

CBE 40445

9/30/20

# FURTHER EXAMINATION OF MASS TRANSFER RESISTANCE IN HETEROGENEOUS CATALYSIS

- COMBINED EXTERNAL  
INTERNAL RESISTANCE FROM  
A "THEORETICAL" PERSPECTIVE
- EFFECT OF MASS TRANSFER  
RESISTANCE ON OBSERVED  
KINETICS

BUT FIRST A TOPIC THAT  
I ENCOUNTERED (AGAIN)

## ORIGINAL (ANTIGENIC) SIN

→ POTENTIAL THAT A PREVIOUS  
ENCOUNTER WITH A PATHOGEN  
AFFECTS YOUR IMMUNESYSTEM  
IN SUCH A WAY AS TO  
REDUCE YOUR ABILITY TO  
FIGHT THE NEXT  
PATHOGEN

— CURRENT ISSUE, WOULD  
THE LATEST FLU VACCINE  
DO THIS RE COVID-19??

NO EVIDENCE OF THIS !!

## Antibody Dependent Enhancement Due to Original Antigenic Sin and the Development of SARS

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### Abstract

Go to:

Human coronavirus (HCoV) is one of the most common causes of respiratory tract infections throughout the world. Two phenomena observed so far in the development of the SARS-CoV-2 pandemic deserve further attention. First, the relative absence of clinical signs of infections in children, second, the early appearance of IgG in certain patients. From the point of view of immune system physiology, such an early rise of specific IgG is expected in secondary immune responses when memory to a cross-reactive antigen is present, usually from an earlier infection with a coronavirus. It is actually typical for the immune system to respond, to what it already knows, a phenomenon that has been observed in many infections with closely related viruses and has been termed "original antigenic sin." The question then arises whether such cross-reactive antibodies are protective or not against the new virus. The worst scenario would be when such cross-reactive memory antibodies to related coronaviruses would not only be non-protective but even enhance infection and the clinical course. Such a phenomenon of antibody dependent enhancement (ADE) has already been described in several viral infections. Thus, the development of IgG against SARS-CoV-2 in the course of COVID-19 might not be a simple sign of viral clearance and developing protection against the virus. On the contrary, due to cross-reaction to related coronavirus strains from earlier infections, in certain patients IgG might enhance clinical progression due to ADE. The patient's viral history of coronavirus infection might be crucial to the development of the current infection with SARS-CoV-2. Furthermore, it poses a note of caution when treating COVID-19 patients with convalescent sera.

WHY SOME  
PEOPLE  
GET REALLY  
SICK



## A Novel Hypothesis for Original Antigenic Sin in the Severe Disease of SARS-CoV-2 Infection

Heinz Kohler and Peter Nara

Published Online: 21 Aug 2020 | <https://doi.org/10.1089/mab.2020.0029>

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### Abstract

In this hypothesis, we address the biological/immunological pathway leading to severe disease or death after infection with severe acute respiratory syndrome coronavirus 2 (SARS-CoV-2). The underlying immune response is described with "original antigenic sin" (OAS) whereby previous infections influence the response to future virus encounters. We cite evidence for OAS-induced immunopathology in HIV-1 disease. We hypothesize that similar immune abnormalities can occur after infection with SARS-CoV-2. This hypothesis is supported by recent analysis of the antibodies in infected patients demonstrating serological and B cell abnormalities. The concept of symmetrical clonal regulation developed earlier for the immune network illustrates the pathway suggested by our hypothesis and may be helpful to develop strategies avoiding severe coronavirus disease 2019.

## Individualizing Risk Prediction for Positive Coronavirus Disease 2019 Testing

Results from 11,672 Patients

Lara Jehi, MD, MHCDS,<sup>a,\*</sup> Xinge Ji, MS,<sup>b</sup> Alex Milinovich, MS,<sup>b</sup> Serpil Erzurum, MD,<sup>c</sup> Brian P. Rubin, MD, PhD,<sup>d</sup> Steve Gordon, MD,<sup>e</sup> James B. Young, MD,<sup>f</sup> and Michael W. Kattan, PhD<sup>b</sup>

In the development cohort, 11,672 patients fulfilled study criteria, including 818 patients (7.0%) who tested positive for COVID-19; in the validation cohort, 2295 patients fulfilled criteria, including 290 patients who tested positive for COVID-19. Male, African American, older patients, and those with known COVID-19 exposure were at higher risk of being positive for COVID-19. Risk was reduced in those who had pneumococcal polysaccharide or influenza vaccine or who were on melatonin, paroxetine, or carvedilol. Our model had favorable discrimination (c-statistic = 0.863 in the development cohort and 0.840 in the validation cohort) and calibration. We present sensitivity, specificity, negative predictive value, and positive predictive value at different prediction cutoff points. The calculator is freely available at <https://riskcalc.org/COVID19>.

FLU SHOT  
REDUCED  
COVID-19  
CASES

DOES THIS  
GENERALIZE?

SORTING OUT SUCH QUESTIONS: SYSTEMS ENGINEERING

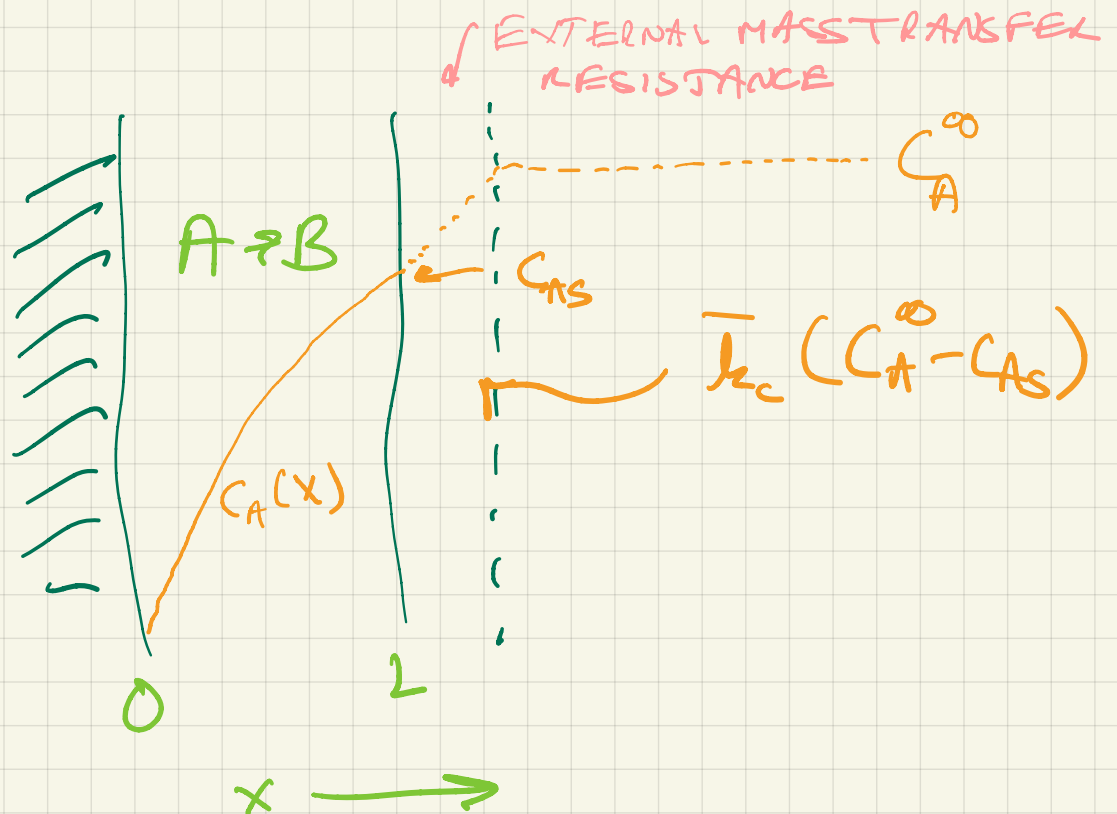
EXAMINATION OF COMBINED  
EXTERNAL + INTERNAL  
RESISTANCE FROM SOLUTIONS  
TO "EXACT" EQUATIONS

CONSIDER 1ST ORDER REACTION

SLAB GEOMETRY



$$r = k_c A$$



$$0 = D_{TA}^- \cdot \frac{\delta^2 C_A}{\delta X^2} - k C_A$$

SOLVE INSIDE PELLET

WITH A BOUNDARY CONDITION  
THAT ACCOUNTS FOR EXTERNAL  
MASS TRANSFER

$$\eta \equiv \frac{X}{L} \quad (0-1)$$

$$\Theta \equiv \frac{C_A}{C_{A0}}$$

$$\phi^2 \equiv \frac{h L}{D_{TA}^-}$$

REACTION RATE  
CONSTANT

$$Bi \equiv \frac{L \bar{h}_c}{D_{TA}^-}$$

MASS TRANSFER  
COEFFICIENT

$$0 = \frac{d^2\theta}{d\eta^2} - \phi^2\theta$$

$$\left. \frac{\partial\theta}{\partial\eta} \right|_{\eta=1} = -Bi(\theta(1) - 1)$$

FLUX INSIDE PELLET = FLUX TO SURFACE OF PELLET

$$\theta'(\eta=0) = 0$$

NO FLUX PAST THE "BOUNDARY"

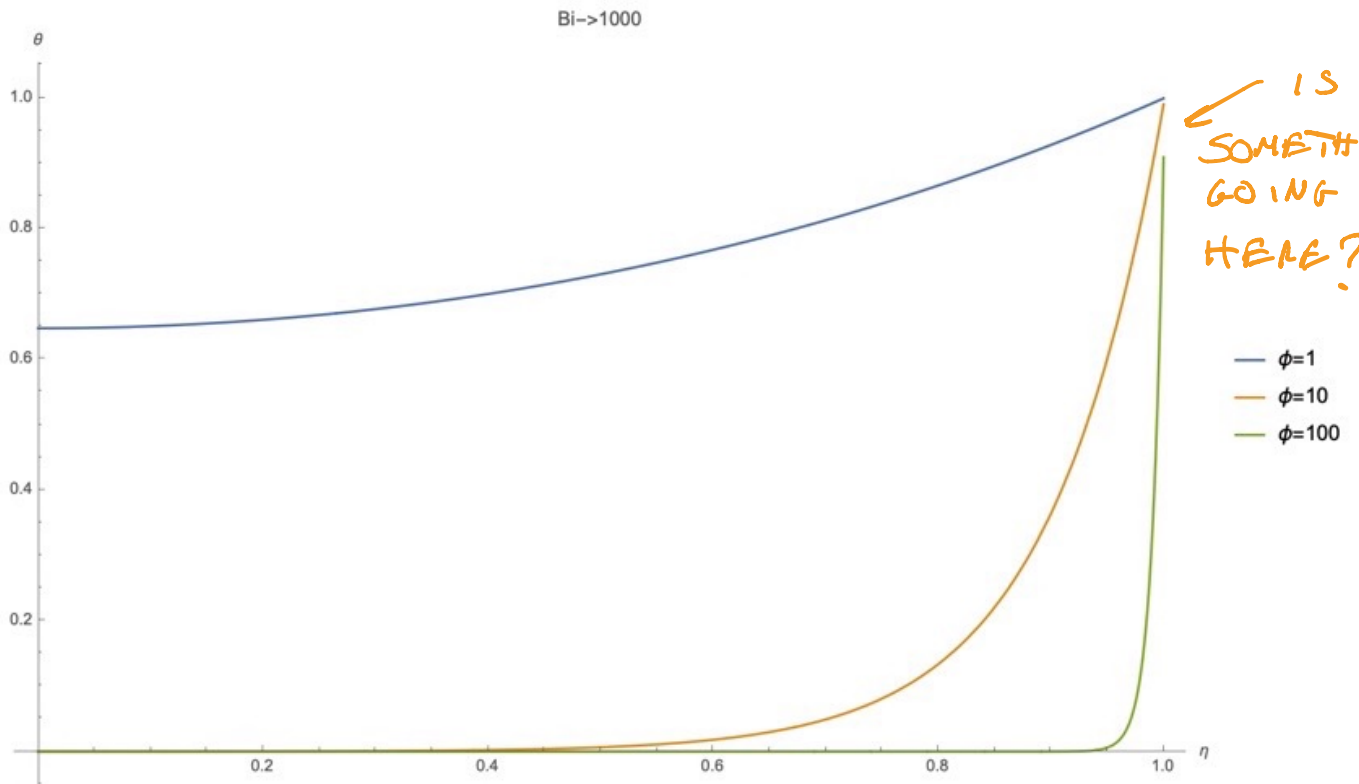
FOR A CYLINDER OR SPHERE, THIS IS A SYMMETRY CONDITION ACROSS  $r=0$

$$\theta(\eta) = \frac{Bi \cosh(\eta\phi)}{Bi \cosh(\phi) + \phi \sinh(\phi)}$$

FOR  $Bi = 1000$   $Bi \equiv \frac{L \bar{h}_c}{D_{TA}}$

EXTERNAL MASS TRANSFER  
IS NOT LIMITING UNTIL VERY  
HIGH REACTION RATES

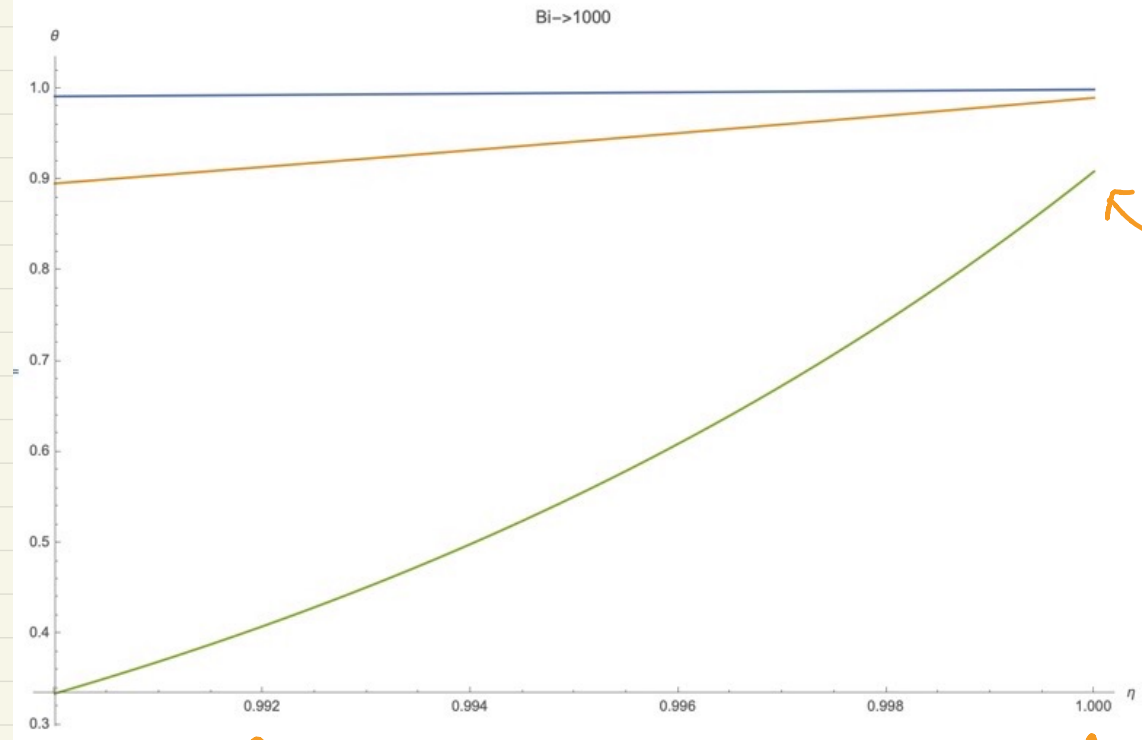
```
bianswerplot = Plot[{ans /. {phi -> 1, Bi -> 1000}, ans /. {phi -> 10, Bi -> 1000}, ans /. {phi -> 100, Bi -> 1000}}, {eta, theta, 1},  
AxesLabel -> {"eta", "theta"}, PlotRange -> All, PlotLegends -> {"phi=1", "phi=10", "phi=100"}, PlotLabel -> "Bi->1000"]
```



```

bianswerplot95 = Plot[{ans /. {phi -> 1, Bi -> 1000}, ans /. {phi -> 10, Bi -> 1000}, ans /. {phi -> 100, Bi -> 1000}}, {eta, .99, 1},
  AxesLabel -> {"eta", "theta"}, PlotRange -> All, PlotLegends -> {"phi=1", "phi=10", "phi=100"}, PlotLabel -> "Bi->1000"]

```



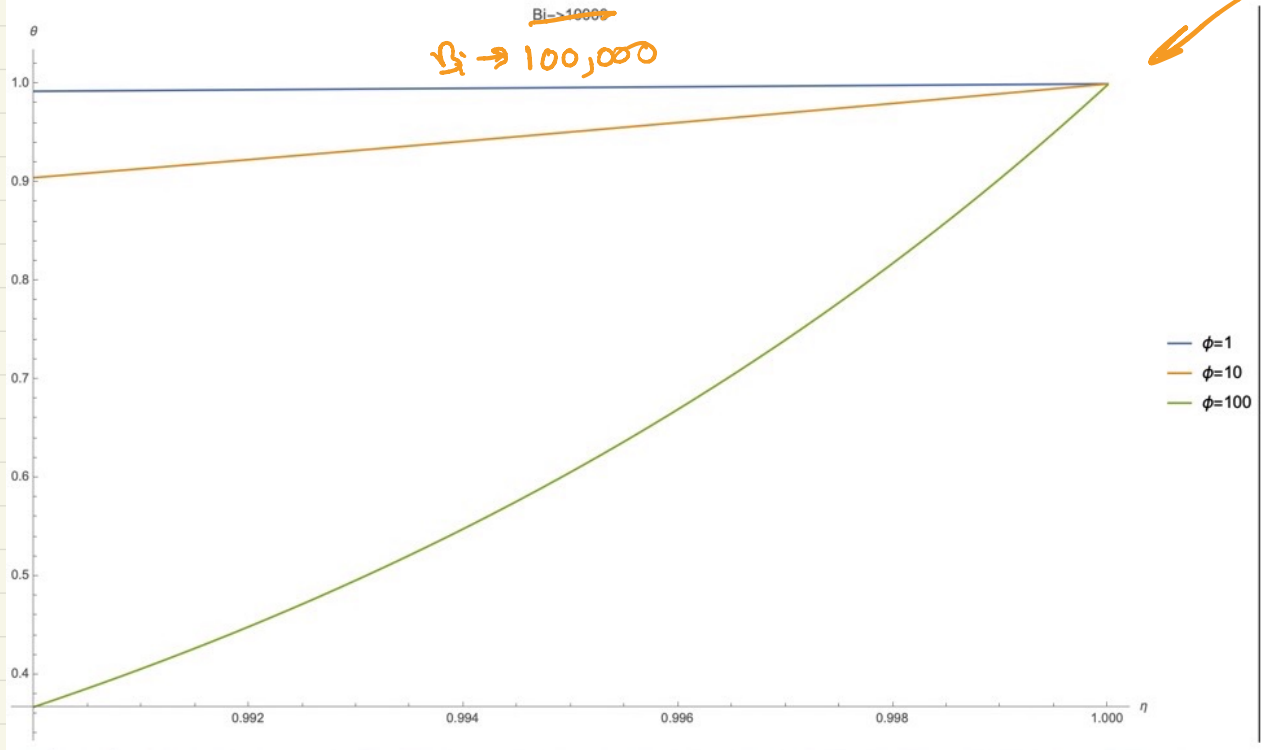
YES, IF  
REACTION IS  
FAST  
 $Ca_s < 1$



```

bianswerplot2 = Plot[{ans /. {phi -> 1, Bi -> 100000}, ans /. {phi -> 10, Bi -> 100000}, ans /. {phi -> 100, Bi -> 100000}}, {eta, .99, 1},
  AxesLabel -> {"eta", "theta"}, PlotRange -> All, PlotLegends -> {"phi=1", "phi=10", "phi=100"}, PlotLabel -> "Bi->100000"]

```



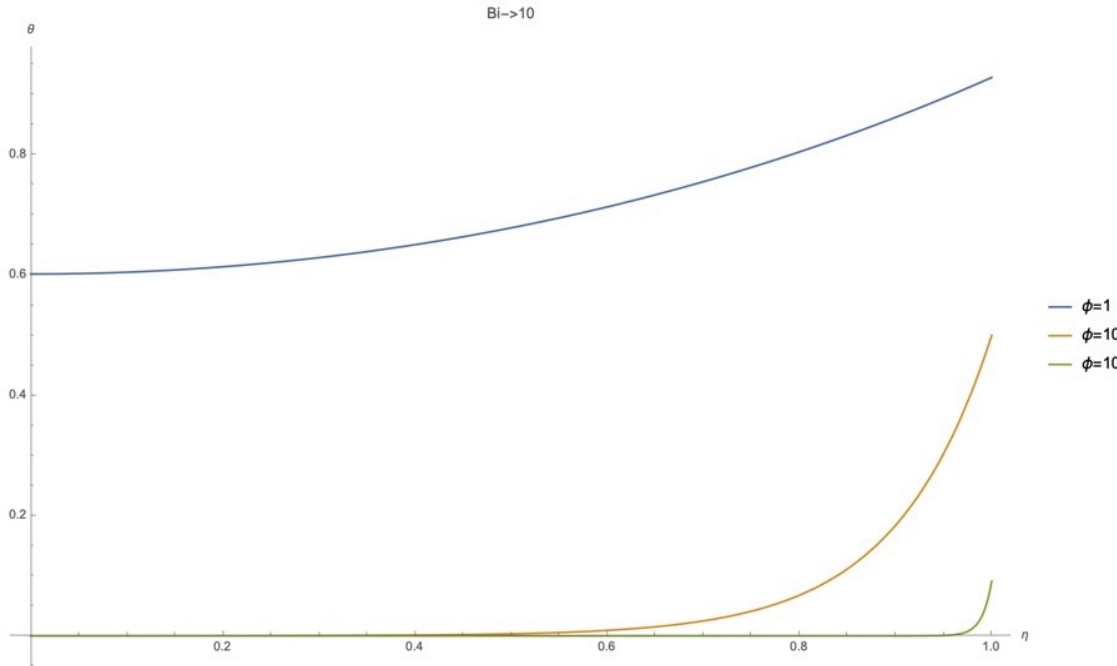
~~Bi -> 10000~~  
 $Bi \rightarrow 100,000$

AT  
 $Bi = 100,000$   
WE GET  
 $Ca_s = 1$



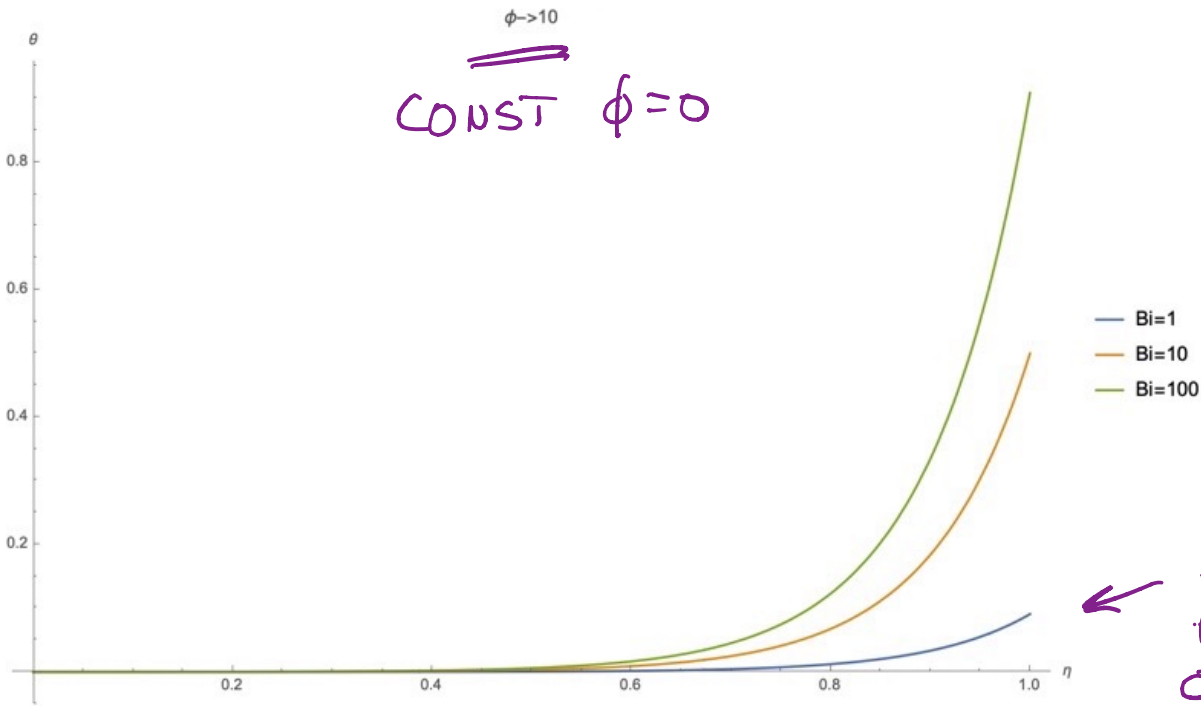
# A MORE MODERATE Bi

```
bianswerplot10 = Plot[{ans /. {phi -> 1, Bi -> 10}, ans /. {phi -> 10, Bi -> 10}, ans /. {phi -> 100, Bi -> 10}}, {eta, 0, 1}, AxesLabel -> {"eta", "theta"}, PlotRange -> All, PlotLegends -> {"phi=1", "phi=10", "phi=100"}, PlotLabel -> "Bi->10"]
```



SUBSTANTIAL EFFECT OF EXTERNAL RESISTANCE

```
bianswerplot = Plot[{ans /. {phi -> 10, Bi -> 1}, ans /. {phi -> 10, Bi -> 10}, ans /. {phi -> 10, Bi -> 100}}, {eta, 0, 1}, AxesLabel -> {"eta", "theta"}, PlotRange -> All, PlotLegends -> {"Bi=1", "Bi=10", "Bi=100"}, PlotLabel -> "phi->10"]
```



$\phi \rightarrow 10$   
 $\Rightarrow$   
 CONST  $\phi = 0$

← VERY BIG EFFECT OF MASS

TRANSFER RESISTANCE

WHAT IS FLUX TO SURFACE

$$\left. \frac{\partial \theta}{\partial \eta} \right|_{\eta=1} = \frac{Bi \phi \sinh(\phi)}{Bi \cosh(\phi) + \phi \sinh(\phi)}$$

THIS IS A FAMILIAR FORM

IF  $\phi \gg 1$  FLUX  $\rightarrow Bi$

$$\theta(1) = 0 \quad (C_s = 0)$$

MASS TRANSFER IS CONTROLLING

IF  $Bi \rightarrow \infty$

$$\text{FLUX} = \phi \tanh \phi$$

OR

$$\eta = \frac{\text{FLUX}}{\phi^2} = \frac{\tanh \phi}{\phi}$$

SAME RESULT AS BEFORE

MORE GENERALLY

$$\eta = \frac{\frac{\partial \phi}{\partial \eta} \Big|_{\eta=1}}{\phi^2} = \frac{Bi}{\phi^2 + Bi \coth \phi}$$
$$= \frac{\tanh \phi}{\phi \left( 1 + \frac{\phi \tanh \phi}{Bi} \right)}$$

WHAT DOES THIS SAY ABOUT REACTION RATE

$$D_{TA}^e \frac{\partial C_A}{\partial x} \Rightarrow \text{RATE OF } C_A \text{ GOING INTO CATALYST}$$

$$\frac{\partial \phi}{\partial \eta} \Big|_{\eta=1} = \frac{Bi \phi \sinh(\phi)}{Bi \cosh(\phi) + \phi \sinh(\phi)}$$

MAKE DIMENSIONAL:

$$D_{TA}^2 \frac{dC_A}{dx} = \frac{C^\infty}{L} D_{TA} \frac{\partial \theta}{\partial M} =$$

$$= \frac{\bar{h}_c C^\infty}{1 + \frac{\bar{h}_c}{hL} \coth \left[ \frac{hL^2}{D_{TA}} \right]}$$

$$Lh \gg h_c$$

$$\text{FLUX} = \bar{h}_c C^\infty$$

JUST EXTERNAL  
MASS TRANSFER

$$h_c \gg Lh$$

$$\text{FLUX} = h C^\infty L \tanh \left[ \frac{hL^2}{D_{TA}} \right]$$

YOU CAN PHYSICALLY REDUCE

EXTERNAL MASS TRANSFER

RESISTANCE BY "STIRRING FASTER"

$$Sh = 2 + 0.6 Re^{1/2} Sc^{1/3}$$

USUALLY MASS TRANSFER HAS  
LIMITED RANGE ~ FACTOR ~ 5-10

SO OTHERWISE TO REDUCE  
EFFECT OF  $\bar{T}_c$ ,

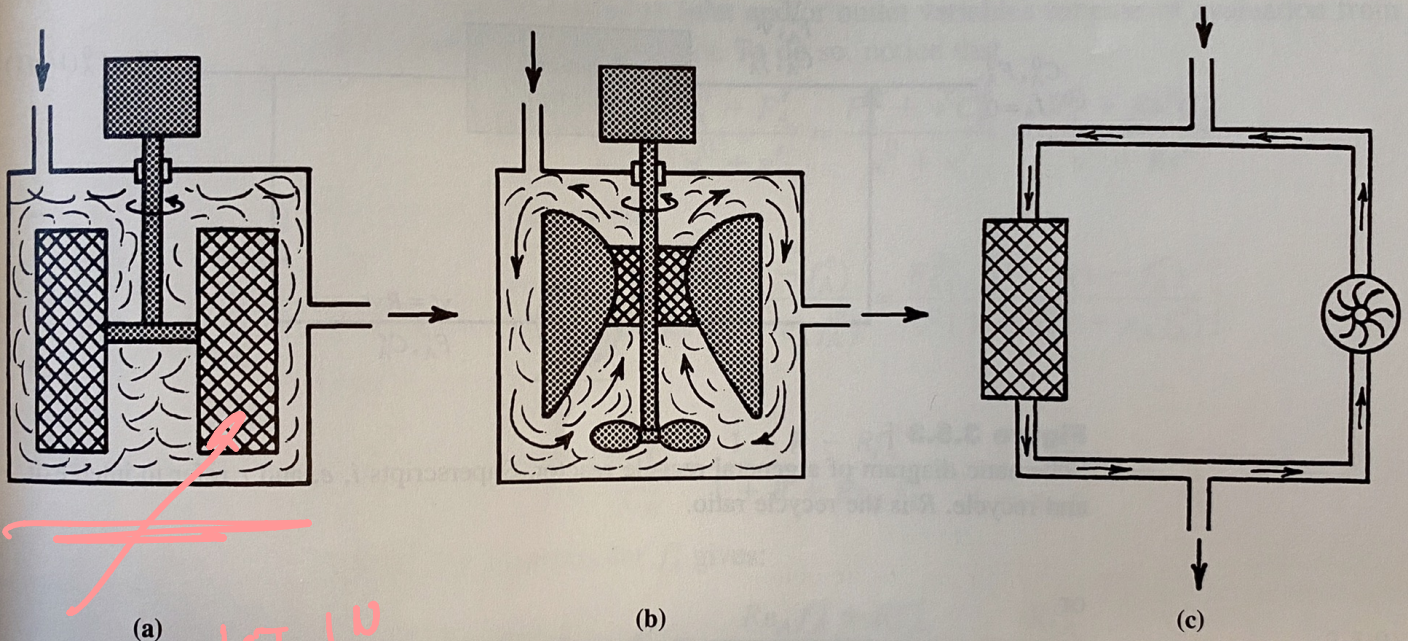
SMALLER  $L$ , ( $R_p$ )

SMALLER  $k$ , LOWER CATALYST  
LOADING,  
LOWER TEMP

ANALYSIS OF RATE DATA  
FOR SITUATIONS WHERE  
MASS TRANSFER RESISTANCE  
COULD BE IMPORTANT

— STIRRING SPEED —

— PARTICLE SIZE —

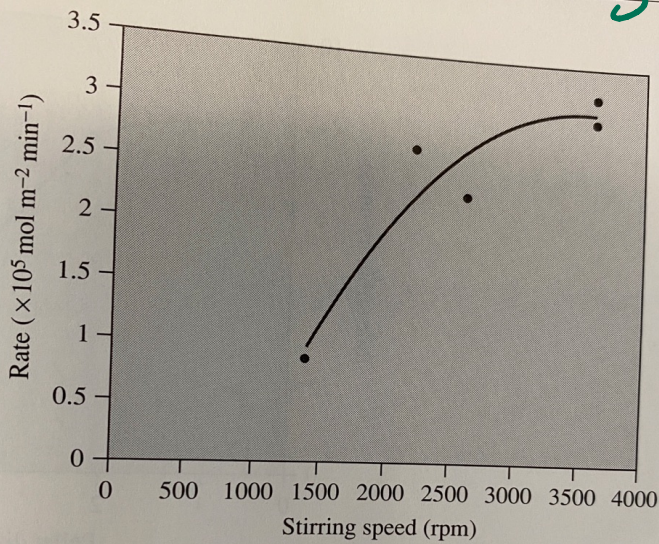


CATALYST IN  
 "BASKET"  
 THAT IS  
 STIRRED

**Figure 3.5.2 |** Stirred contained solids reactors. [Reproduced from V. W. Weekman, Jr., *AIChE J.*, **20** (1974) p. 835, with permission of the American Institute of Chemical Engineers. Copyright © 1974 AIChE. All rights reserved.] (a) Carberry reactor, (b) Berty reactor (internal recycle reactor), (c) external recycle reactor.

FOR GOOD MASS TRANSFER

$$Sh = 2 + 0.6 Re^{1/2} Sc^{1/3}$$

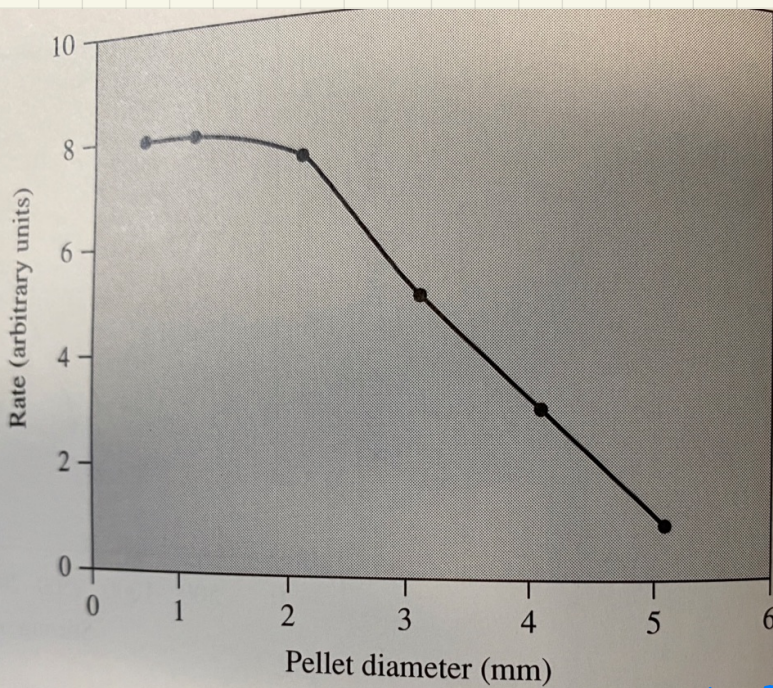


FACTOR OF 3

**Figure 6.5.1 |**

Effect of agitation on the rate of 2-propanol dehydrogenation to acetone at 355 K over Ni catalysts. [Rates are calculated at constant conversion level from the data in D. E. Mears and M. Boudart, *AIChE J.*, **12** (1966) 313.] In this case, increasing the stirring speed increased the rate of acetone diffusion away from the catalyst pellet and decreased product inhibition.

... are encountered in a catalytic reac



**Figure 6.5.2 |**

Schematic illustration of the influence of catalyst pellet size on the observed reaction rate.

CAUSE REDUCE BOTH EXTERNAL + INTERNAL RESISTANCE



# RULES OF THUMB

(IN TERMS OF OBSERVED RATE)

INTERNAL  
MASS TRANSFER,  
NOT LIMITING:

$$\frac{\Lambda_{\text{OBS}} R_p^2}{D_{\text{TA}}^e C_{\text{AS}}} < 1$$

n ORDER:

$$\frac{\Lambda_{\text{OBS}} R_p^2}{D_{\text{TA}}^e C_{\text{AS}}} < \frac{1}{n}$$

EXTERNAL  
RESISTANCE NOT  
LIMITING!

$$\frac{\Lambda_{\text{OBS}} R_p^2}{k_c C_{\text{AB}}} < \frac{.15}{n}$$

CAN ALSO CONSIDER  
HEAT TRANSFER LIMITATIONS

INTER PHASE

$$\frac{\Delta H_v R_{obs} R_p}{h_f T_B} < 0.15 \frac{R_g T_B}{E}$$

INTERNAL TO PARTICLE

$$\frac{\Delta H_v R_{obs} R_p}{\lambda^e T_S} < .75 \frac{R_g T_S}{E}$$