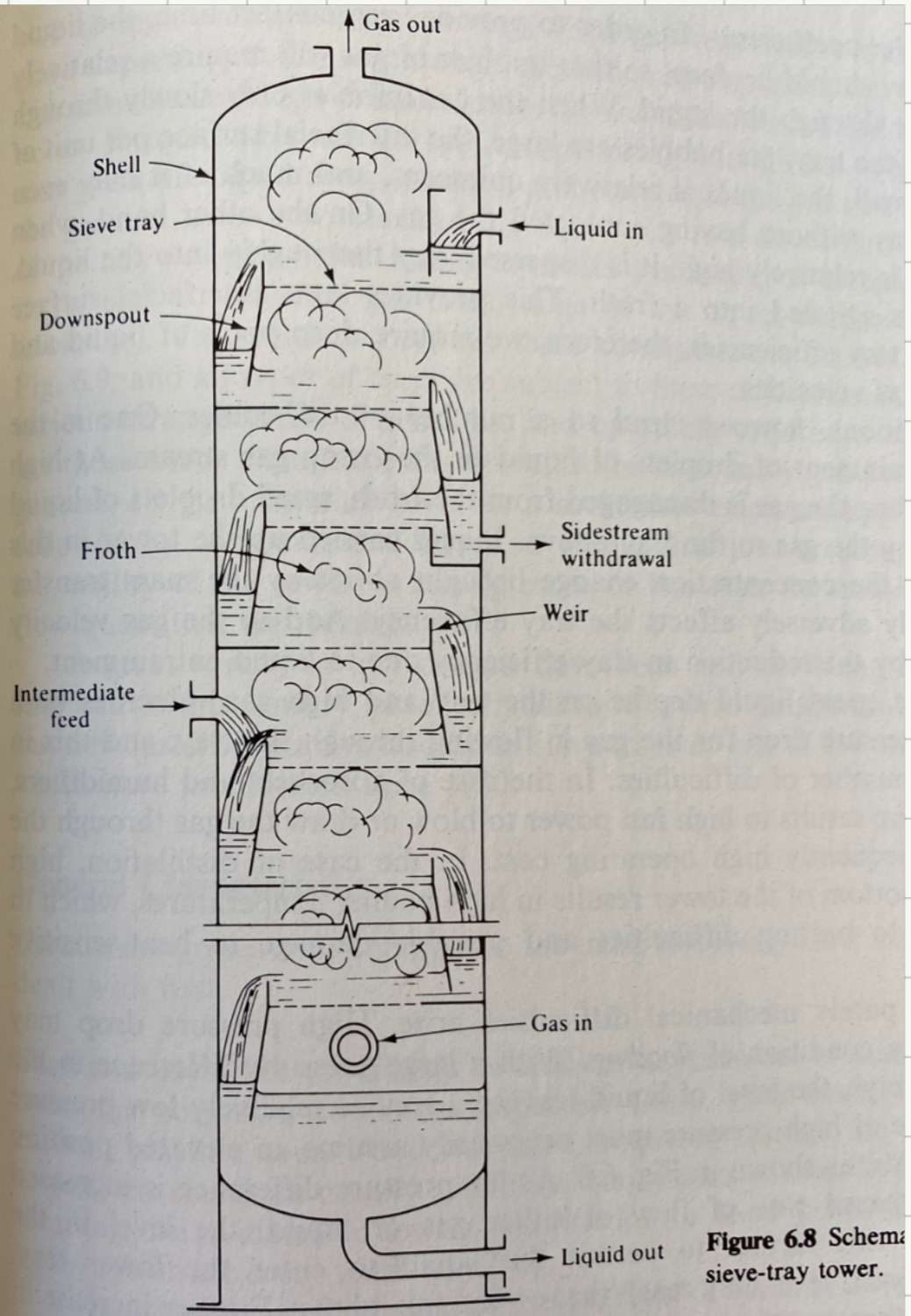
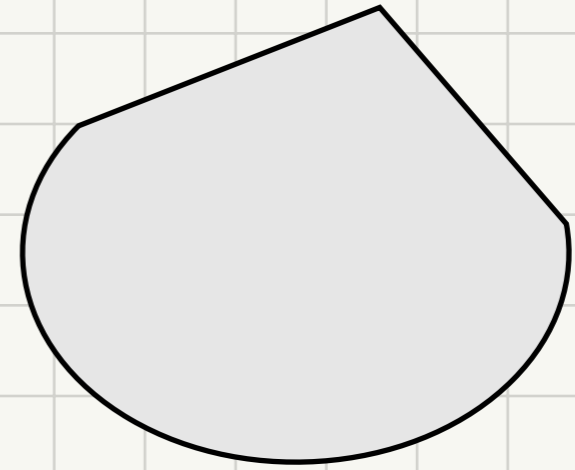


Figure 6.8 Schematic sieve-tray tower.

the mechanical design used and the conditions of operation. The tower, on the other hand, depends upon the quantities of liquid through the tray. Once the number of equilib

FLOWS WITHIN A COLUMN



SIEVE TRAY

BOILING MIXTURE

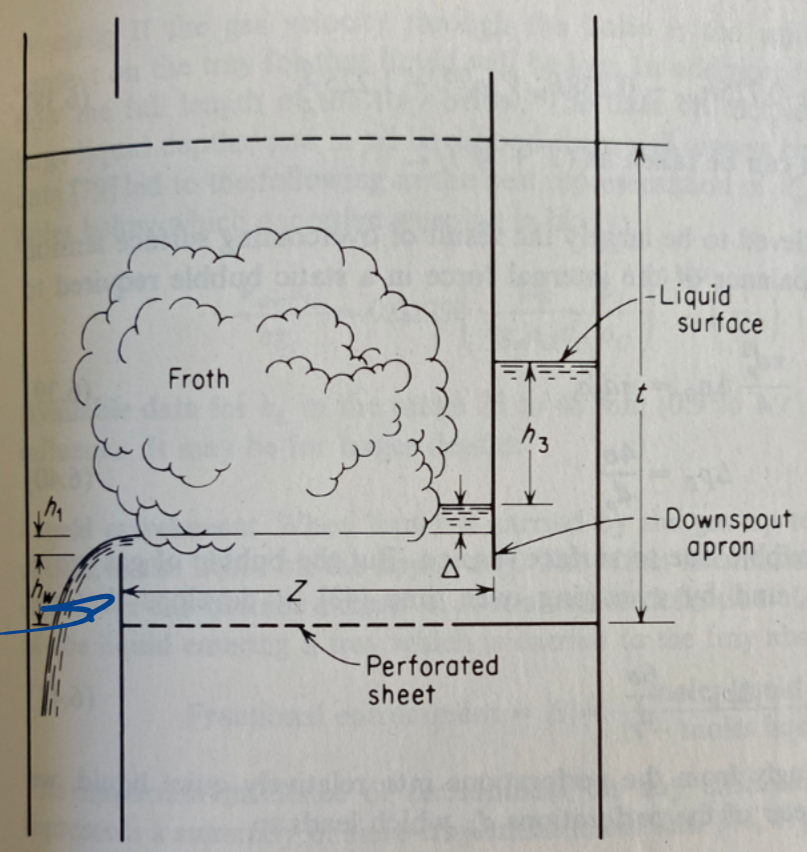


Figure cross-f

thickness, and an exit loss [64]

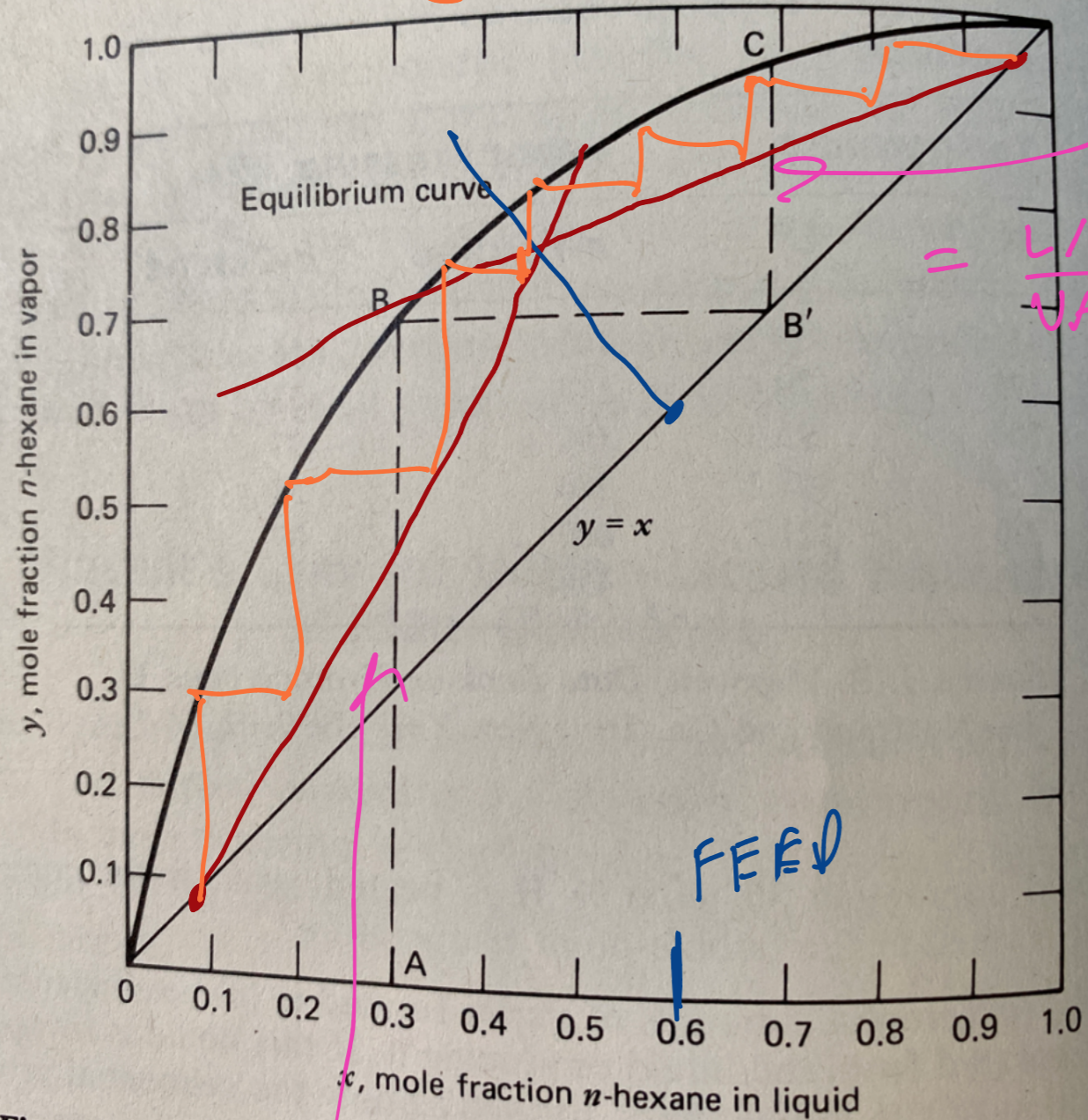
$$\frac{2h_D g \rho_L}{V_o^2 \rho_G} = C_o \left[0.40 \left(1.25 - \frac{A_o}{A_n} \right) + \frac{4lf}{d_o} + \left(1 - \right. \right.$$

The Fanning friction factor f is taken from a standard chart [15]. C_o depends upon the ratio of plate thickness to hole diameter [82]. Over

$$C_o = 1.09 \left(\frac{d_o}{l} \right)^{0.25}$$

Thermodynamic Equilibrium Diagrams

8-TRAYS



FROM THIS
y-x DIAGRAM
AND MASS
BALANCES

SLOPE
= LIQUID FLOW
VAPOR FLOW

FEED

McCABE-THIELE

METHOD

WE TOOK A
FEED OF

$$x_H = .6$$

AND SEPARATED
IT INTO

$$x_H = .95$$

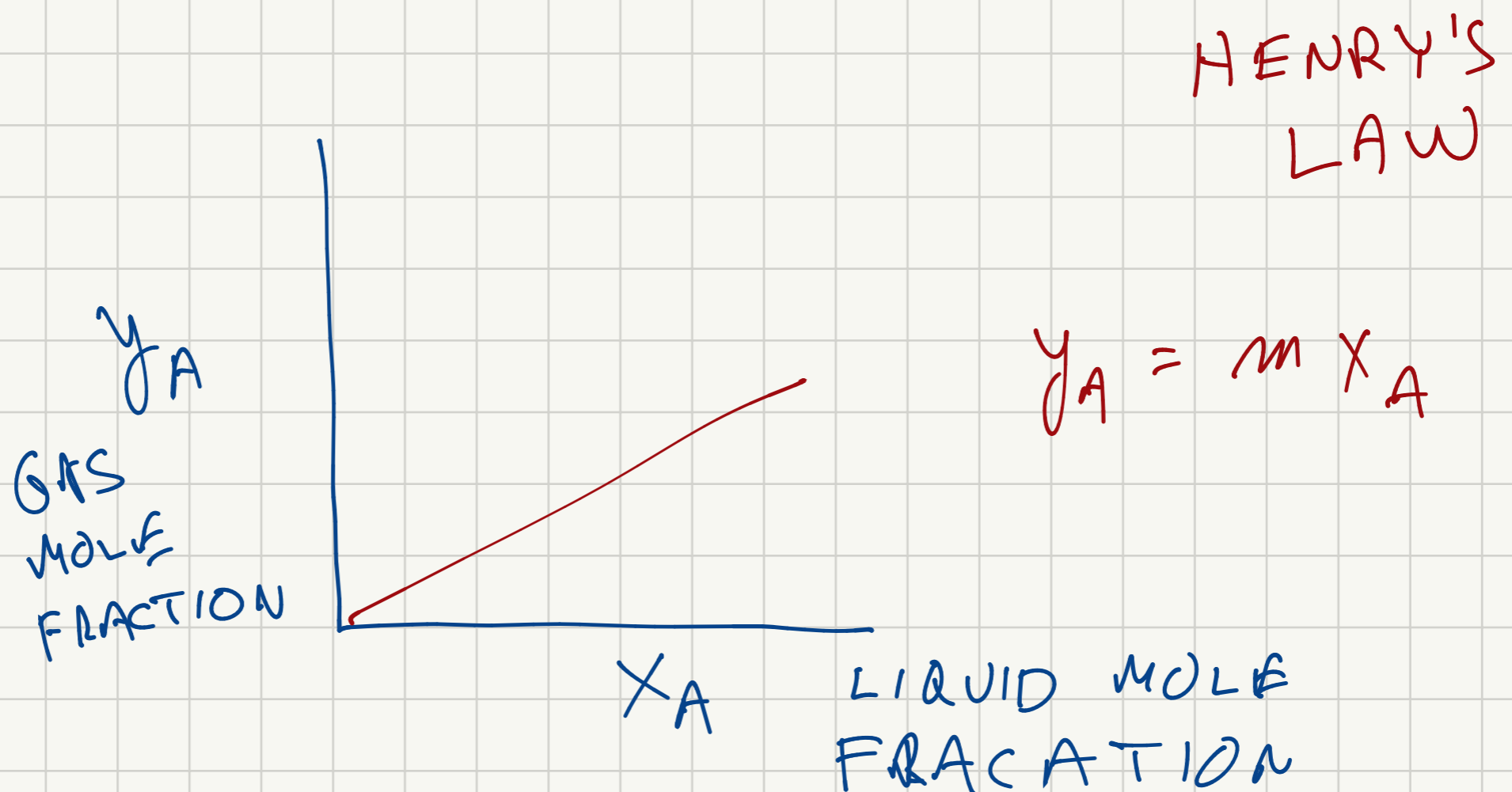
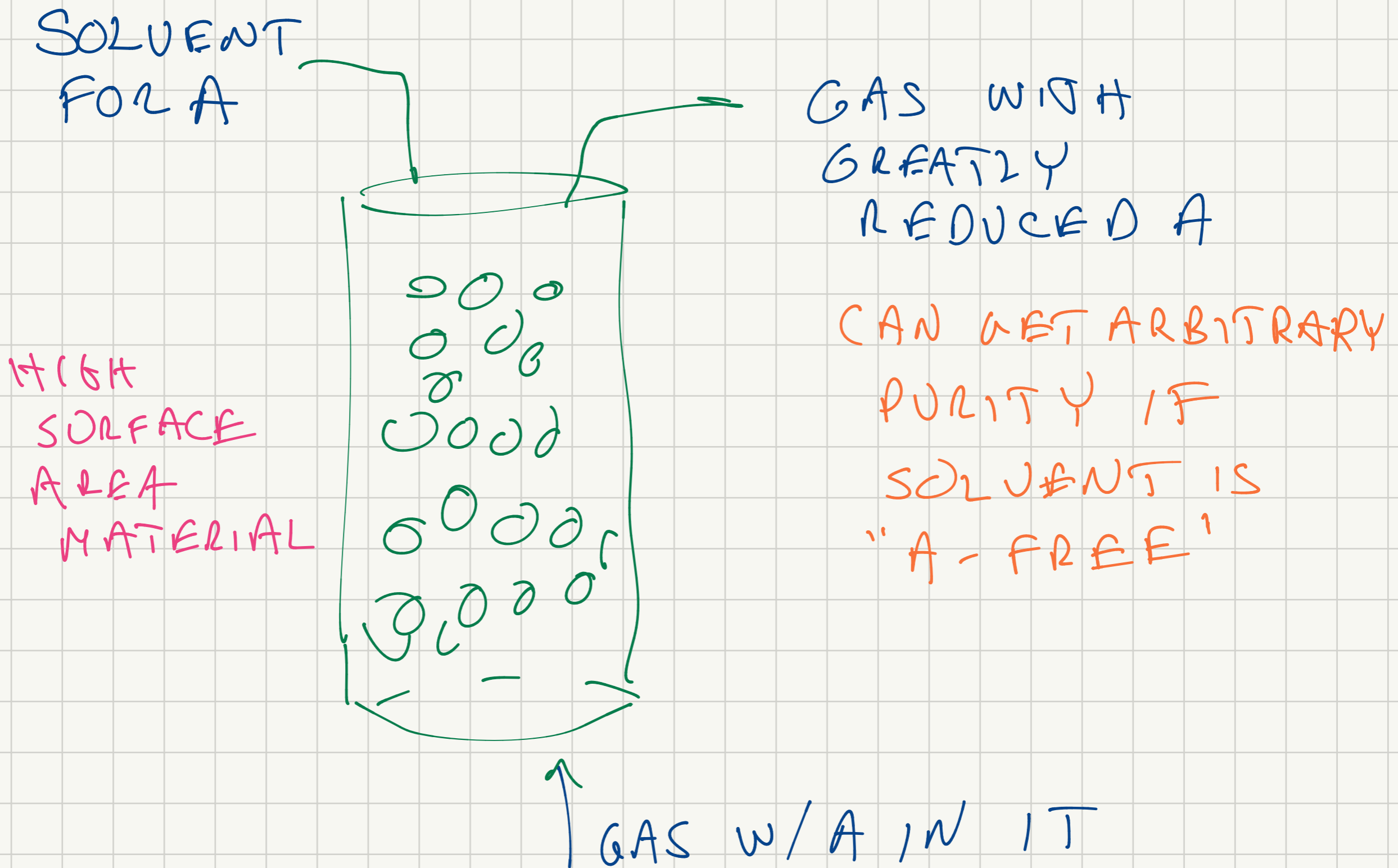
$$x_H = .1$$

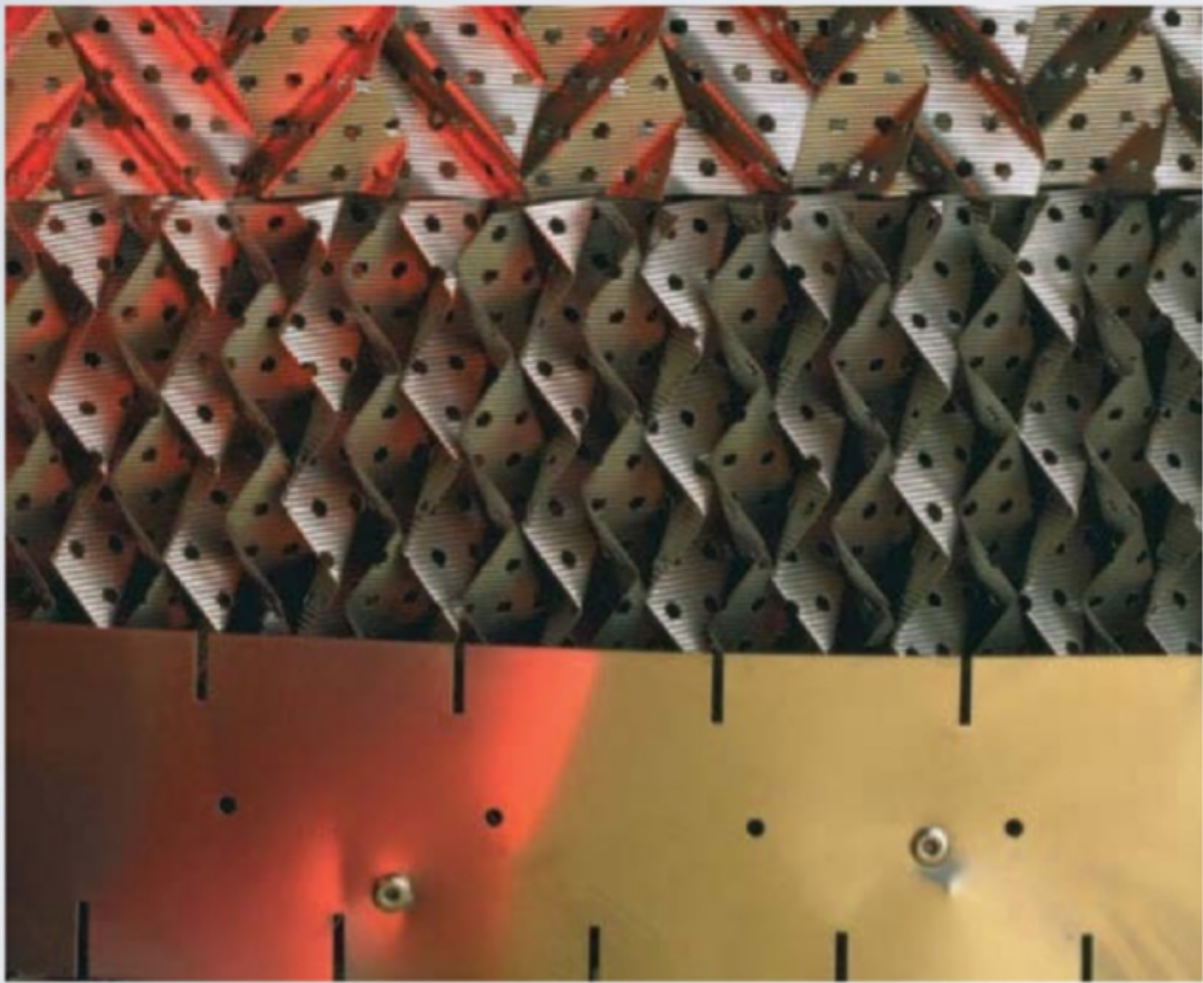
USING 8
EQUILIBRIUM
STAGES

Figure 3.3. The x-y diagram for n-hexane-n-octane, at 101 kPa. (E. J. Henley and E. M. Rosen, *Material and Energy Balance Computations*, John Wiley & Sons, New York, © 1969.)

COMPONENT MASS BALANCE
GIVES "OPERATING" LINE

AS IT TURNS OUT, YOU
DON'T ACTUALLY HAVE TO
USE EQUILIBRIUM STAGES.





Structured

"DUMPED" PACKING

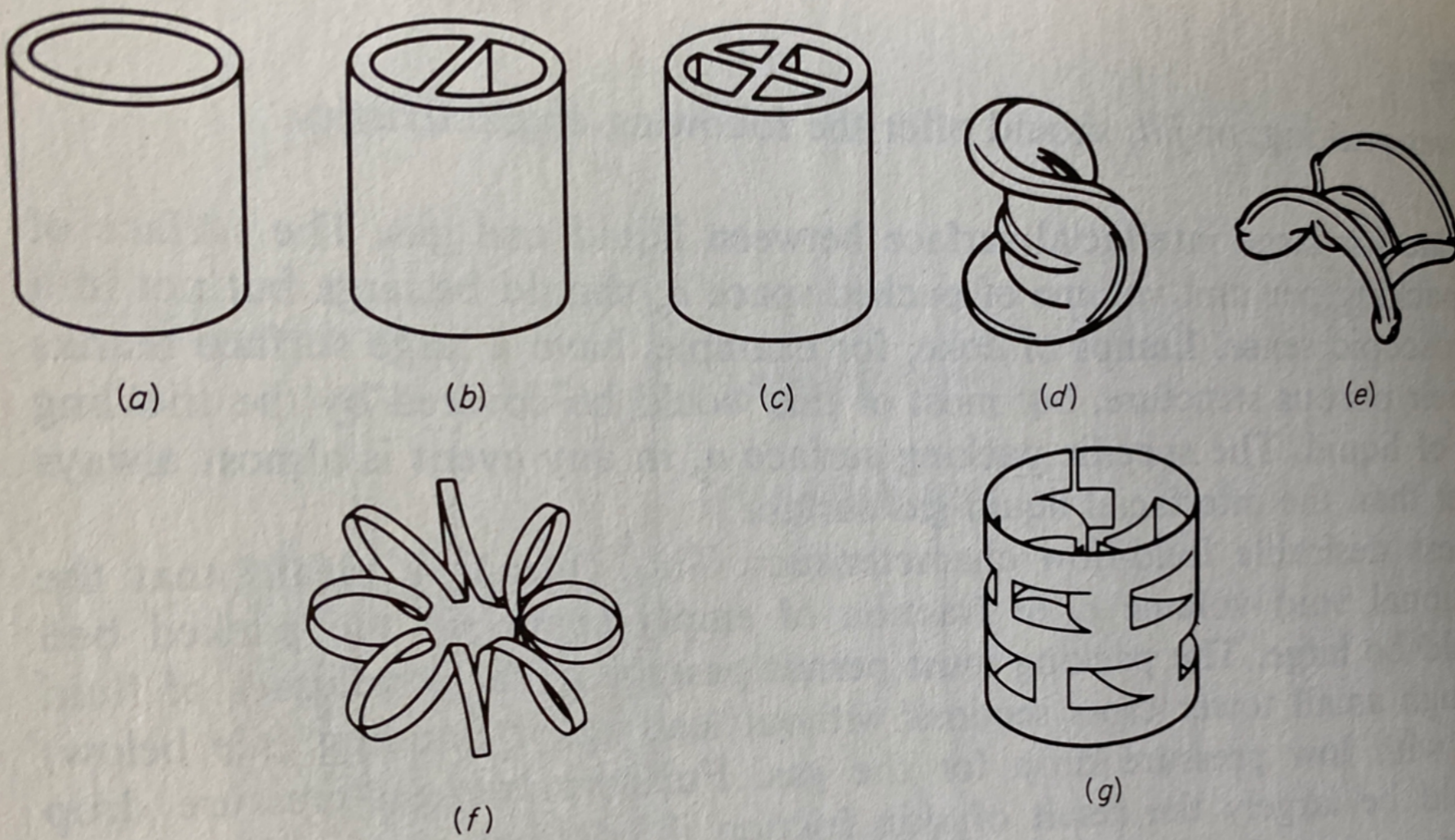


Figure 6.28 Some random tower packings: (a) Raschig rings, (b) Lessing ring, (c) partition ring, (d) Berl saddle (courtesy of Maurice A. Knight), (e) Intalox saddle (Chemical Processing Products Division, Norton Co.), (f) Tellerette (Ceilcote Company, Inc.), and (g) pall ring (Chemical Processing Products Division, Norton Co.).

ings offer larger specific surface (and

A IS KEY DIMENSIONLESS
 PARAMETER $A \equiv \frac{L}{mG}$

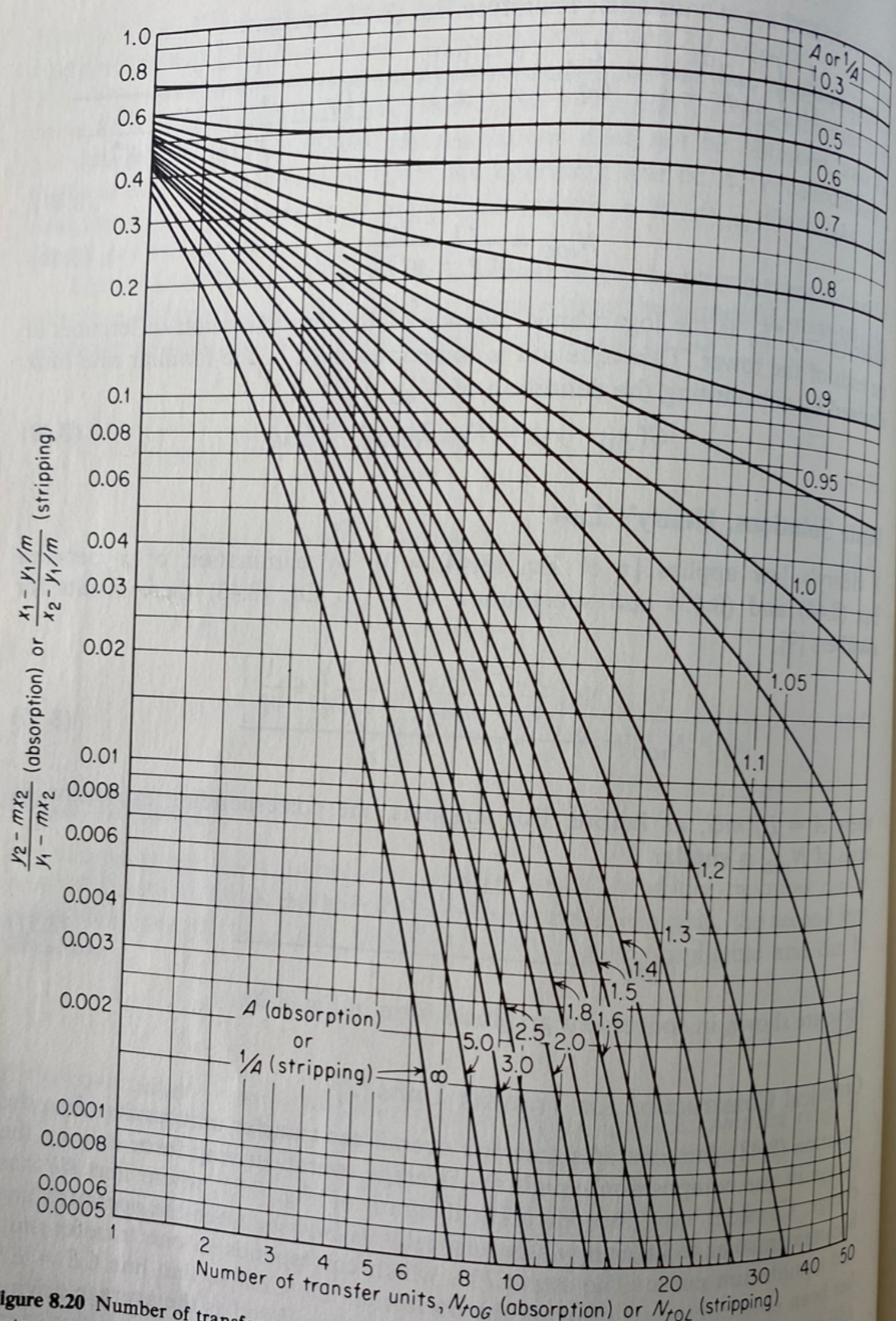


Figure 8.20 Number of transfer units for absorbers or strippers with constant absorption or stripping factor.

N_{TOG}

$$Z = N_{TOG} H_{OG}$$

$$H_{OG} = \frac{G}{\text{RATE OF MASS TRANSFER}}$$

UNIT OPERATIONS

GAS ABSORBER

THE GAS ABSORBER IN THE IMPERIAL COLLEGE PILOT USES AN MEA IN WATER LIQUID TO ABSORB CO_2 FROM A MIXTURE IN N_2

ABSORBER AND STRIPPER



Structured



Both give: Random

- high surface area between liquid and gas ($350 \text{ m}^2/\text{m}^3$)
- continuous mixing of liquid and gas and they flow through column
- high fraction of "void" space so that the pressure drop is low