

CBE 30399

2/11/16

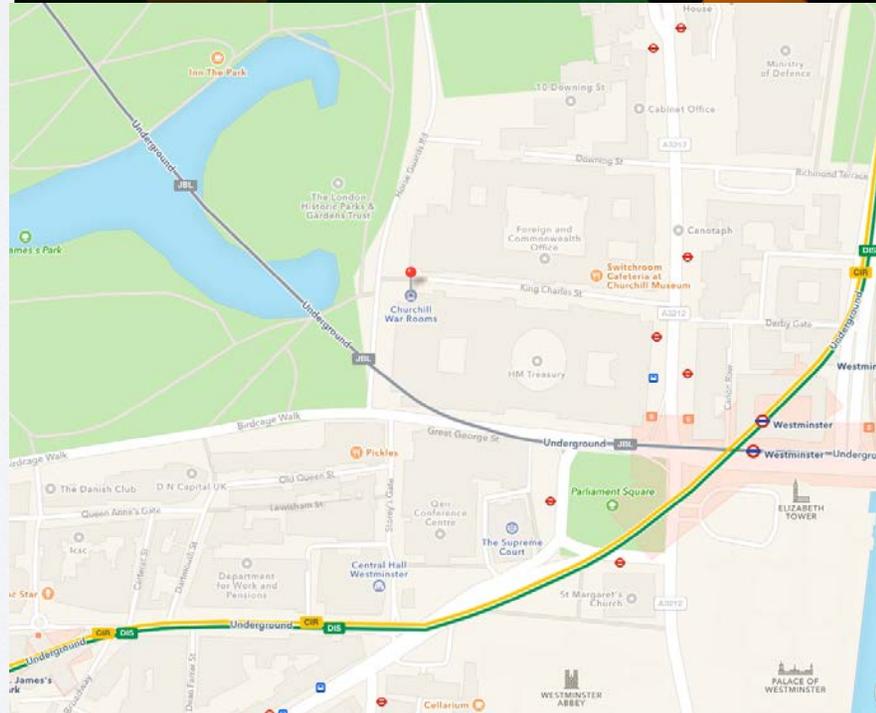
TOPICS

- Something about... London!
- Continuation of discussion of gas absorption

PROFESSOR MCCREADY'S DON'T MISS LIST!

- Cabinet War Rooms and Churchill Museum

CABINET WAR ROOMS



PROFESSOR MCCREADY'S DON'T MISS LIST!

- Cabinet War Rooms and Churchill Museum
- Tower Bridge tour

TOWER BRIDGE



PROFESSOR MCCREADY'S DON'T MISS LIST!

- Cabinet War Rooms and Churchill Museum
- Tower Bridge tour
- Westminster Abby (tour and go to Mass there)
- St Paul's Cathedral (tour, climb to the top!)

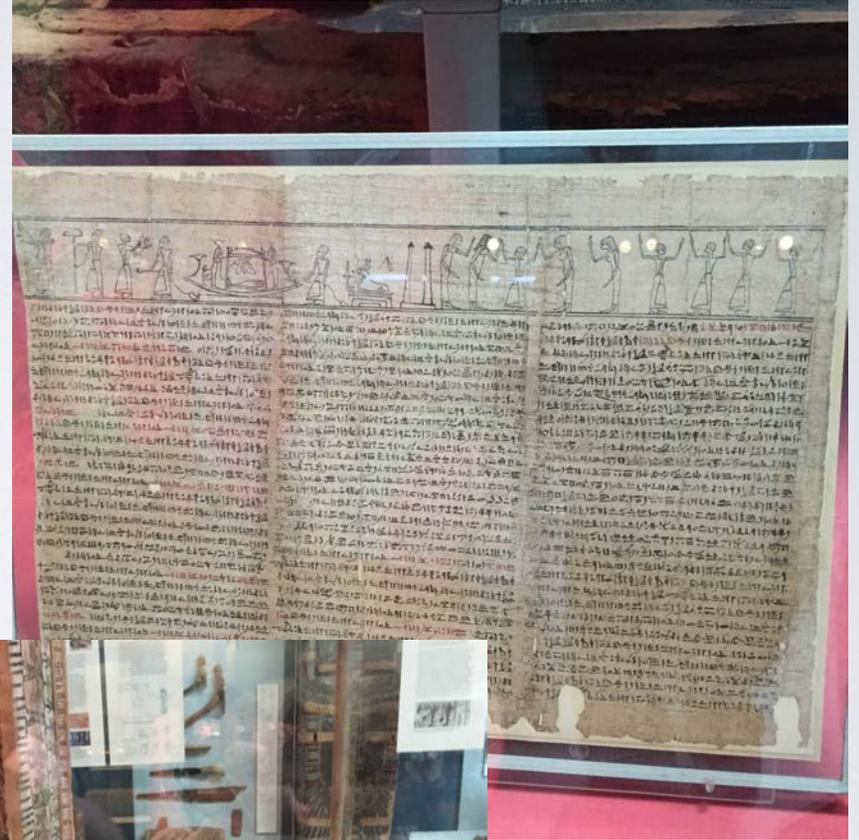
WESTMINSTER ABBY/ST.PAUL'S CATHEDRAL



PROFESSOR MCCREADY'S DON'T MISS LIST!

- Cabinet War Rooms and Churchill Museum
- Tower Bridge tour
- Westminster Abby (tour and go to Mass there)
- St Paul's Cathedral (tour, climb to the top!)
- British Museum

BRITISH MUSEUM



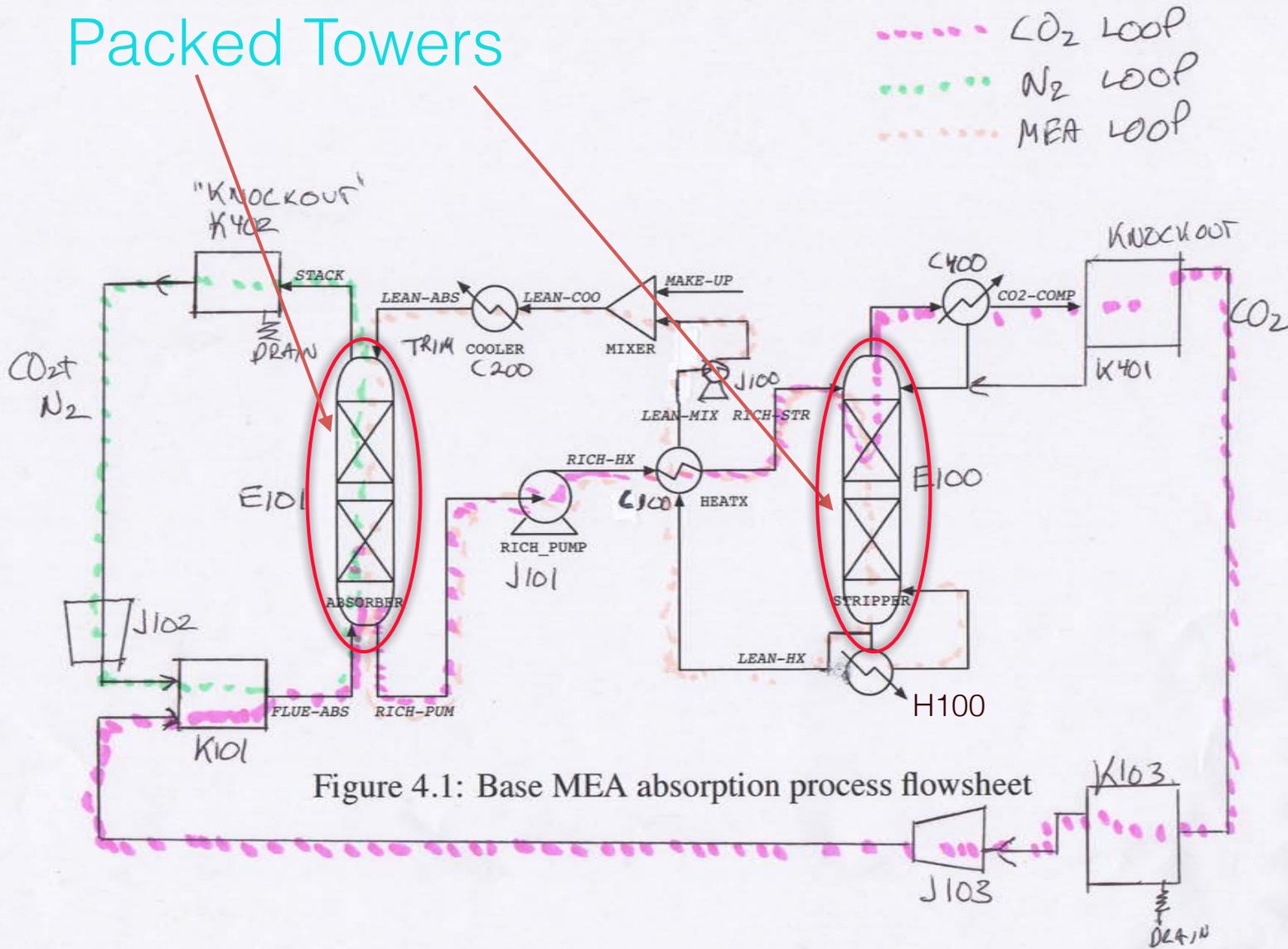
ASSUMING YOU SEE THESE OTHER PLACES ON OUR TOURS

- Windsor Castle
- Tower of London
- Thames Cruise
- Bus Tour

GAS ABSORPTION/STRIPING

Imperial Flowsheet

Packed Towers



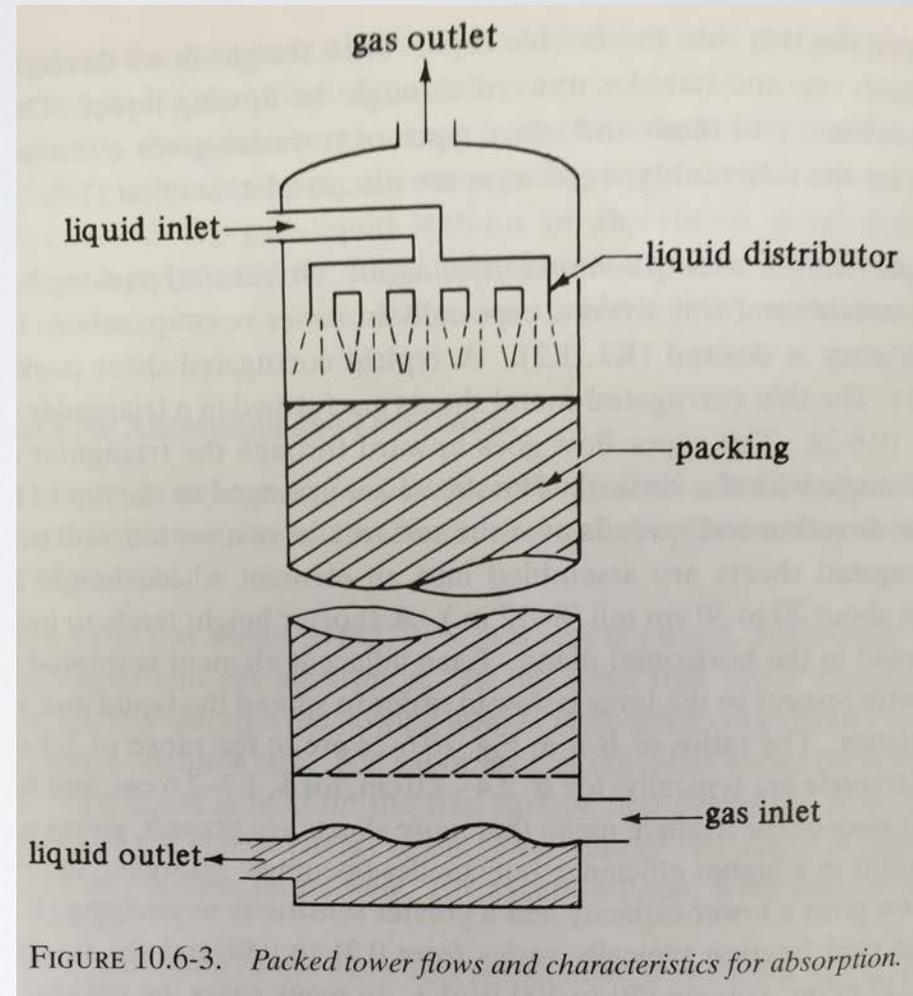
THE TWO COLUMNS



PACKED TOWER

- **Why Countercurrent**

- greater overall “driving force” (concentration difference)
- (potentially) no limitation on amount of CO₂ removed
 - could contact lowest concentration exiting gas with “pure” solvent



ABSORBER AND STRIPPER



Structured



Both give:

Random

- high surface area between liquid and gas
- continuous mixing of liquid and gas and they flow through column
- high fraction of “void” space so that the pressure drop is low

TWO BASIC PRINCIPLES

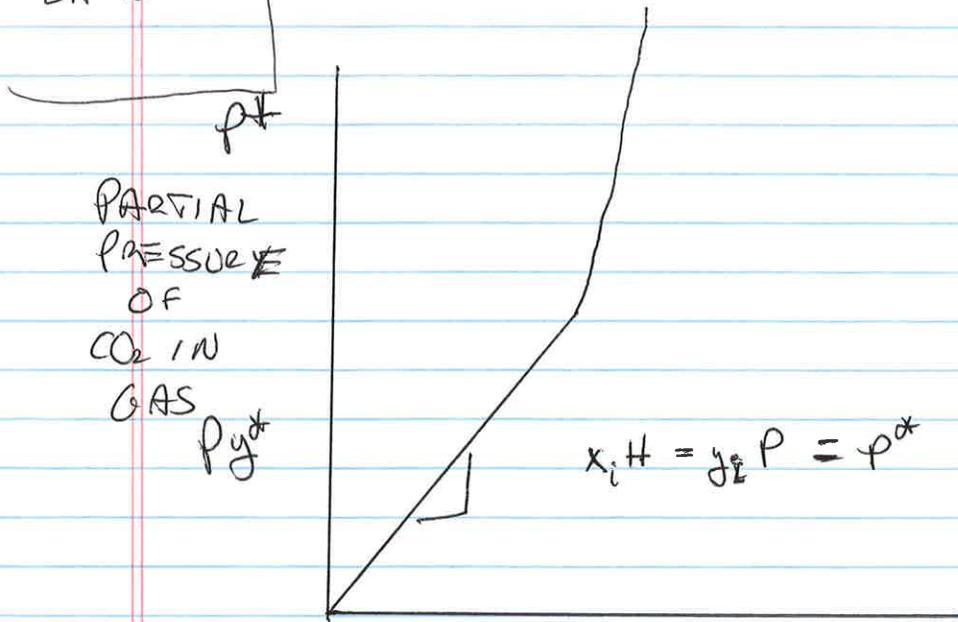
- Conservation of mass
 - Keep track of chemical species and deal with reaction
- Rate of transfer equation
 - analogous to Newton's Law of cooling

SIMPLEST
CONCEPTUAL
APPROACH

CHANGE IN TOTAL
PRESSURE

GAS-LIQUID EQUILIBRIUM
BEHAVIOR

2/14/16 ①



PARTIAL
PRESSURE
OF
CO₂ IN
GAS
 P_y

$$x_i H = y_i P = P^{\alpha}$$

X , MOLE FRACTION
OF CO₂
IN LIQUID

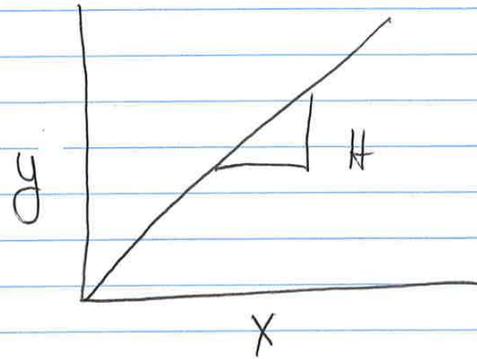
H = HENRY'S LAW
COEFFICIENT

y = MOLE FRACTION OF
CO₂ IN GAS.

SMALLER H \Rightarrow HIGHER SOLUBILITY

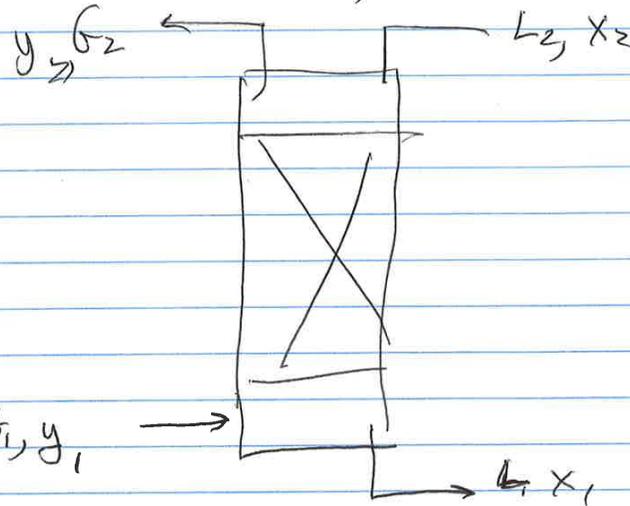
(2)

SO LET'S USE :



$$y = Hx$$

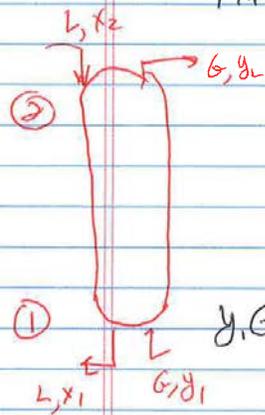
MASS BALANCE, JUST THINK OF
CO₂ IN AIR, LIQUID W/ CO₂ DROPT



• Chalk...

(3)

MASS BALANCE (MOLES)



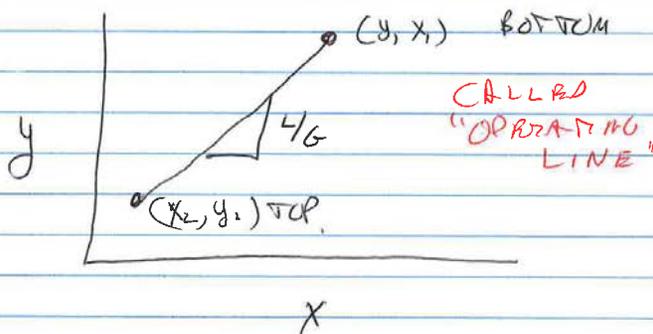
$$G_1 + L_2 = G_2 + L_1$$

COULD BE CONSTANT, $L_1 = L_2$
 $G_1 = G_2$

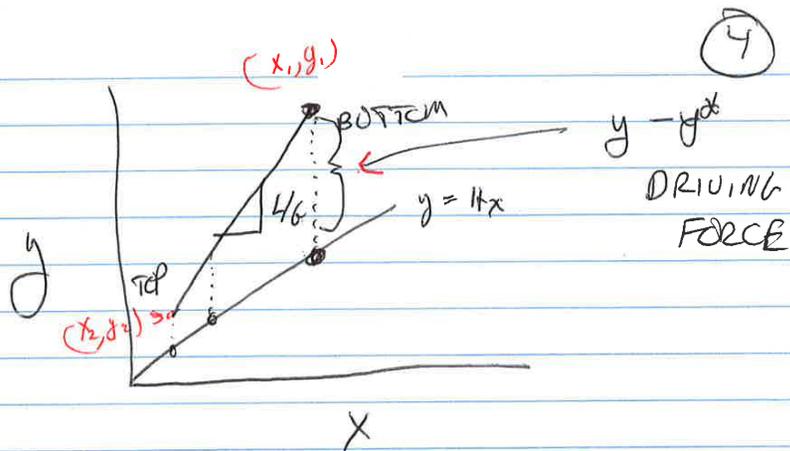
$$CO_{2,IN} = CO_{2,OUT} \quad \text{COMPONENT MASS BALANCE..}$$

$$y_1 G + L x_2 = y_2 G + L x_1$$

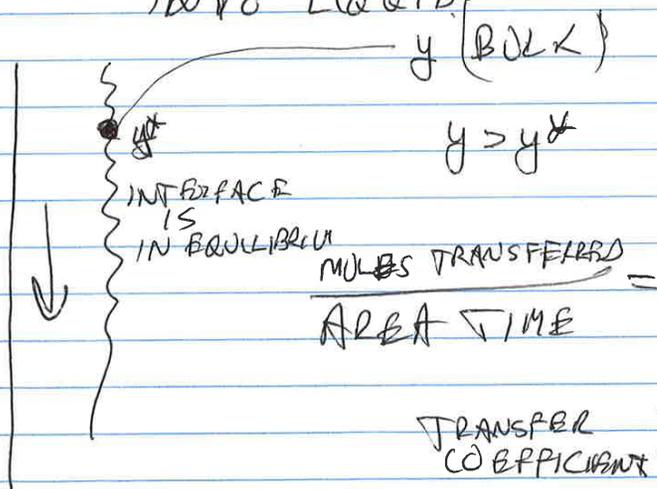
$$(y_1 - y_2) G = (x_1 - x_2) L$$



$$\frac{L}{G} = \frac{(y_1 - y_2)}{(x_1 - x_2)}$$

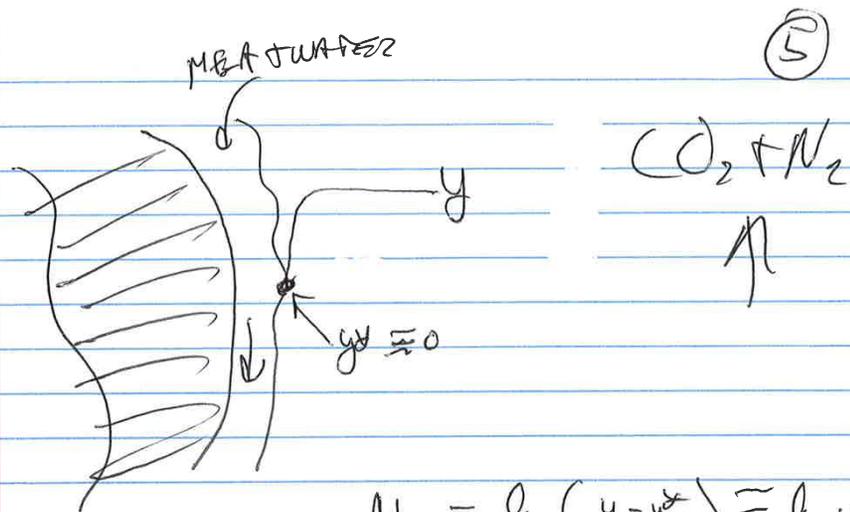


ALL ALONG COLUMN,
CONCENTRATION IN GAS OF
 CO_2 IS $>$ EQUILIBRIUM
VALUES, SO CO_2 GOES
INTO LIQID.



TRANSFER COEFFICIENT \times DRIVING FORCE

$$N_{\text{CO}_2} = k_{\text{CG}} (y - y^*)$$



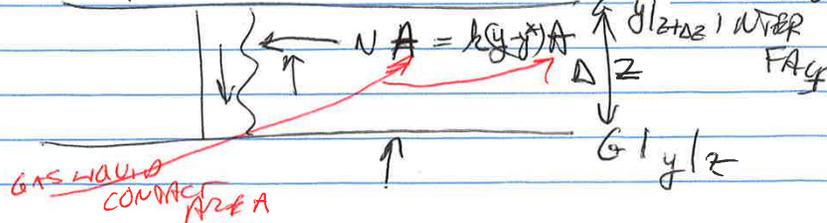
THINGS ARE CHANGING.
HOW DO WE DEAL WITH THIS?

TAKE "CONCEPTUALLY" A

"DIFFERENTIAL SLICE"

ACROSS COLUMN. (X-SECTION)

DO A MASS BALANCE
CHANGE OF MOLES IN GAS = MOLES
CROSSING



5A

F02 AIR (DIFFERENTIAL) CONTACT
VOLUME CO₂ BALANCE

$$\frac{\text{MOLES CO}_2 \text{ IN}}{\text{TIME}} - \frac{\text{MOLES CO}_2 \text{ OUT}}{\text{TIME}} = \text{RATE AT WHICH CO}_2 \text{ CROSSES FROM GAS} \rightarrow \text{LIQUID}$$

$$Gy|_z - Gy|_{z+\Delta z} = NA$$

(MOLE FLUX) (CONTACT AREA)

$$Gy|_z - Gy|_{z+\Delta z} = \int q(y-y^*) A V$$

↙ CROSS SECTION

$$\Delta V = A_{\text{cross}} \Delta z$$

$$q = \frac{\text{CONTACT AREA OF PACKING}}{\text{VOLUME OF PACKING}}$$

$$-G \frac{(y|_{z+\Delta z} - y|_z)}{\Delta z} = k a (y - y^*) A_{\text{TOWER}}$$

$$- \frac{dy}{dz} = \frac{k a}{G} (y - y^*) A$$

$$\int_0^z dz = - \frac{G/A}{k a} \int_{y_1}^{y_2} \frac{dy}{(y - y^*)}$$

$$z = \left(\frac{G/A}{k a} \right) \int_{y_1}^{y_2} \frac{dy}{(y - y^*)}$$

HEIGHT OF
PACKING

NEEDED

INVERSE
EFFICIENCY

OF
MESH
TRANSFER

N_{OG} N_{OG}

HOW
MUCH IS
SEPARATION
TO

ACCOMPLISH

⑦

IF $y^* = \text{CONST}$

$$-\int_{y_1}^{y_2} \frac{dy}{y - y^*} = \ln \left(\frac{y_1 - y^*}{y_2 - y^*} \right)$$

IF $y^* = 0$.

I.E. FOR MEA
ABSORPTION
W/ CO₂

$$-\int_{y_1}^{y_2} \frac{dy}{y} = \ln \left(\frac{y_1}{y_2} \right)$$

FOR THE 2 IMPERIAL EXPTS,

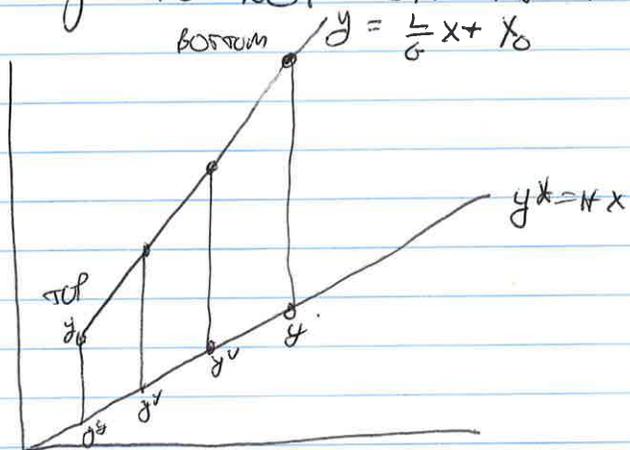
YOU CAN MEASURE y AT
BEGINNING MIDDLE END
SOME MORE IN BETWEEN.

YOU KNOW "z"
CONCENTRATIONS W/VE NOG
DETERMINE

→ HOG.

(74)

IF y^* IS NOT CONSTANT



$$y - y^* = y(x) - \underbrace{Hx}_{\text{SAME } X}$$

IF WE HAVE A y , WHICH X DO WE NEED?

$$y = \frac{L}{G}x + \left(y_2 - \frac{L}{G}x_2\right)$$

SOLVE FOR X

$$X = \frac{G}{L}(y - y_2) + x_2$$

SO THE INTEGRAL IS:

7B

$$= - \int_{y_1}^{y_2} \frac{dy}{y - Hx} =$$

$$= - \int_{y_1}^{y_2} \frac{dy}{y - H \left(\frac{G}{L} (y - y_2) + y_2 \right)}$$

$$A \equiv \frac{L}{HG}$$

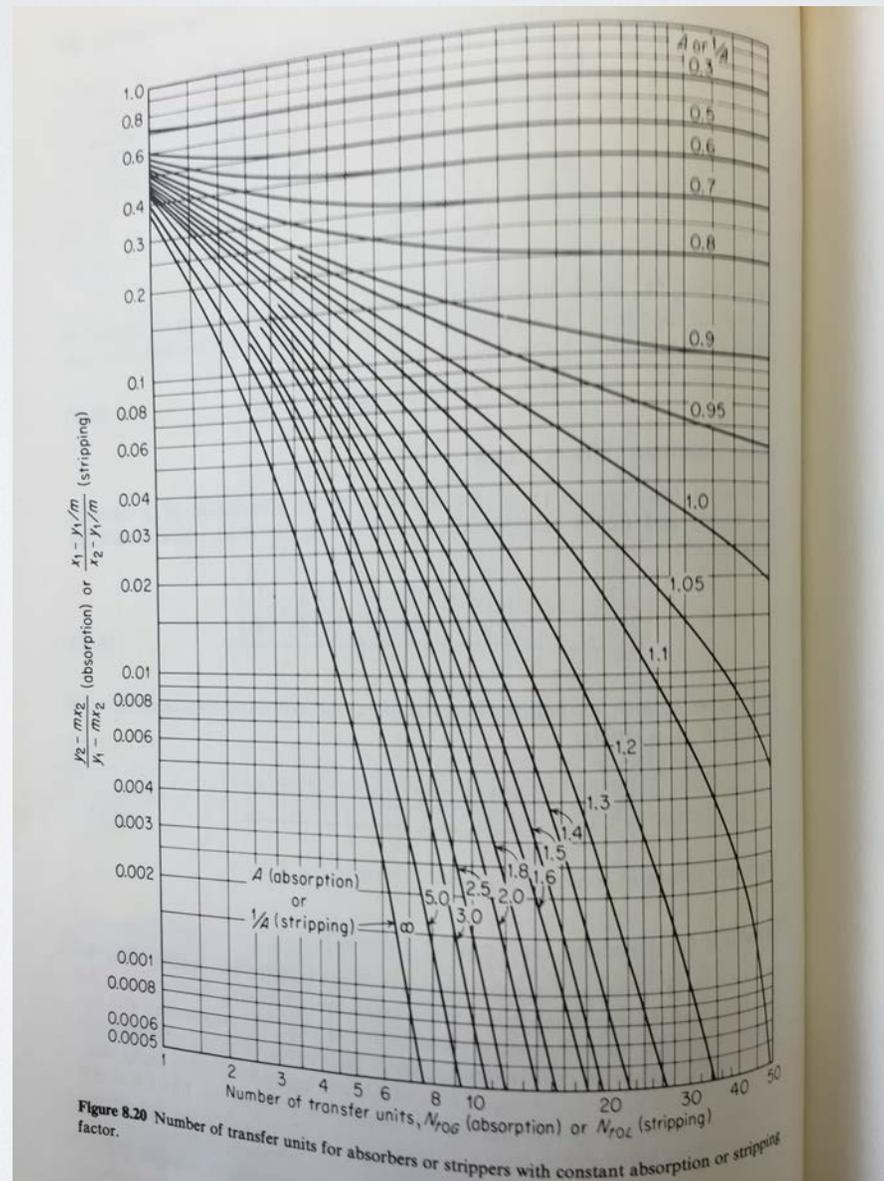
EASIER TO
ABSORB IF
A IS MADE
LARGER

$$= - \int_{y_1}^{y_2} \frac{dy}{\left(1 - \frac{1}{A}\right)y + \frac{y_2}{A} - H y_2}$$

$$= - \frac{1}{A-1} \ln \left[\frac{A(Hx_2 - y) + (y_1 - y_2)}{A(Hx_2 - y_2)} \right]$$

$$= \frac{\ln \left[\frac{(y_1 - Hx_2) \left(1 - \frac{1}{A}\right) + \frac{1}{A}}{(y_2 - Hx_2) \left(1 - \frac{1}{A}\right) + \frac{1}{A}} \right]}{1 - \frac{1}{A}}$$

ABSORPTION FACTOR CHART



HENRY'S LAW FOR CO₂ IN WATER

$$\text{For CO}_2 \quad H = 1590 \exp\left[-2400\left(\frac{1}{T} - \frac{1}{298}\right)\right] \quad \chi$$

$$\text{@ } 298 \quad H = 1590$$

2

For Sid COLUMN.
DON'T INTEGRATE FORMULAE...

GO TO

$$-\frac{dy}{dz} = \frac{k_a}{G} (y - y^*) A$$

$$k_a = \frac{\left(\frac{G}{A}\right) \frac{1}{(y - y^*)} \left(-\frac{dy}{dz}\right)}{a_v}$$

a_v = PROPERTY OF "PACKING"
350 m²/m³

$\frac{dy}{dz} = \frac{\Delta y}{\Delta z}$ ← MEASURE AT TWO "STAGES"
DISTANCE BETWEEN MEASUREMENTS

$y^* = 0, y$

$\frac{G}{A}$ = GAS FLOW RATE
CROSS AREA OF TOWER.

NOW SWITCH TO NOTATION
FOR THE PILOT PLANT.

YOU WANT TO CALCULATE
"K_G"

$$K_G = \frac{G \frac{dy}{dz}}{P(y - y^*) a_v}$$

$$K_G [=] \frac{\text{KMOLKS}}{\text{m}^2 \text{ hr kPa}}$$

$$G = \frac{\text{KMOLKS}}{\text{hour} \cdot \text{m}^2} = \frac{\text{SLIP} \cdot G}{A_T}$$

$$P = \text{TOTAL PRESSURE} \sim 1 \text{ ATM} \\ \sim 101.3 \text{ kPa}$$

$$a_v = \frac{350 \text{ m}^2}{\text{m}^3}$$

(10)

$$\frac{\partial Y_A}{\partial z} = \frac{\Delta Y_A}{\Delta z}$$

↓
COULD BE

$$\Delta z = 1.37 \text{ m} \quad \text{BETWEEN MEASUREMENT POINTS}$$

$$Y \equiv \frac{y}{1-y}$$

$$\left. \begin{array}{l} y_{\text{BOTTOM}} \sim .05 \\ y_{\text{NEXT POINT}} \sim .03 \end{array} \right\} 1.37 \text{ m.} \quad \begin{array}{l} Y_p = .052 \\ Y_N = .031 \end{array}$$

$$K_G = \frac{\left(\frac{119 \text{ kmole}}{\text{hr m}^2} \right) \left(\frac{.052 - .031}{1.37 \text{ m}} \right)}{\frac{101.3 \text{ kPa} (.04 - 0)}{350 \text{ /m}}}$$

$$K_G = 1.0013 \frac{\text{kmole}}{\text{m}^2 \text{ hr kPa}}$$

(11)

FOR THE LABORATORY ABSORBER,

DIDN'T WORK LAST YEAR,
SO I AM GUESSING SOME...

$$Z = \frac{G/A_T}{K_{OG}} \int_{y_1}^{y_2} \frac{dy}{(y - y^*)}$$

$$K_{OG} = \frac{1}{1 - \frac{mV'}{L'}} \ln \left[\left(1 - \frac{mV'}{L'} \right) \left(\frac{y_B}{y_T} \right) + \frac{mV'}{L'} \right]$$

$$A_T = \frac{(80 \text{ mm})^2 \pi}{4}$$

Liquid Flow, $\sim 150 \text{ l/min}$
CO₂ Flow $\sim 5 \text{ l/min}$
Air Flow $\sim 20 \text{ l/min}$

(12)

$$Z = H_{OG} N_{OG}$$

DILUTE GAS

$$N_{OG} = \frac{1}{1-A} \ln \left[\left(1 - \frac{1}{A}\right) \frac{y_B}{y_1} + \frac{1}{A} \right]$$

$$H_{OG} = \frac{V}{K_{OG} a A}$$

$V =$ MOLAR GAS
FLOW RATE

$$H = .75 \text{ m}$$

$$V = \frac{30 \text{ L}}{\text{MIN}} \Rightarrow .014 \text{ mol/s}$$

$$L = 150 \text{ L/HR} \Rightarrow 2.3 \text{ mol/s}$$

$$H = 1580 \quad A = \frac{2.3}{(1580)(.0136)}$$

$$A = .11$$

(13)

$$A_{og} = \frac{H}{NOG} = \frac{1.75}{NOG}$$

$$A = 50 \text{ cm}^2$$

$$L_G = \frac{U/A}{H_{OG}}$$

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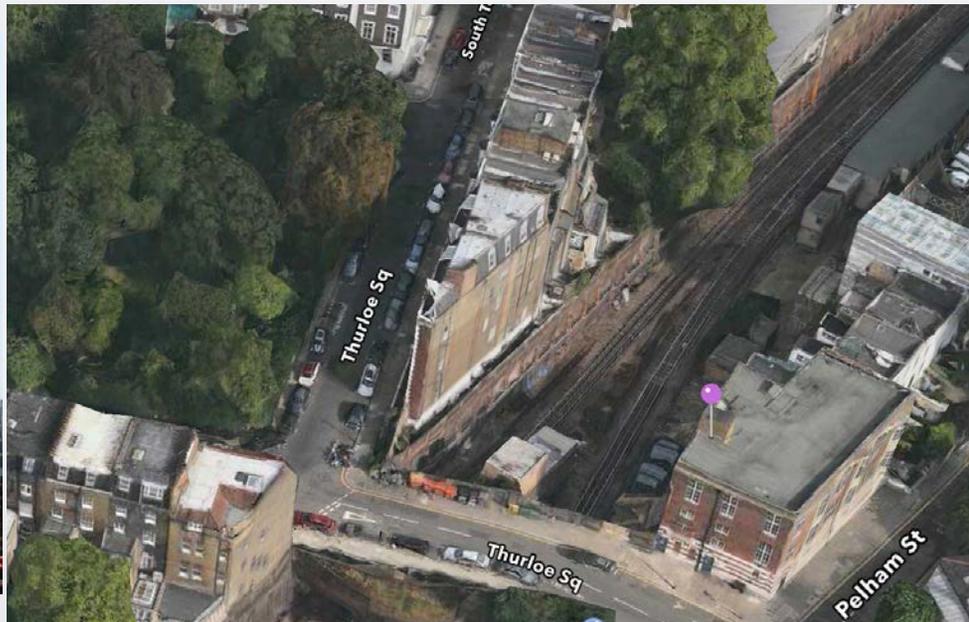
2/18/16

TOPICS

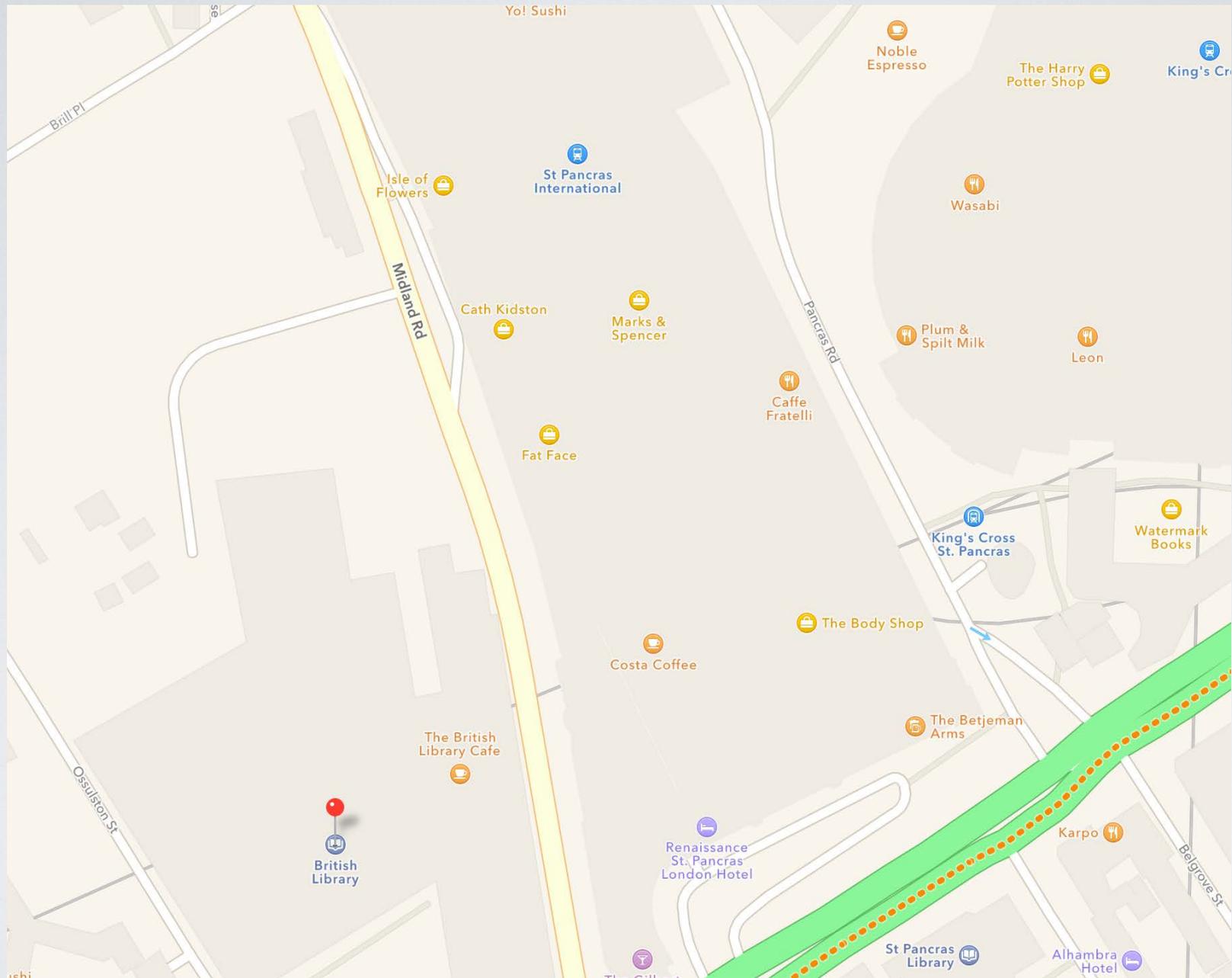
- Something about... London!
- Continuation of discussion of gas absorption

PROFESSOR MCCREADY'S TOP TO-DOS!

- If I am at Imperial and I have an hour:
 - Science Museum and/or Natural History Museum
 - Or go see the really skinny house on the District Line or the fake house-Fronts



- Look at Magna Carta at British Library
 - Origin of individual freedom?
- Right down the street from:
 - King's Cross/St. Pancras



KING'S CROSS/ST. PANCRAS



ST. PANCRAS



- Longest escalator in the London Underground
 - At “Angel” in the Northern Line
- Or do the entire London Subway Tour
- Off of the Northern line is the Royal Air Force Museum
 - Another subject you could be interested in.
- Walking tunnel under the Thames — it must be cool!
- I think you can see 4 “Prets” from a single location standing in Trafalgar Square!
- While I am there I want to go back to the National Gallery to see the da Vinci and the Michelangelo..
 - There was a work slowdown when I was there last year!

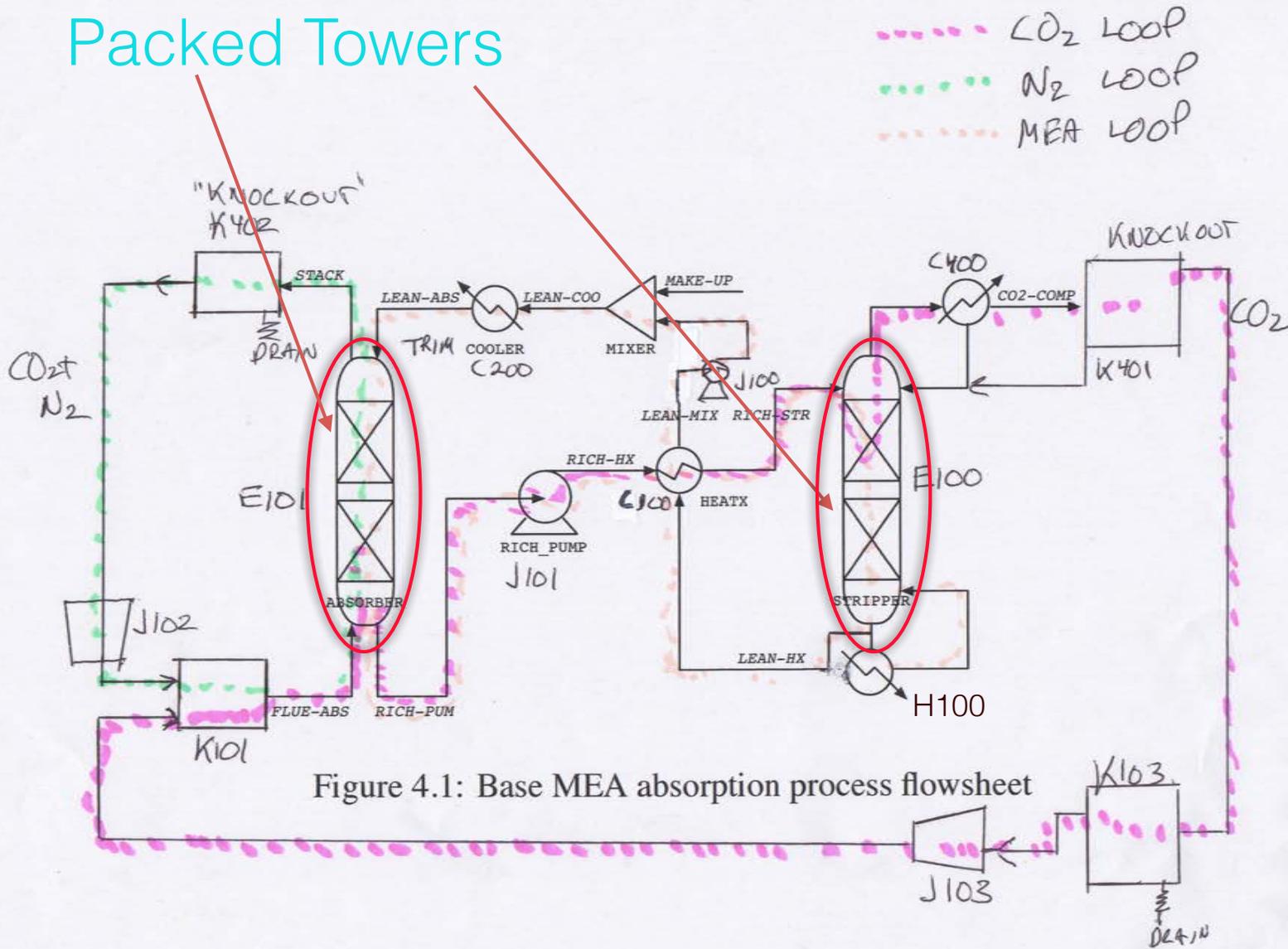
WEST END

- Phantom of the Opera

GAS ABSORPTION/STRIPING

Imperial Flowsheet

Packed Towers



ABSORBER AND STRIPPER



Structured



Both give: Random

- high surface area between liquid and gas
- continuous mixing of liquid and gas and they flow through column
- high fraction of “void” space so that the pressure drop is low

TWO BASIC PRINCIPLES

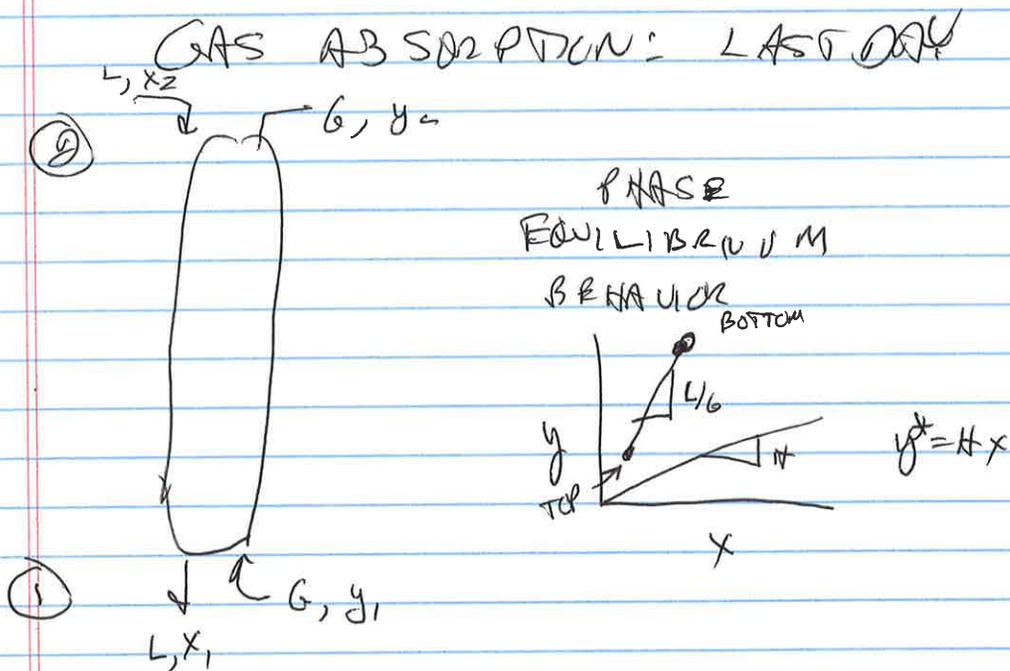
- Conservation of mass
 - Keep track of chemical species and deal with reaction
- Rate of transfer equation
 - analogous to Newton's Law of cooling

30399

2/18/16

①

GAS ABSORPTION: LAST DAY



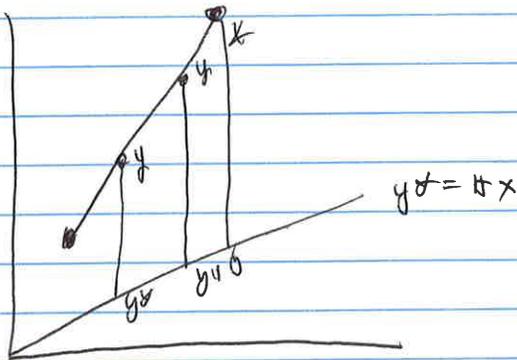
MASS BALANCE ON CO_2 GIVES
"OPERATING LINE"

$$y = \frac{L}{G} x + (y_2 - \frac{L}{G} x_2)$$

RATE AT WHICH CO_2 CROSSES
FROM GAS TO LIQUID

$$N_A = k (y - y^*)$$

(2)



$y - y^s$ IS NOT CONSTANT

SO WE TAKE A DIFFERENTIAL
SLICE OF COLUMN AND
INTEGRATE
 $\int G dz$

$\int G dz$

RATE OF
CHANGE
MOLES
LEAVING
GAS

=

RATE AT
WHICH
MOLES OF
GAS
CROSS PLATE
LIQUID

$$Gy|_z - Gy|_{z+\Delta z} = \rho_a (y - y^s) \Delta z$$

3

$$\Delta V \equiv A_{down} \Delta z$$

$$a = \frac{\text{GAS-LIQUID CONTACT AREA}}{\text{VOLUME OF PACKING}}$$

USED FOR PILOT PLANT ABSORBER TO GET "Z"

$$- \frac{dy}{dz} = \frac{G}{L} \frac{a}{G} (y - y^*) A_T$$

INTEGRATE

$$z = \frac{G/A_{down}}{ka} \int_{y_1}^{y_2} \frac{-dy}{y - y^*}$$

$$z = H_{OG} N_{OG}$$

NEED TO EVALUATE INTEGRAL.

4

IF $y^x = Hx$

$$N_{ij} = - \int_{y_1}^{y_2} \frac{dy}{y - Hx}$$

PRM
OR
LINK

$$X = \frac{G}{L} (y - y_2) + X_2$$

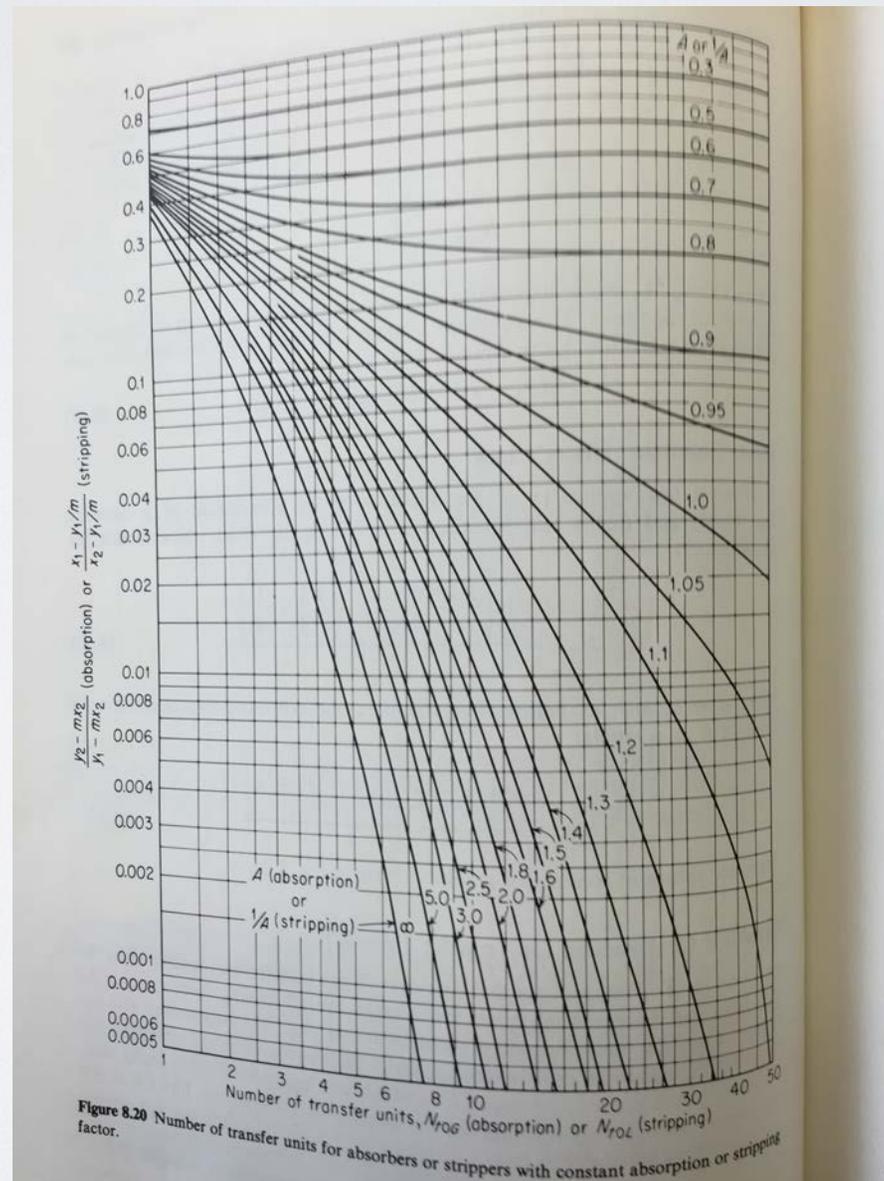
$$A \equiv \frac{L}{HG}$$

LARGE A,
EASIER TO
ASSUM B.

$$= \ln \left[\frac{y_1 - Hx_2}{y_2 - Hx_2} \left(1 - \frac{1}{A} \right)^{\frac{L}{A}} \right]$$

$$1 - 1/A$$

ABSORPTION FACTOR CHART



(5)

For β 16 COLUMN.
DON'T INTEGRATE FORMULA...

GO TO

$$-\frac{dy}{dz} = \frac{k_a}{G} (y - y^*) A$$

$$k_a = \frac{\left(\frac{G}{A}\right) \left(-\frac{dy}{dz}\right)}{(y - y^*)}$$

k_a = PROPERTY OF "PACKING"
 $350 \text{ m}^2/\text{m}^3$

$\frac{dy}{dz} = \frac{\Delta y}{\Delta z}$ ← MEASURE AT TWO "STAGES"
DISTANCE BETWEEN MEASUREMENTS

$y^* = 0, y$

$\frac{G}{A}$ = GAS FLOW RATE
CROSS AREA OF TOWER.

⑥

NOW SWITCH TO NOTATION
FOR THE PILOT PLANT.

YOU WANT TO CALCULATE
"K_G"

$$K_G = \frac{G \frac{dy}{dz}}{P(y - y^*) dz}$$

$$K_G [=] \frac{\text{KMOLHS}}{\text{m}^2 \text{ hr kPa}}$$

$$G = \frac{\text{KMOLHS}}{\text{Hour} \cdot \text{m}^2}$$

$$\frac{G}{A_T}$$

$$A_T = 0.0415 \text{ m}^2$$

$$P = \text{TOTAL PRESSURE} \sim 1 \text{ ATM} \\ \sim 101.3 \text{ kPa}$$

$$Q_v = \frac{350 \text{ m}^3}{\text{m}^3}$$

$$\frac{\partial Y_A}{\partial z} = \frac{\Delta Y_A}{\Delta z}$$

could be

$$\Delta z = 1.37 \text{ m} \quad \text{BETWEEN MEASUREMENT POINTS.}$$

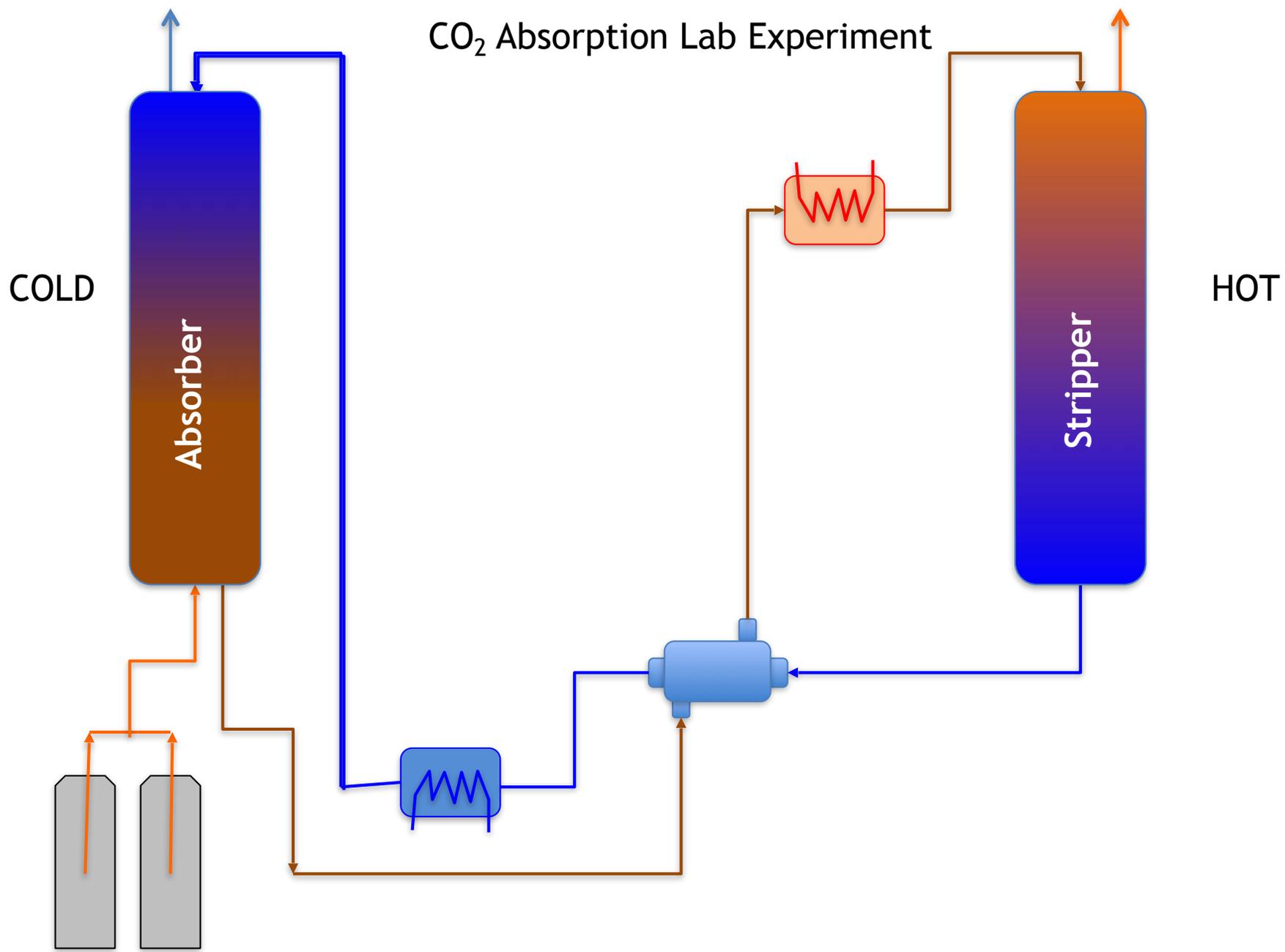
$$Y \equiv \frac{y}{1-y}$$

$$\left. \begin{array}{l} y_{\text{BOTTOM}} \sim .05 \\ y_{\text{NEXT POINT}} \sim .03 \end{array} \right\} 1.37 \text{ m.} \quad \begin{array}{l} Y_B = .052 \\ Y_N = .031 \end{array}$$

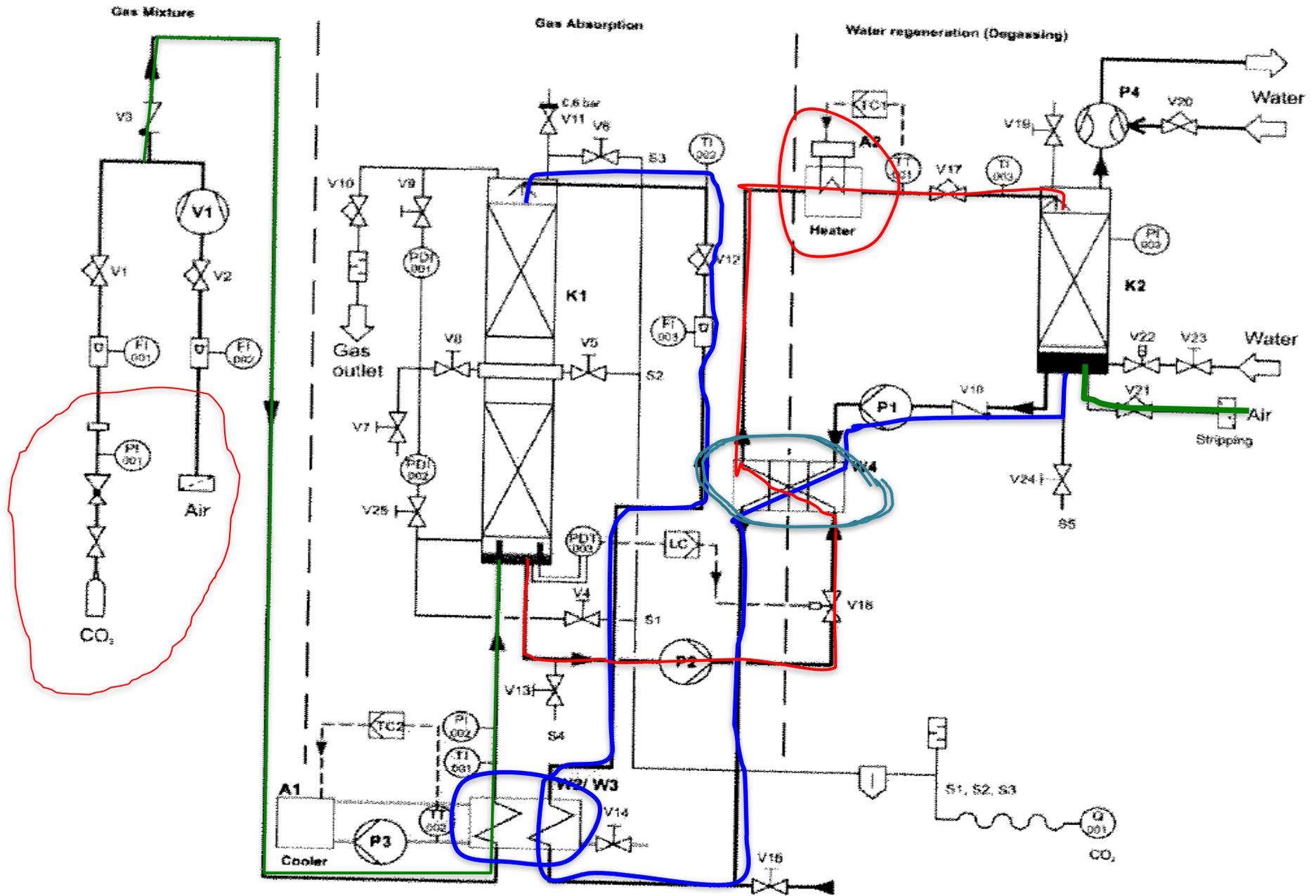
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$$K_G = 1.0013 \frac{\text{kmole}}{\text{m}^2 \text{ hr kPa}}$$

CO₂ Absorption Lab Experiment



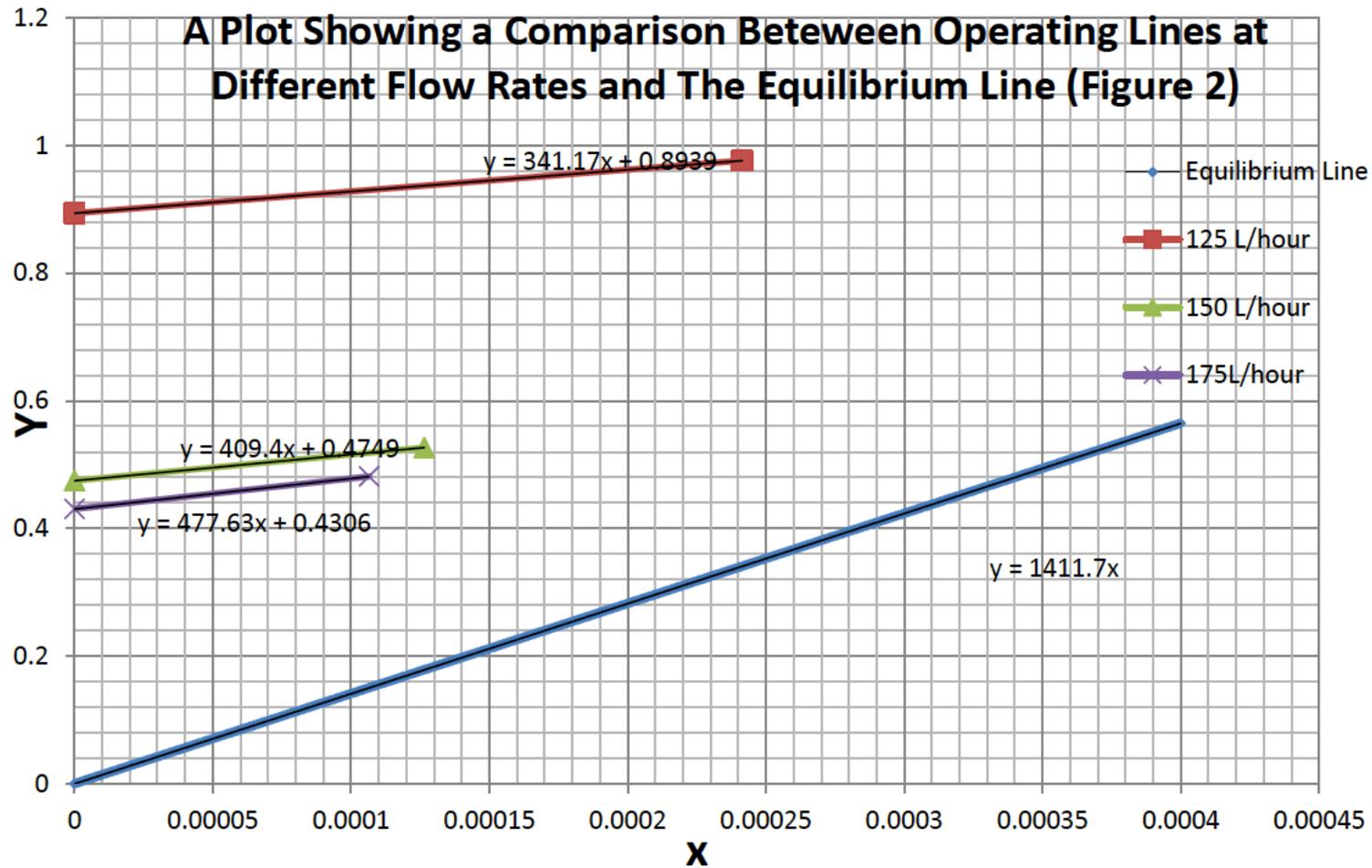




OXYBABY



Example From Student's Result



FOR THE LABORATORY ABSORBER,

DIDN'T WORK LAST YEAR,
SO I AM GUESSING SOME...

$$Z = \frac{G/A_T}{ka} \int_{y_1}^{y_2} \frac{dy}{(y - y^*)}$$

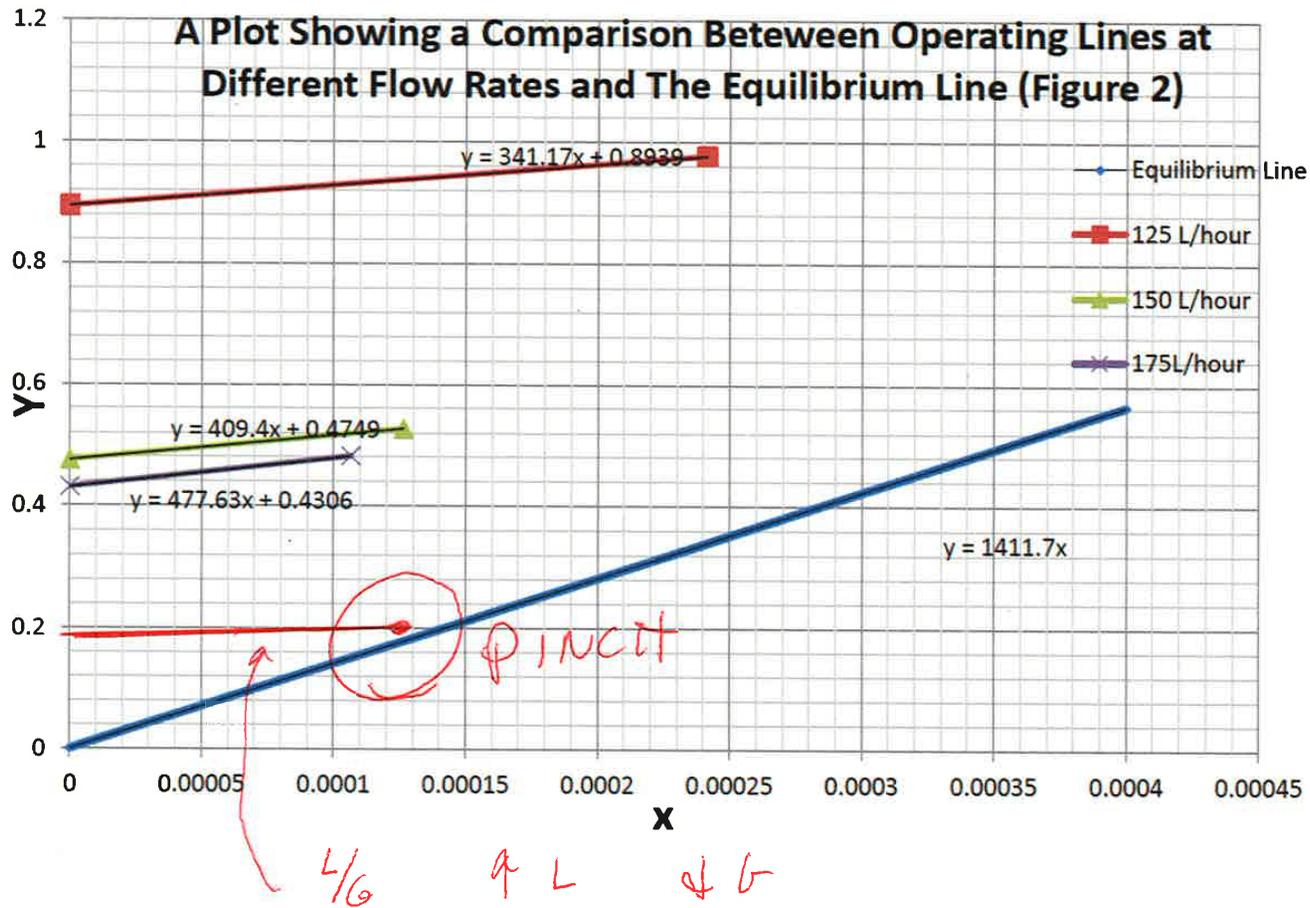
H_{OG} N_{OG}

$$N_{OG} = \frac{1}{1 - \frac{mV'}{L'}} \ln \left[\left(1 - \frac{mV'}{L'} \right) \left(\frac{y_B}{y_T} \right) + \frac{mV'}{L'} \right]$$

$$A_T = \frac{(80 \text{ mm})^2 \pi}{4}$$

LIQUID FLOW, $\sim 150 \text{ l/min}$
 CO_2 FLOW $\sim 5 \text{ l/min}$
 AIR FLOW $\sim 20 \text{ l/min}$

Example From Student's Result



$$Z = H_{OG} N_{OG}$$

DILUTE GAS

$$N_{OG} = \frac{1}{1 - \frac{1}{A}} \ln \left[\left(1 - \frac{1}{A}\right) \frac{y_B}{y_1} + \frac{1}{A} \right]$$

$$H_{OG} = \frac{V}{K_{OG} a A}$$

V = MOLAR GAS
FLOW RATE

$$H = .75 \text{ m}$$

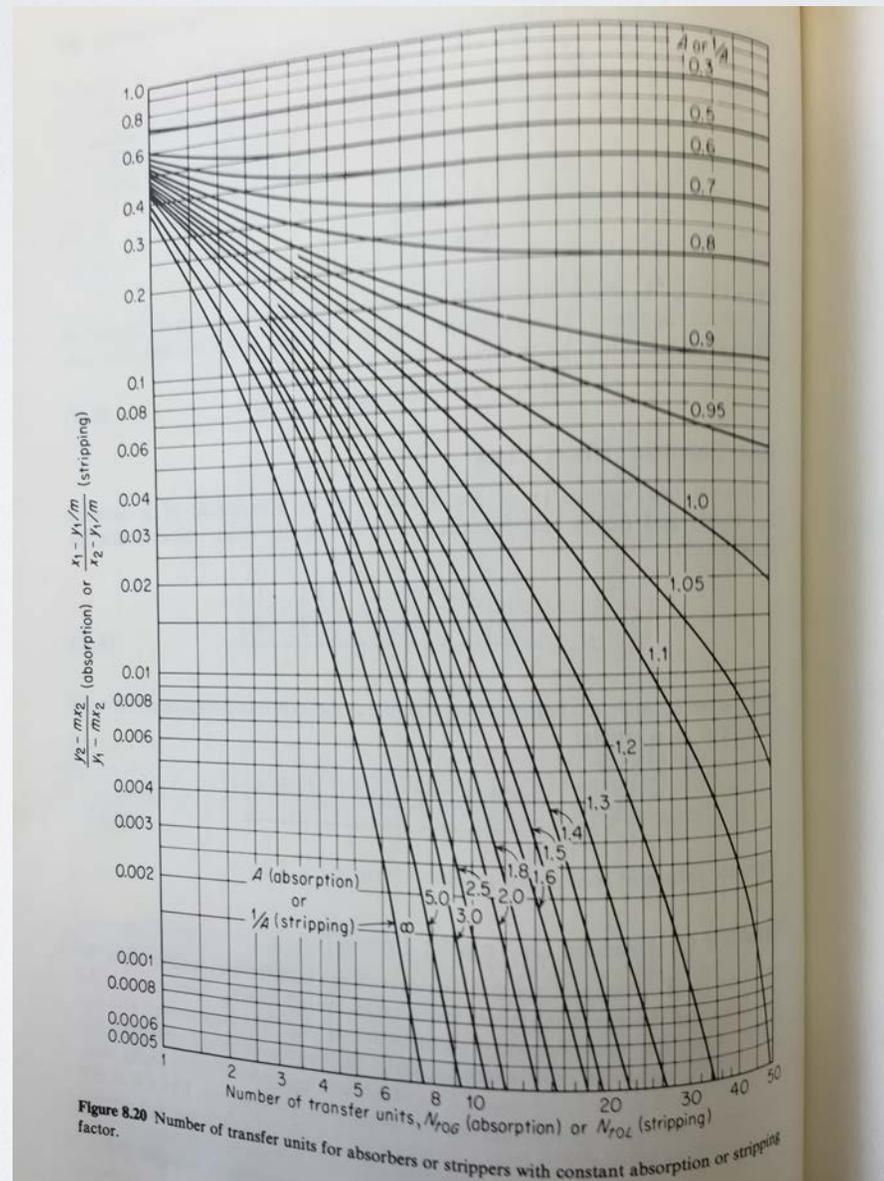
$$V = \frac{300 \text{ L}}{\text{MIN}} \Rightarrow .014 \text{ mol/s}$$

$$L = 150 \text{ L/hr} \Rightarrow 2.3 \text{ mol/s}$$

$$H = 1580 \quad A = \frac{2.3}{(1580)(.0136)}$$

$$A = .11$$

ABSORPTION FACTOR CHART



$$A_{CG} = \frac{H}{NOG} = \frac{1.75}{NOG}$$

$$A_J = 50 \text{ cm}^2$$

$$R_{CG} = \frac{U/A_J}{H_{NOG}}$$

10