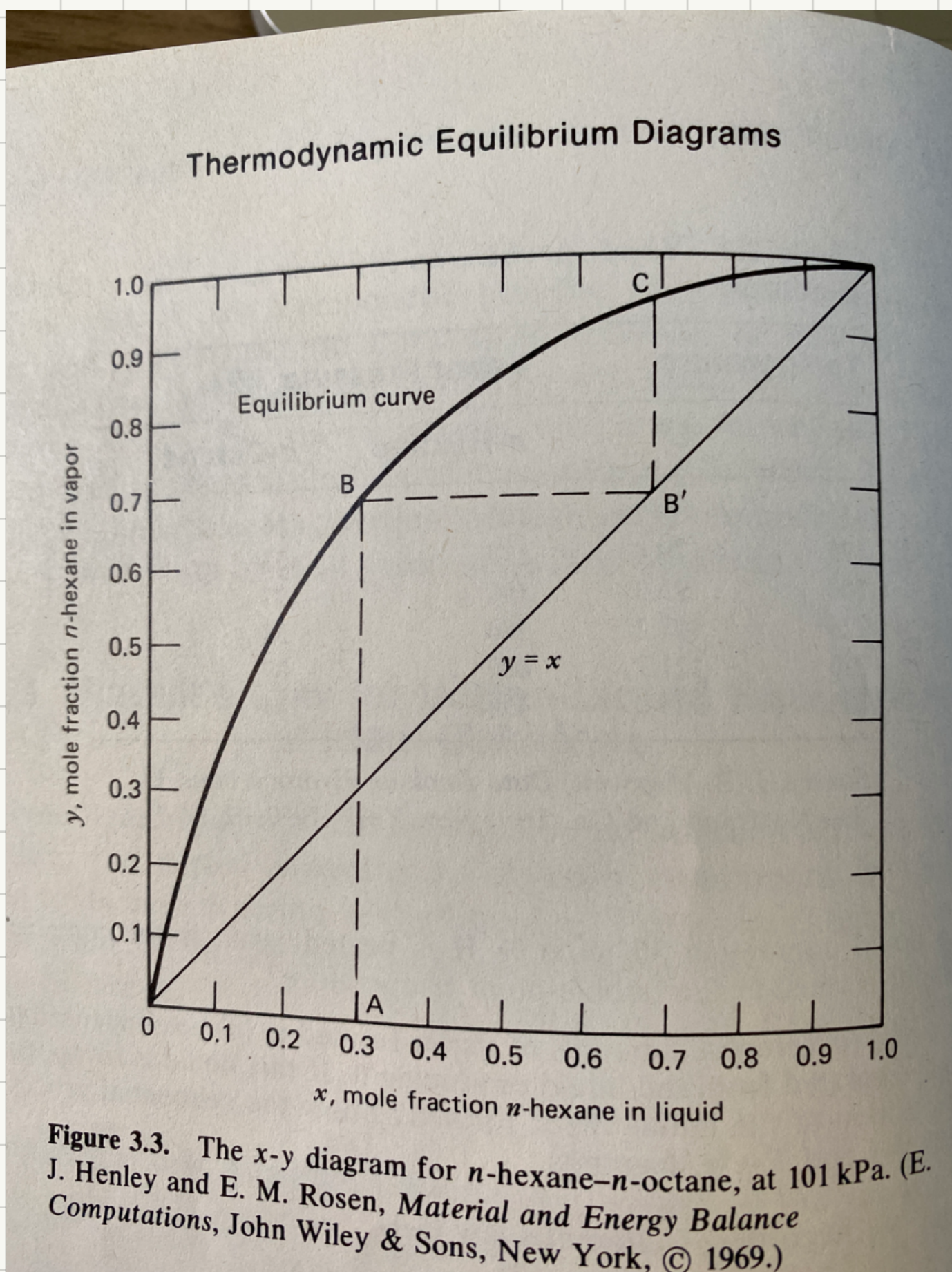


CBE 34487

6/25/20

## MULTI STAGE OPERATIONS

CONSIDER A LIQUID MIXTURE



SUPPOSE  $x = .3$

$y = .7$

IT IS DESIRED  
TO GET HEXANE  
AT  $\sim 0.99$   
PURITY?

WHAT CAN YOU  
DO.?

### Thermodynamic Equilibrium Diagrams

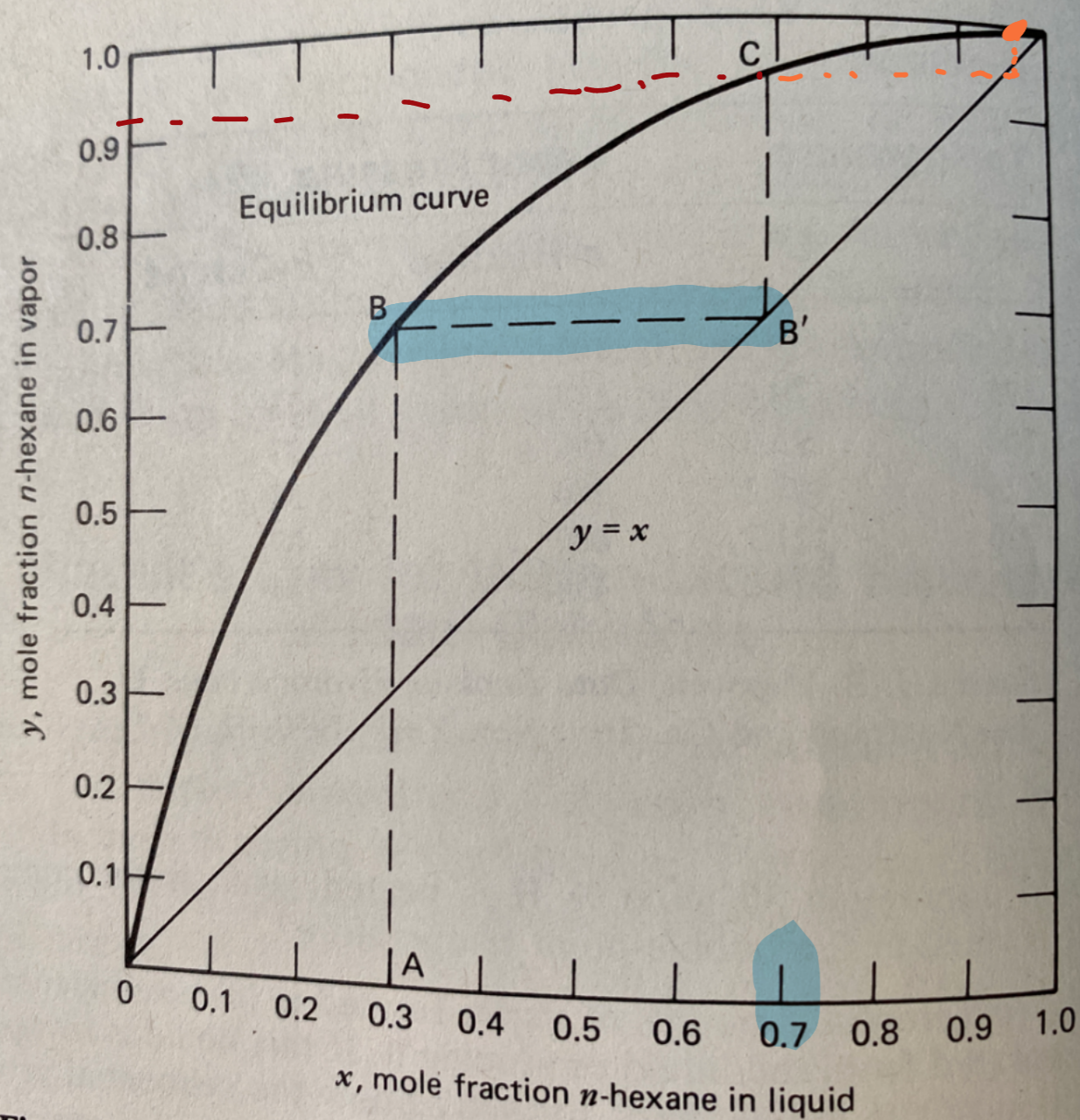


Figure 3.3. The x-y diagram for n-hexane-n-octane, at 101 kPa. (E. J. Henley and E. M. Rosen, *Material and Energy Balance Computations*, John Wiley & Sons, New York, © 1969.)

WE COULD COLLECT  
SOME OF THE  
VAPOR AND  
CONDENSE.  
OF COURSE, IF  
WE PICKED A  
SIGNIFICANT  
FRACTION,  
THE CONCENTRATION  
WOULD DROP.

NOW WE HAVE VAPOR AT  $y = .93$

NOW CONDENSE THIS AND  $x = .93$

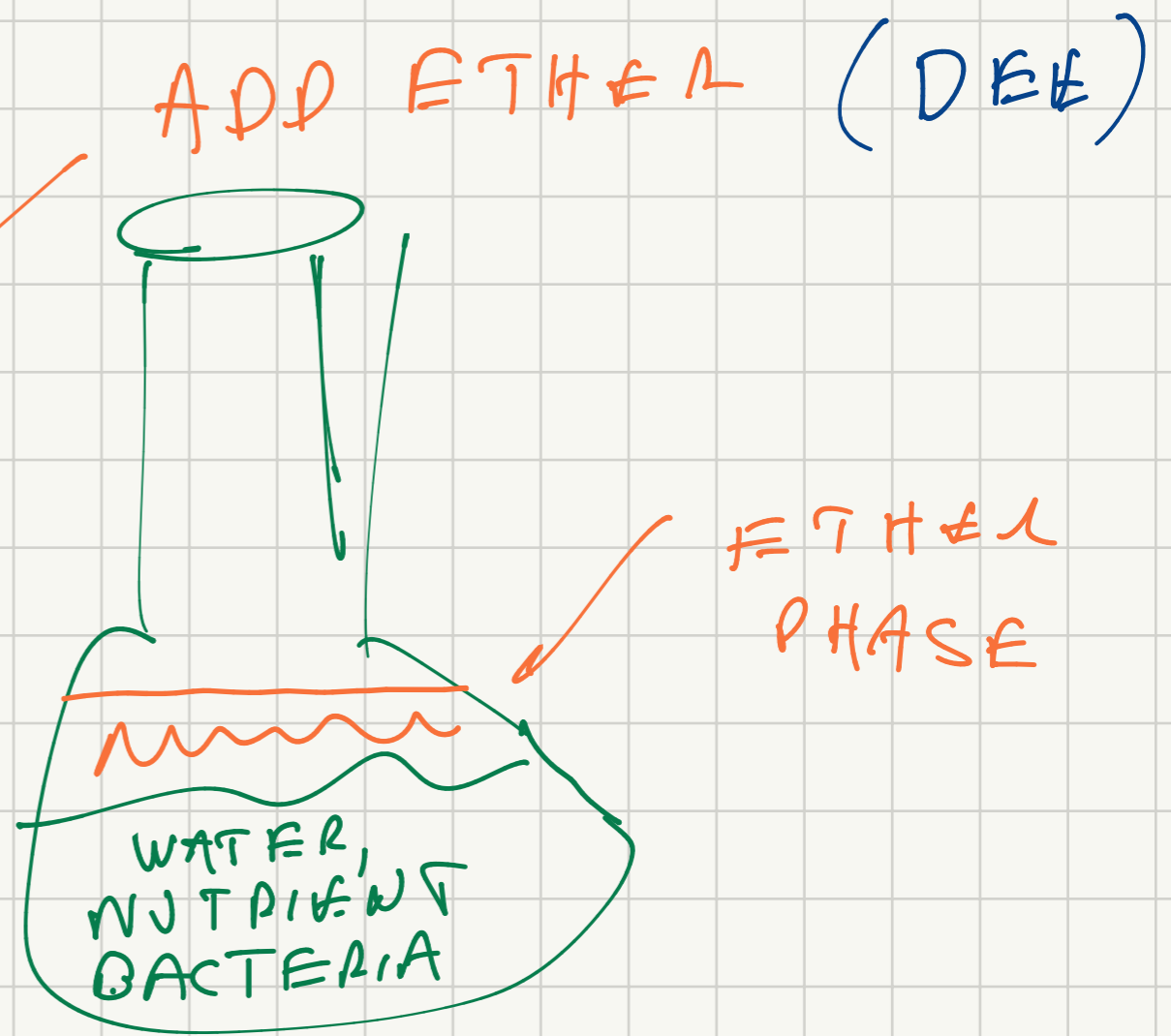
IF WE VAPORIZE AGAIN, WE

WOULD BE CLOSE TO .99

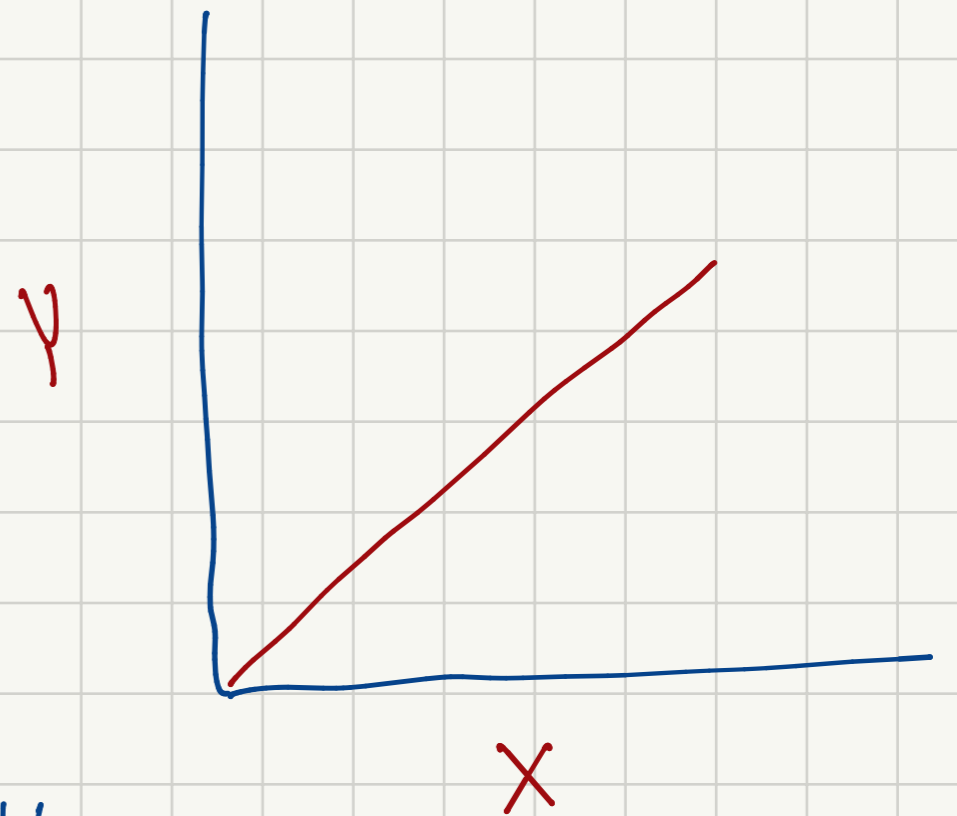
OF COURSE WE WOULD HAVE  
ONLY A SMALL AMOUNT OF PRODUCT.

WE SEE THE PRINCIPLE !!

HOW ABOUT EXTRACTION.



THE BACTERIA  
HAVE PRODUCED  
DESIRED  
COMPOUND  
IT IS AT LEAST  
A LITTLE  
HYDROPHOBIC

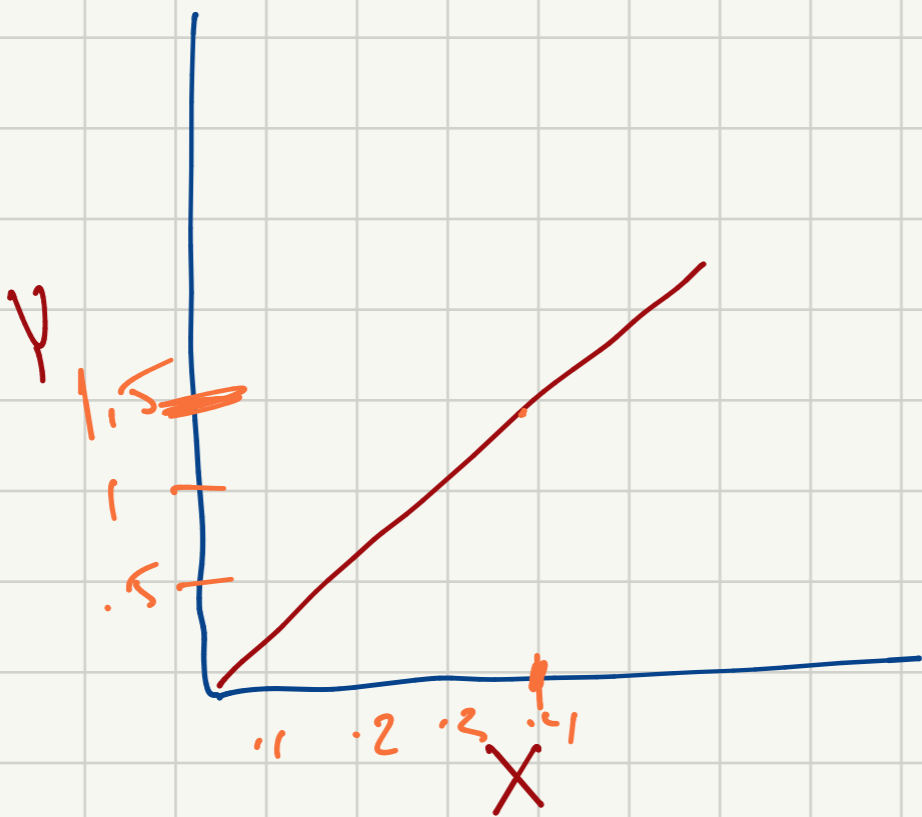


EQUILIBRIUM PARTITIONING

$$Y = m X$$

$$X = \frac{\text{MASS OF P.C.}}{\text{MASS H}_2\text{O}}$$

$$Y = \frac{\text{MASS OF P.C.}}{\text{MASS DEE}}$$

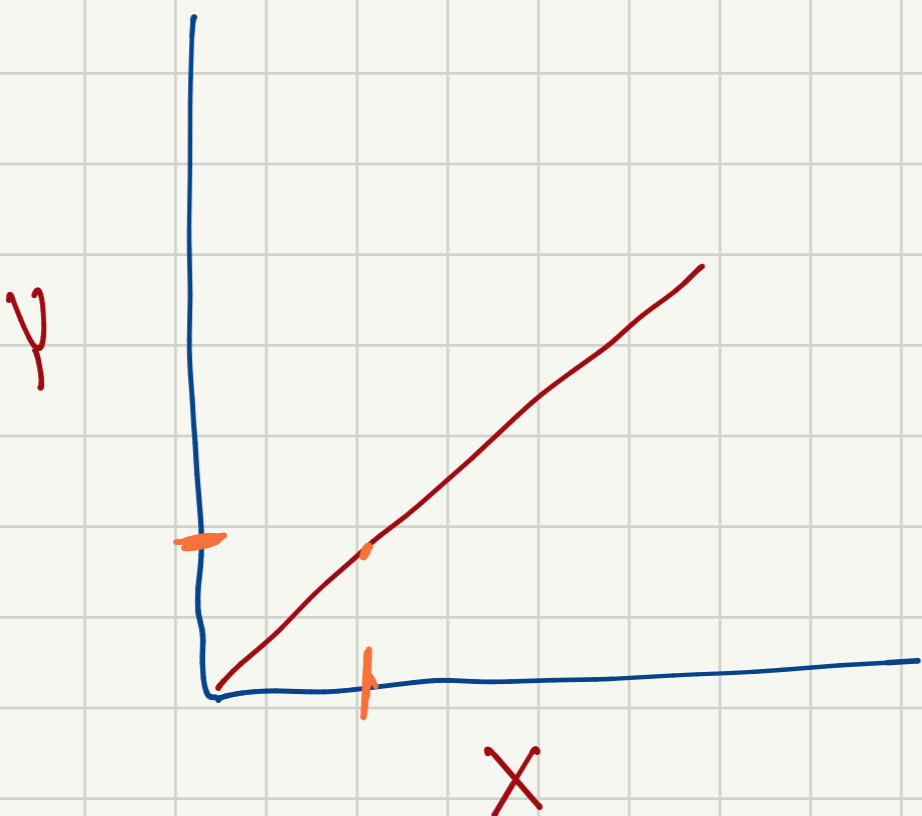


SUPPOSE WE ADD  
500 ML OF DFE TO  
500 BR

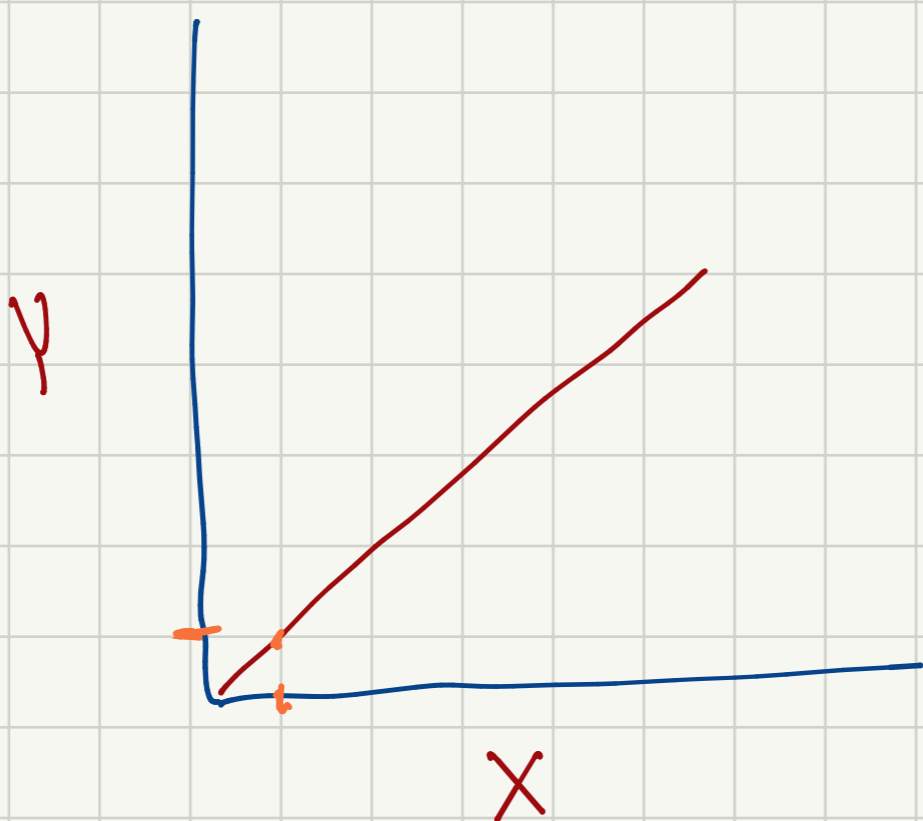
$$X = 0.4$$

$$Y = 1.5$$

WE COULD ADD  
MORE



OR MORE



THIS ACCOMPLISHED

THE GOAL OF

REMOVING

VALUABLE DRUG

FROM BOTH BUT

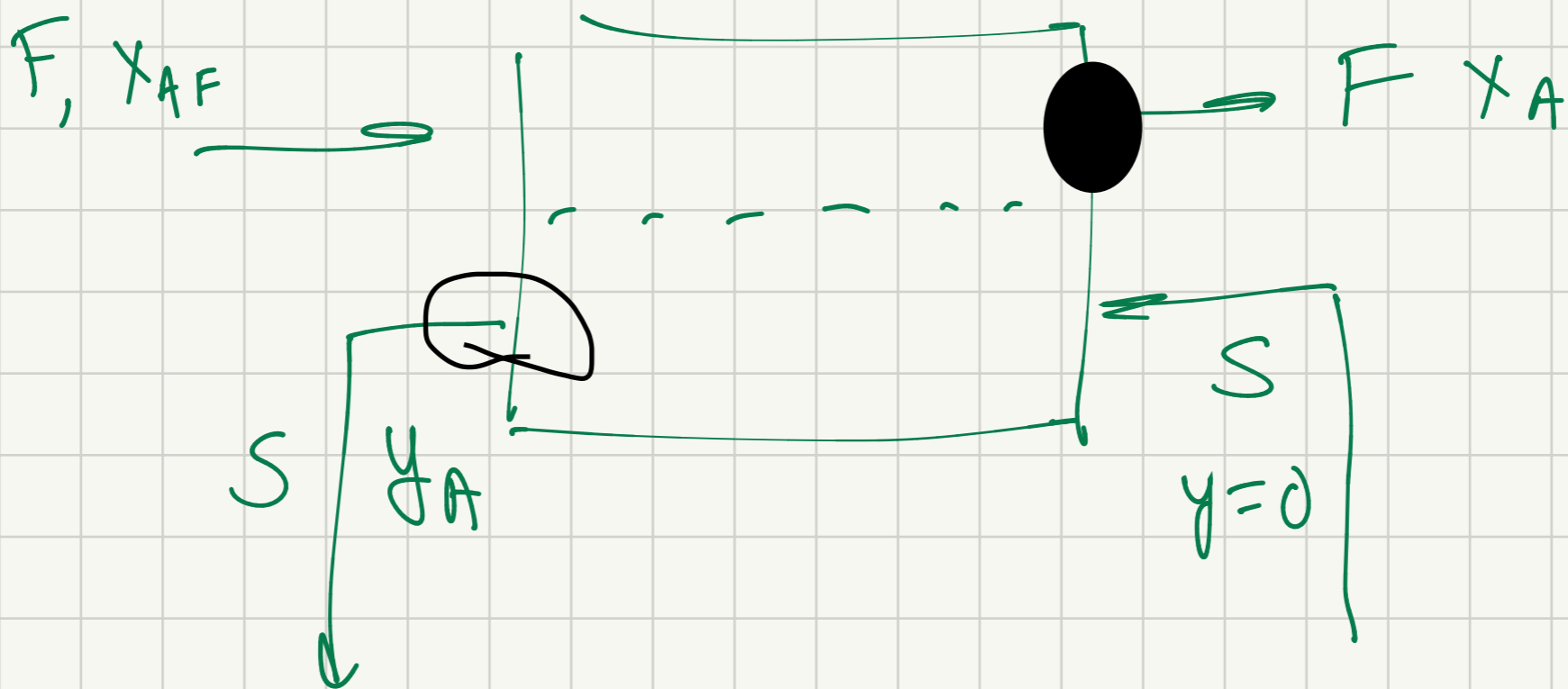
IT IS INCREASINGLY DILUTE!

CONSIDER EXTRACTION

$$Y = m X$$

FEED STREAM,  $F (=) \frac{\text{MASS}}{\text{TIME}}$

SOLVENT STREAM  $S (=) \frac{\text{MASS}}{\text{TIME}}$



$$\cancel{y_s} S + X_{AF} F = F X_A + S y_A$$

(IN) (OUT)

$$y_A = m X_A$$

AMOUNT  
REMAINING  
IN  
FEED  
STREAM

$$X_{AF} F = F X_A + S m X_A$$

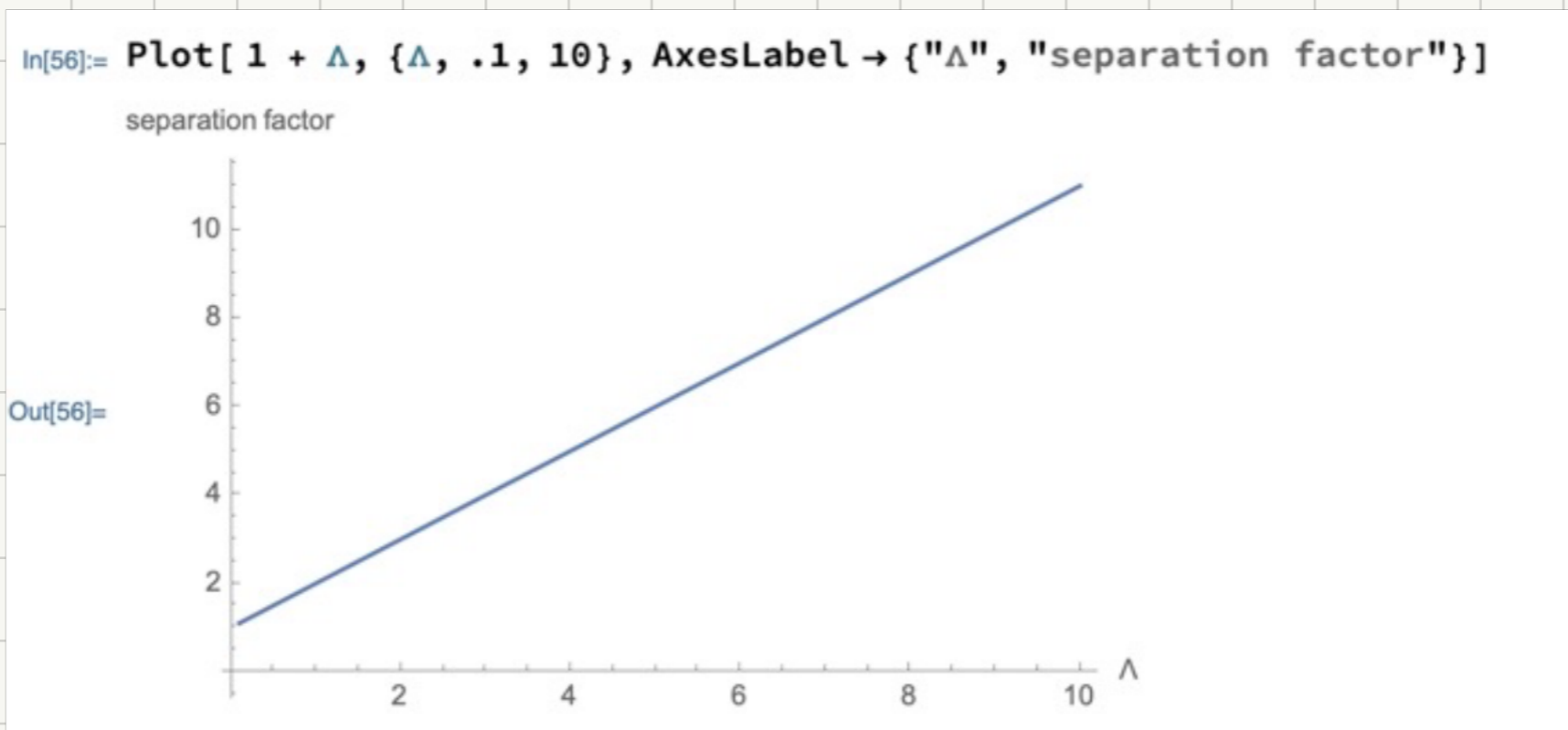
$$\frac{X_A}{X_{AF}} = \frac{1}{1 + \frac{mS}{F}}$$

$$\frac{X_A}{X_{AF}} = \frac{1}{1 + \frac{mS}{F}}$$

PICK,  $\Lambda \equiv \frac{mS}{F}$ ,  $\xi \equiv \frac{X_{AF}}{X_A}$

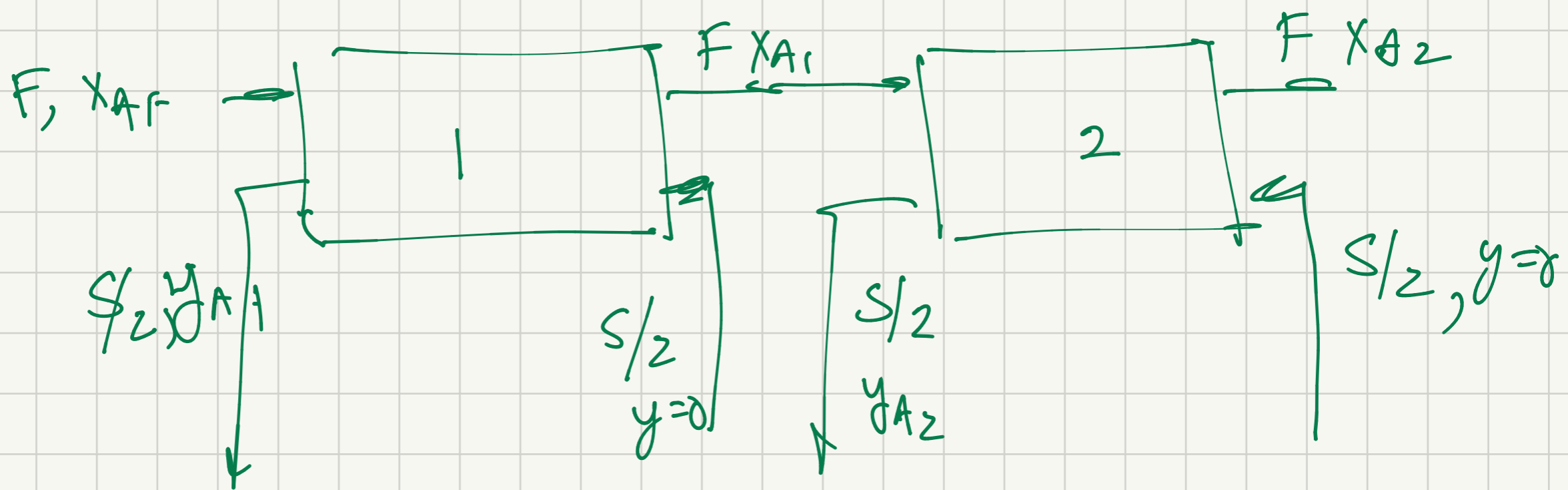
'BIGGER' IS BETTER

$$\xi = 1 + \Lambda$$



m MAY BE FIXED BY CHEMISTRY  
OTHER WISE MUST INCREASE S.!!

# SUPPOSE



①

$$F x_{AF} = F x_{A1} + \frac{S}{2} y_{A1}$$

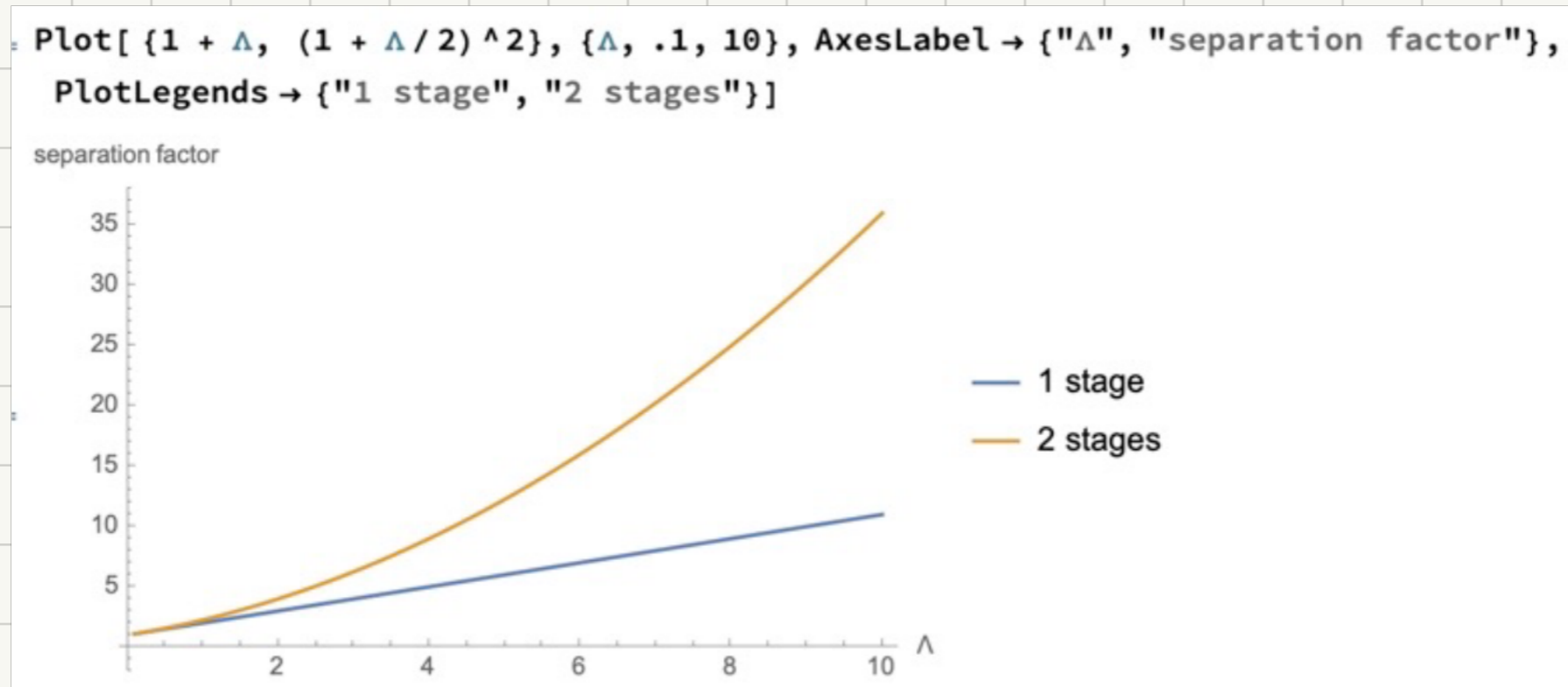
$$y = m x$$

②

$$F x_{A1} = F x_{A2} + \frac{S}{2} y_{A2}$$

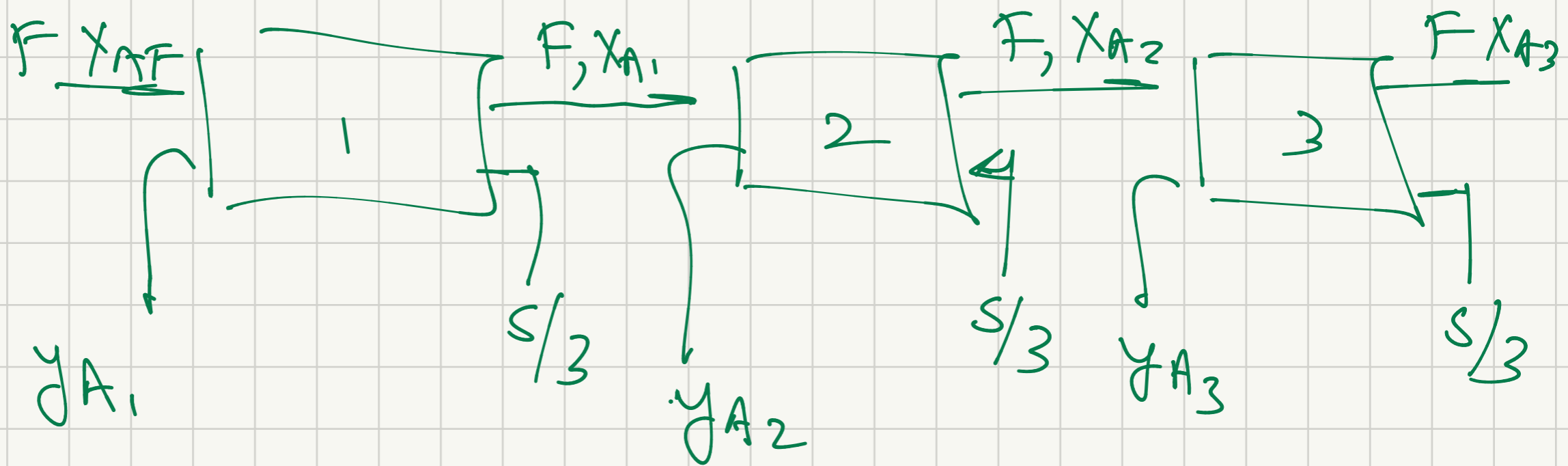
$$\xi_2 = \left(1 + \frac{\Delta}{2}\right)^2$$

TWO STAGES IS BETTER



HOW ABOUT 3...

CROSS  
CURRENT



$$F_{X_{AF}} = F_{X_{A_1}} + y_{A_1} \frac{S}{3}$$

$$F_{X_{A_1}} = F_{X_{A_2}} + y_{A_2} \frac{S}{3}$$

$$F_{X_{A_2}} = F_{X_{A_3}} + y_{A_3} \frac{S}{3}$$

$$\xi_3 = \frac{X_{AF}}{X_{A_3}} = \left(1 + \frac{1}{3}\right)^3$$

WE CAN NOW GUESS...

$$\xi_m = \left(1 + \frac{1}{n}\right)^m$$

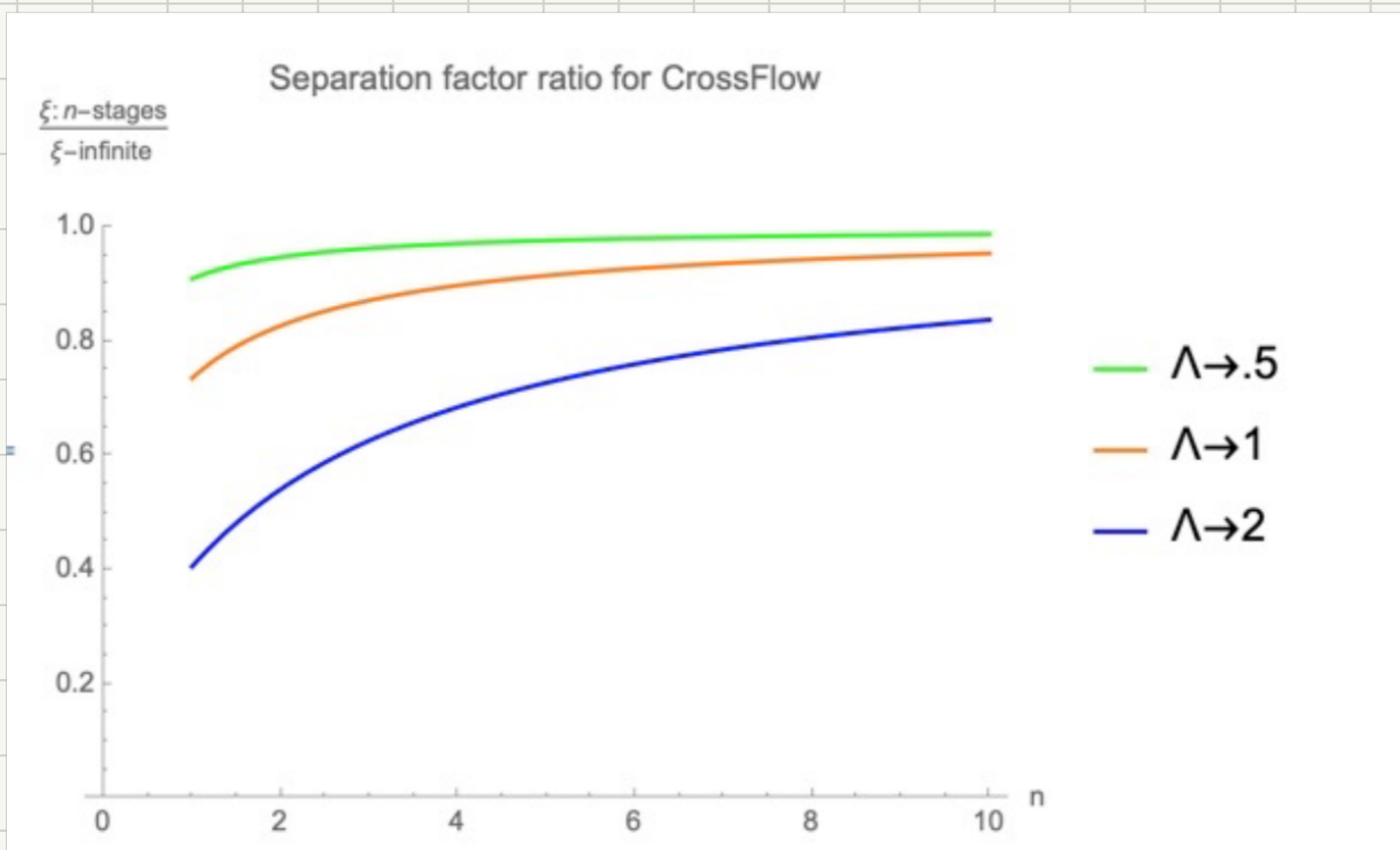
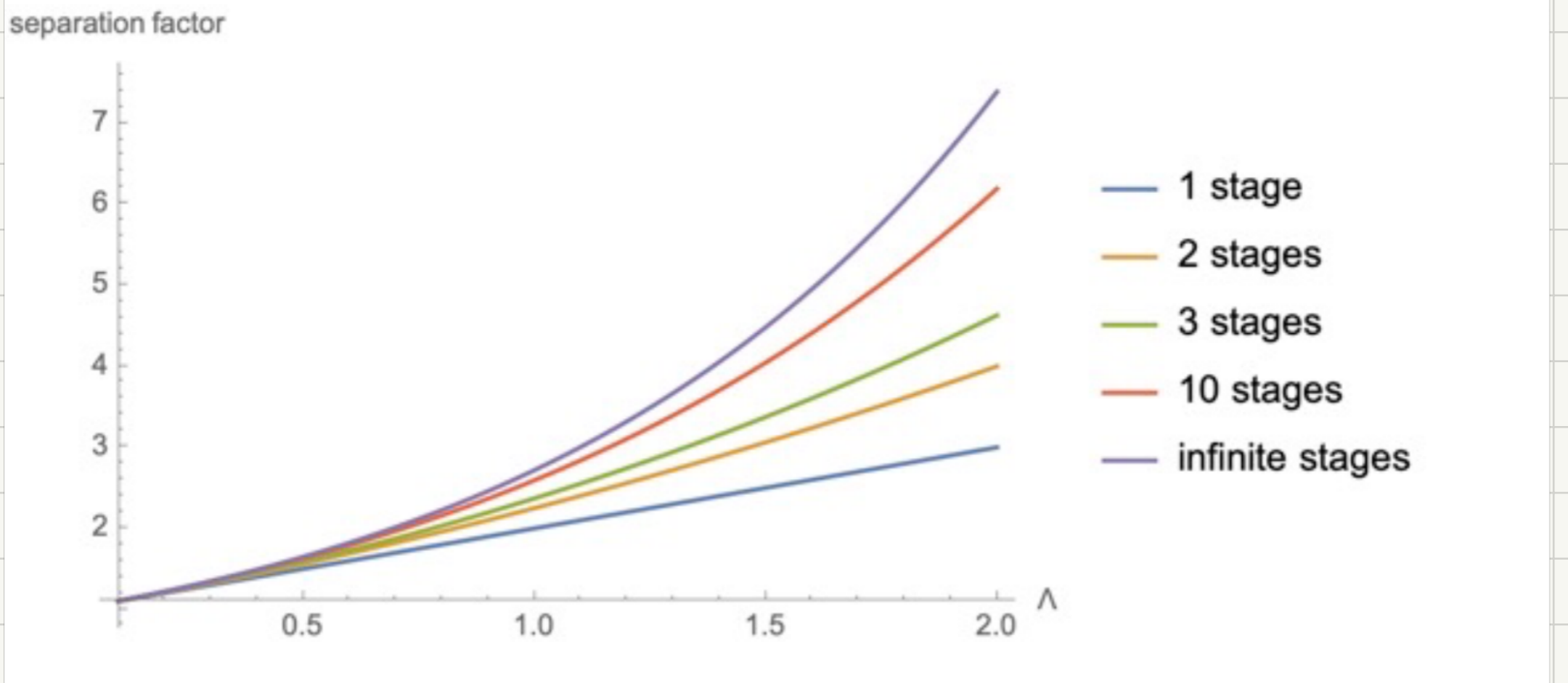
As  $m \rightarrow \infty$  ...



$$\xi_{\infty} = \text{Exp}(\Lambda)$$

WHICH SEEMS REALLY GOOD!!

```
Plot[ {1 + Δ, (1 + Δ/2)^2, (1 + Δ/3)^3, (1 + Δ/10)^10, Exp[Δ]}, {Δ}
AxesLabel -> {"Δ", "separation factor"},
PlotLegends -> {"1 stage", "2 stages", "3 stages", "10 stages", "infi
```

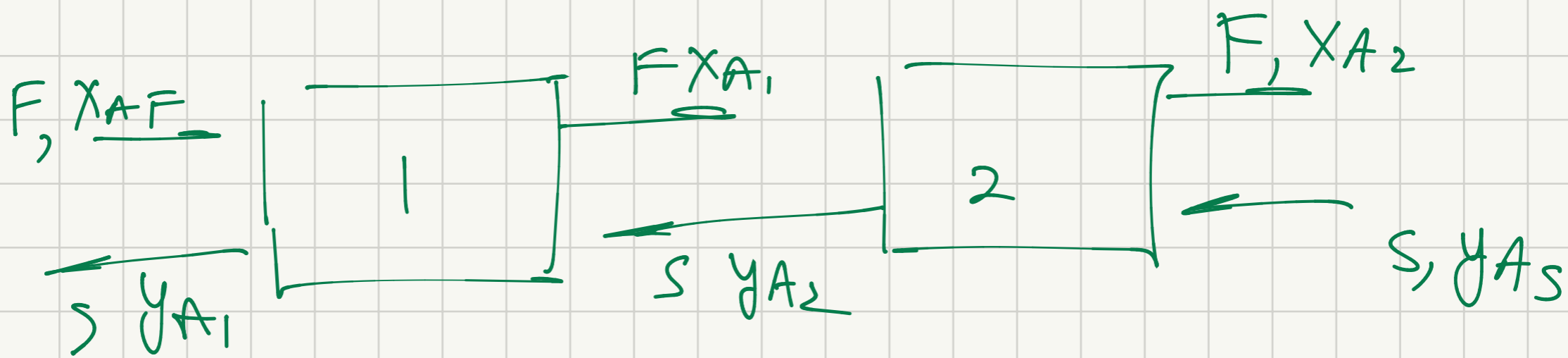


IF  $\Lambda > 1$   
 MORE  
 STAGES  
 HELPS  
 FOR QUITE  
 A LOT OF  
 STAGES  
 IF YOU NEED  
 IT!!

HOWEVER... WE CAN DO  
EVEN BETTER !!

(CAN AN EXPONENTIAL BE BEAT?)

COUNTER CURRENT



①

$$F X_{AF} + S y_{A2} = F X_{A1} + S y_{A1}$$

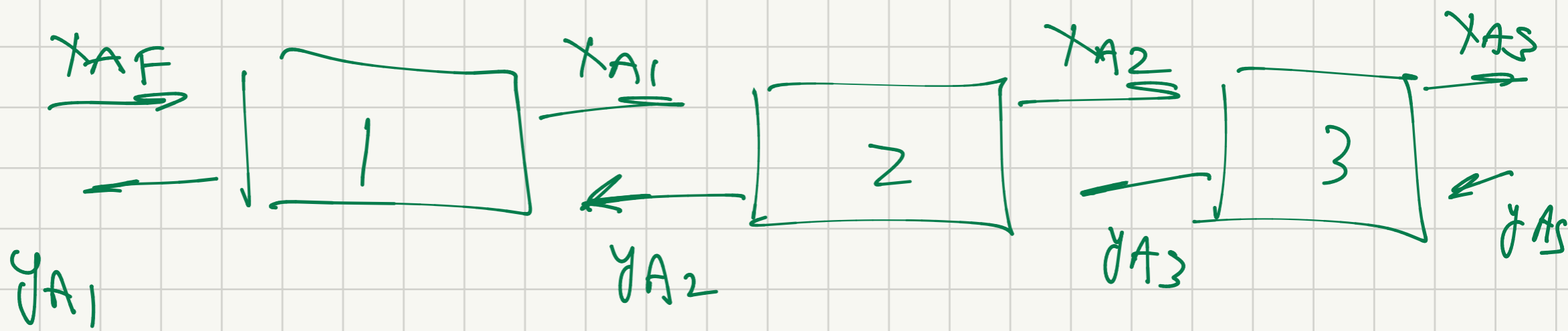
②

$$F X_{A1} + S y_{AS} = F X_{A2} + S y_{A2}$$

$$X_{A2} = \frac{X_{AF}}{1 + \Lambda + \Lambda^2}$$

$$y_{A2} = \frac{y_{AS}}{1 + \Lambda + \Lambda^2}$$

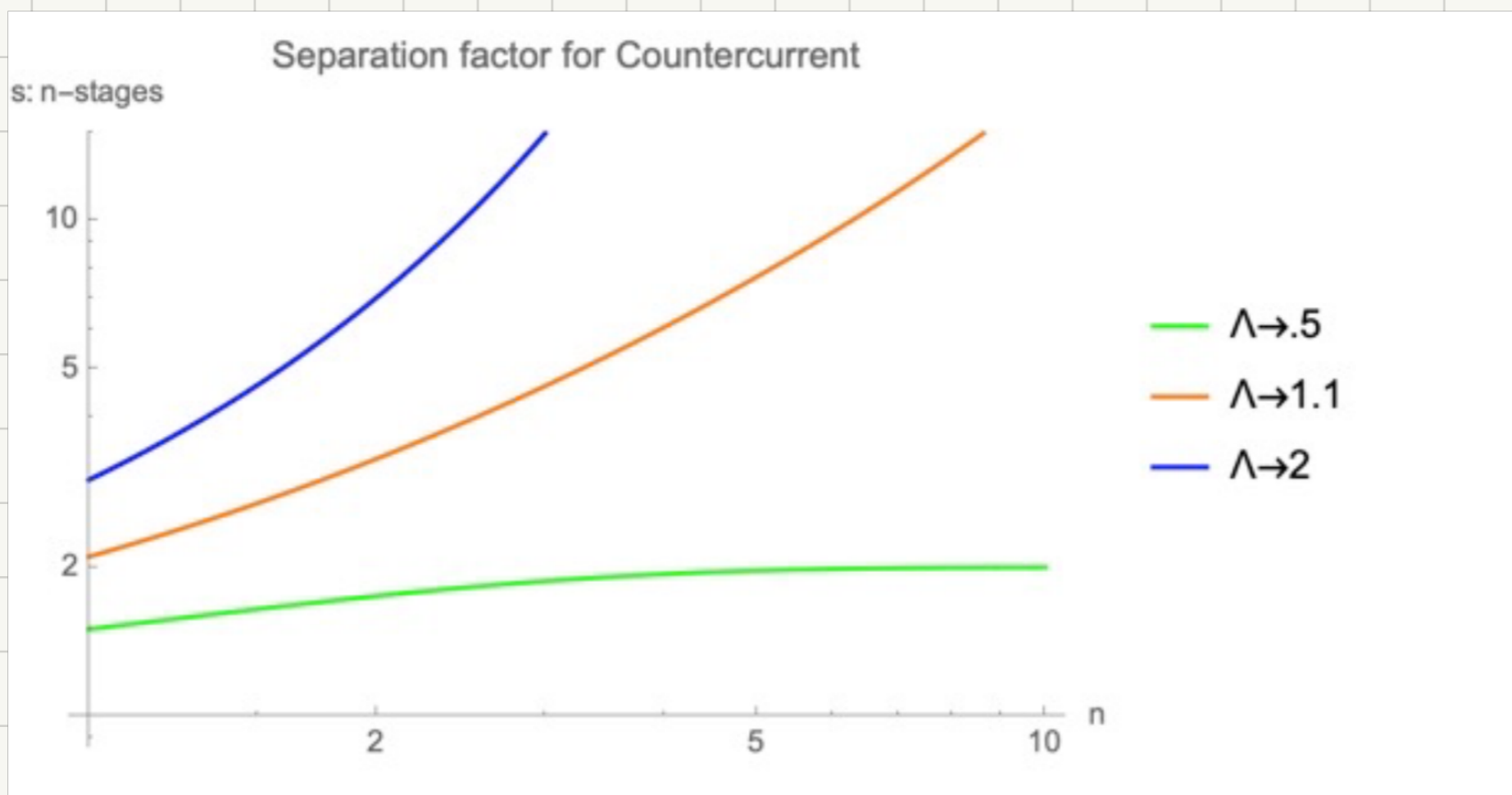
LET'S CHECK 3 . . . .



$$\frac{X_{A3}}{X_{AF}} = \frac{1}{1 + \Lambda + \Lambda^2 + \Lambda^3}$$

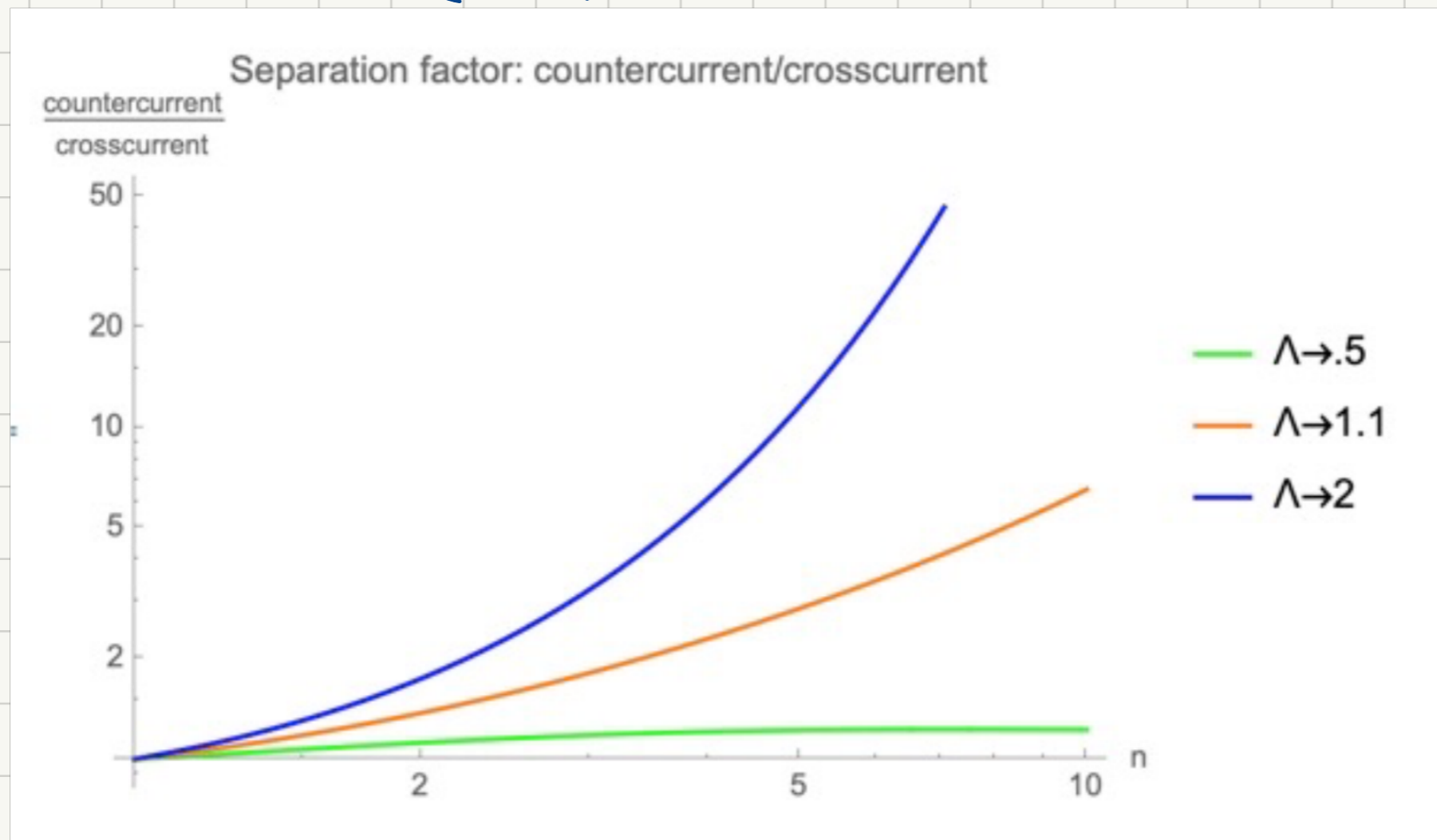
SO WE HAVE

$$\xi_m = \sum_{i=0}^m \Lambda^i$$



IF  $\Lambda > 0$   
CAN GET  
AS LARGE  
OF  $\xi$   
AS YOU  
NEED

WE COMPARE CROSS CURRENT TO COUNTERCURRENT...



IF  $\Lambda > 1$ , SUBSTANTIAL BENEFIT

CROSS CURRENT  $\xi_{\infty} = \exp(\Lambda)$

IF  $\Lambda$  IS LIMITED,  $\xi$  IS LIMITED

COUNTERCURRENT

$$\xi_{\infty} = \sum_{i=0}^{\infty} \Lambda^i$$

IF  $\Lambda > 1$

$\xi$  IS UNLIMITED.

SO ALMOST ALWAYS... COUNTERCURRENT.

KEY DIMENSIONLESS PARAMETER:

$$\Lambda \equiv \frac{m S}{F}$$

$$\xi_n = \sum_{i=0}^n \Lambda^i$$

$$\xi_n = \frac{\Lambda^{n+1} - 1}{\Lambda - 1}$$

$$n = \frac{\ln(1 + (\Lambda - 1)\xi_n)}{\ln(\Lambda)} - 1$$

KREMSER EQ

# EXTRACTION COLUMN

## Mixco (Lightnin CMContactor) (Oldshue-Rushton) Column.

REFERENCES: Oldshue and Rushton, *Chem. Eng. Progress*, 48, 297 (1952). Dykstra, Thompson, and Clouse, *Ind. Eng. Chem.*, 50, 161 (1958). Gustison, Treybal, and Capps, *Chem. Eng. Progress, Symp. Ser.*, in press.

Refer to Fig. 21-47. The extractor is an extension of the simple baffled mixing vessel into a multistage column.

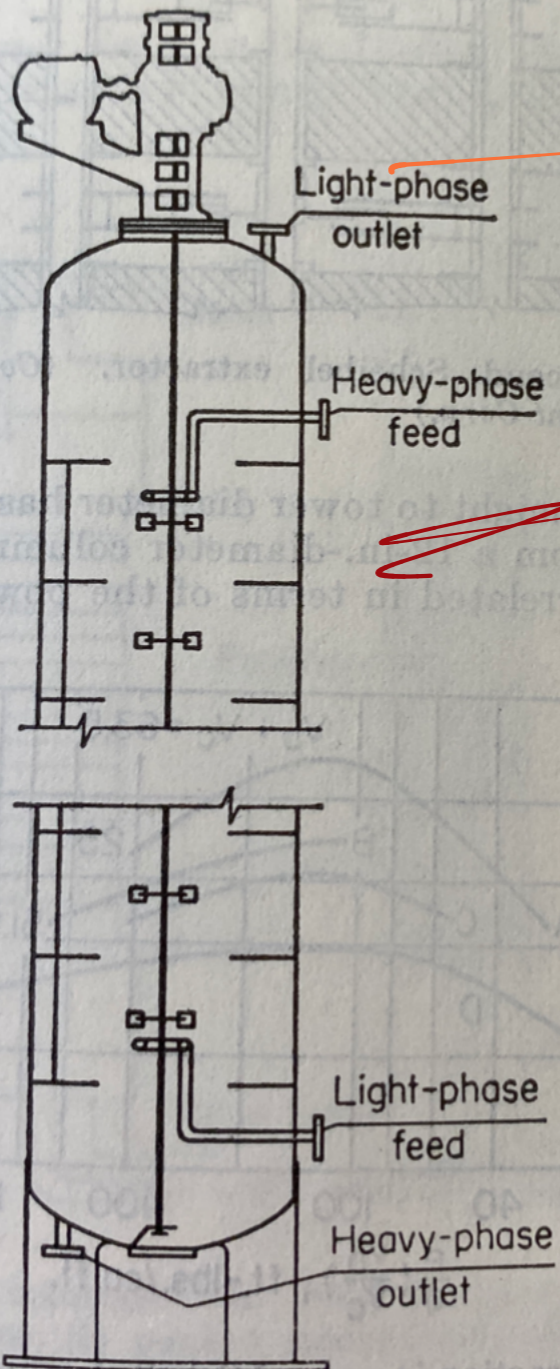


Fig. 21-47. Mixco (Oldshue-Rushton) extractor.

Although commercial application has been made, data are scarce and limited to towers of small diameter. The preferred proportions are  $Z = 0.5T$ ,  $d_c > d_i$ .

H.E.T.S., ft.

Fig. 21-4  
ketone-ac  
X = flood

[Data of C

A som  
Eguchi,  
20, 2 (1  
(1957);  
is chara  
between  
centric  
column,  
( $V_c =$   
fraction

Sche

REFER  
1958; Br  
771 (194  
Eng. Ch

MAYBE,  
EVAPORATE  
SOLVENT  
CRYSTALLIZE  
PRODUCT

PROBABLY  
NEVER  
ACCUMULATION  
IN EQ.  
PLUS NEVER  
ALLOWED  
TO  
SEPARATE  
INTO  
PHASES

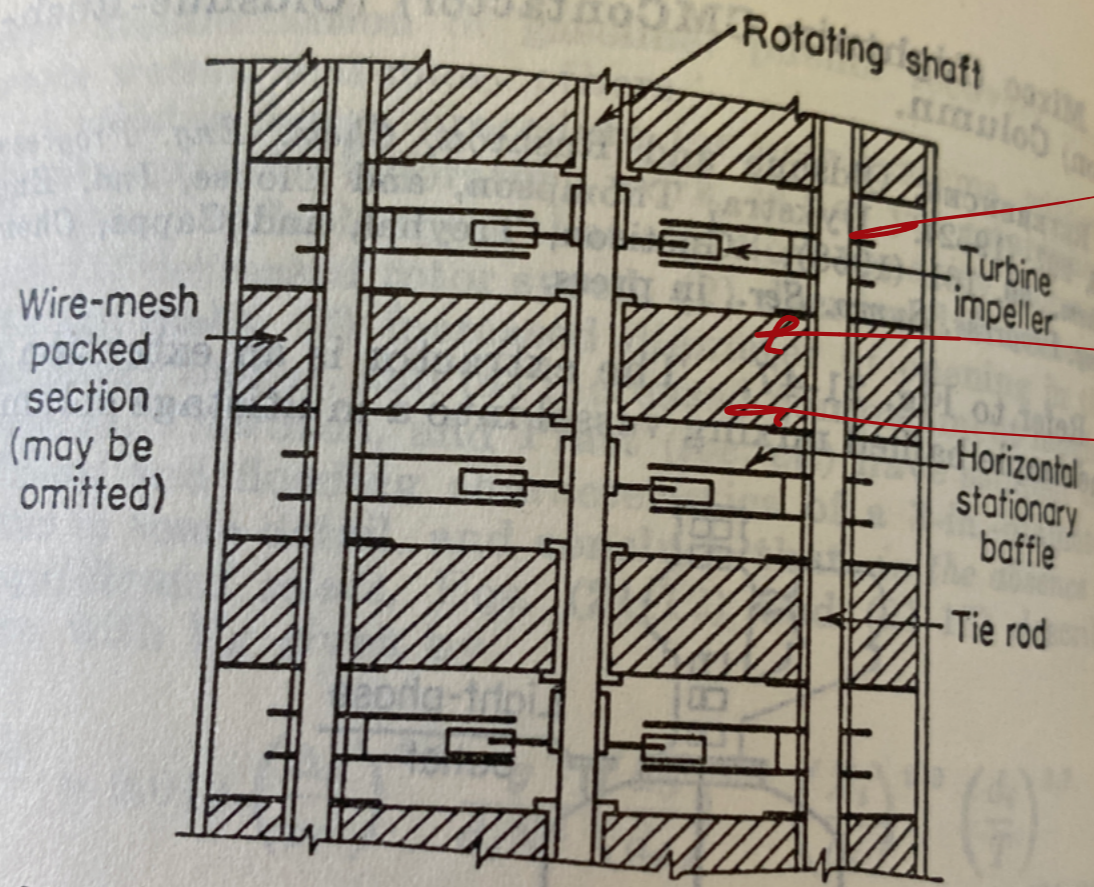
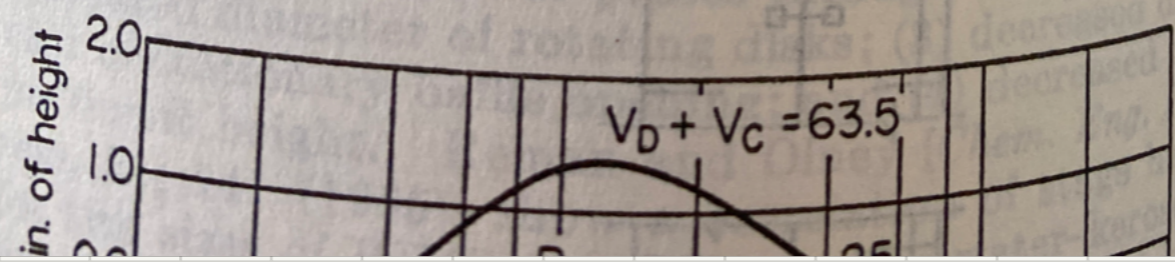


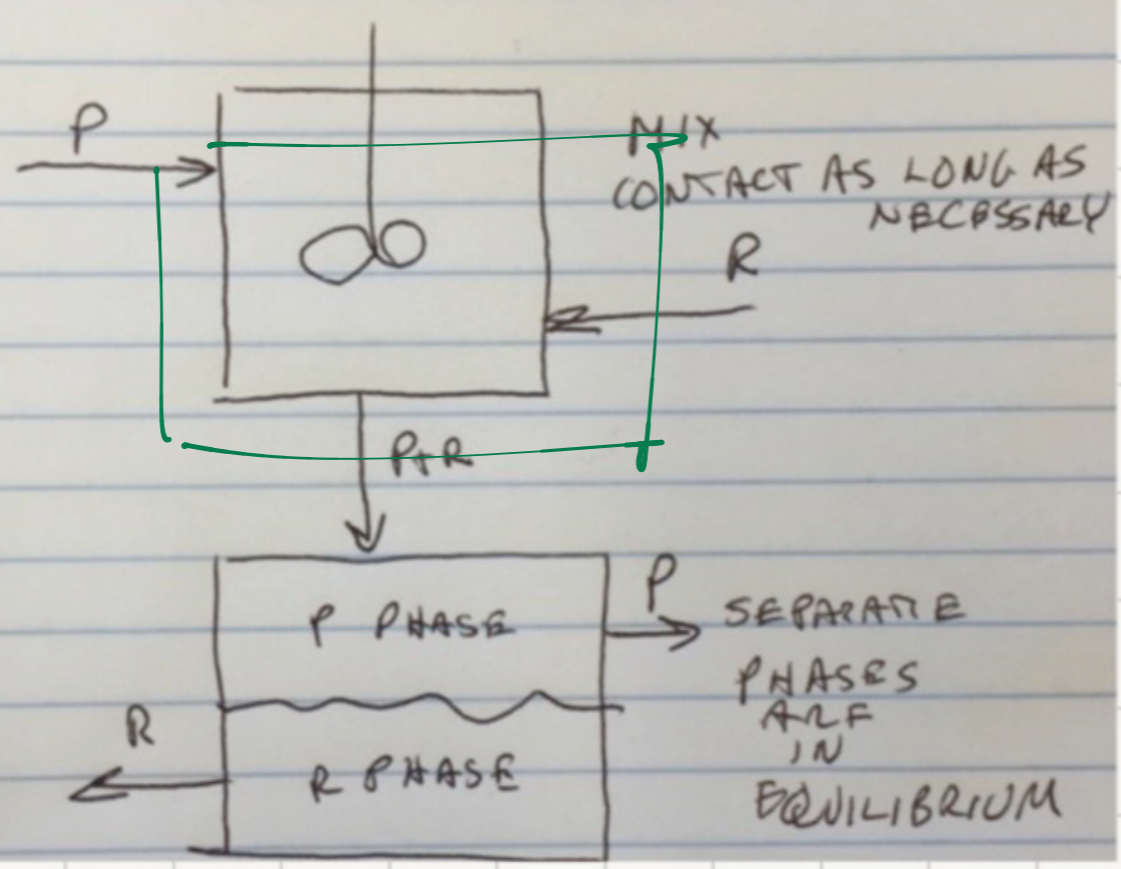
FIG. 21-51. Second Scheibel extractor. (Courtesy of York Process Equipment Corp.)

compartment height to tower diameter has been reduced. Data taken from a 12-in.-diameter column are shown in Fig. 21-52, correlated in terms of the power applied per



MIXING  
SETTLING

SCHEMATIC OF EQUILIBRIUM STAGE



IDEALLY AN EXTRACTOR LOOKS MORE LIKE THIS...

# FOR DISTILLATION

EACH TRAY COULD BE CLOSE TO EQUILIBRIUM

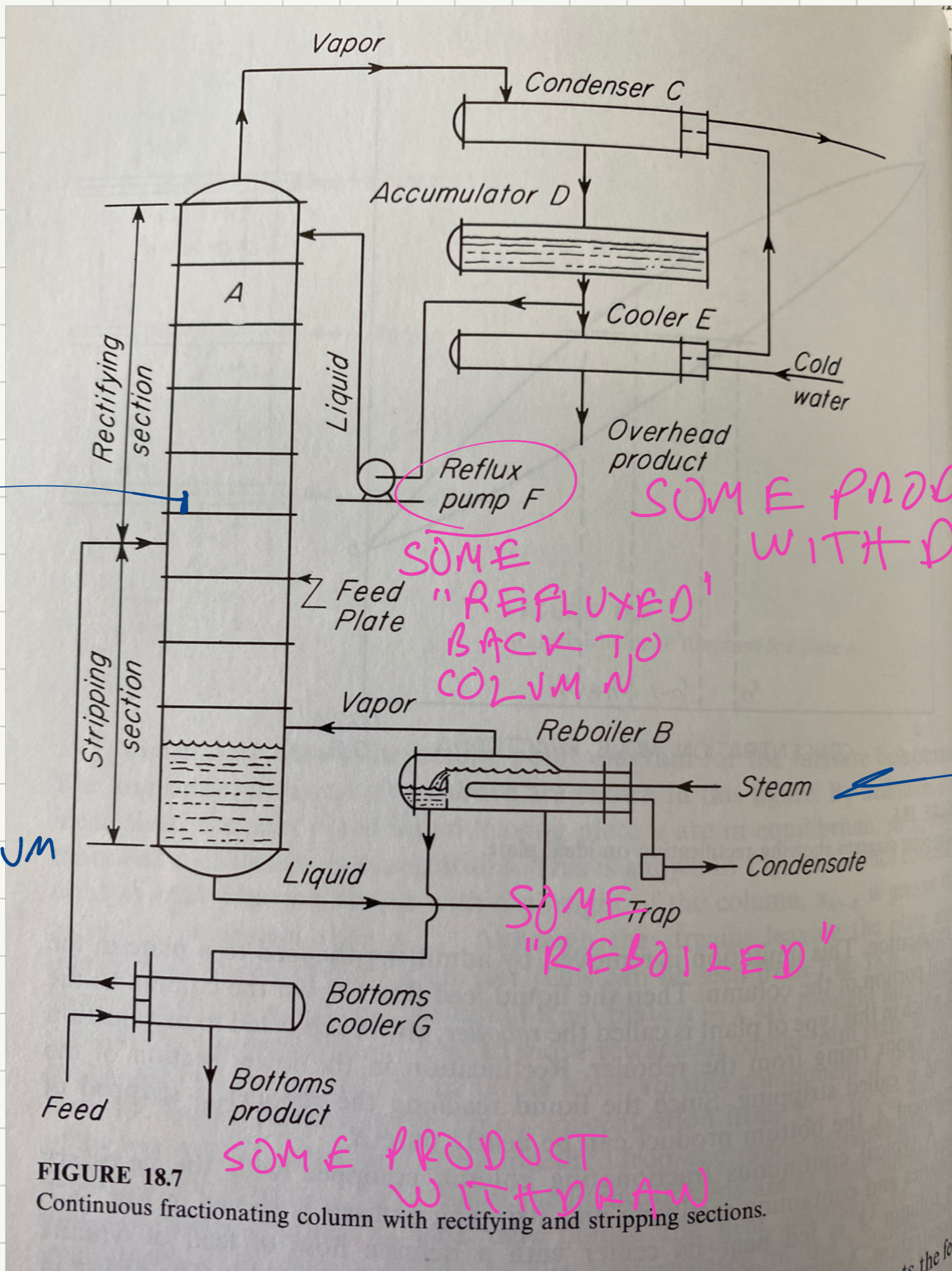


FIGURE 18.7 Continuous fractionating column with rectifying and stripping sections.

SOME PRODUCT WITHDRAWN

SOME "REFLUXED" BACK TO COLUMN

SOME "REBOILED"

SOME PRODUCT WITHDRAWN

HEAT IN PROVIDES ENERGY TO ALLOW SEPARATION

INNERENT TRADE OFF BETWEEN # TRAYS & RATE OF HEATING

CAPITAL COSTS

OPERATING COSTS



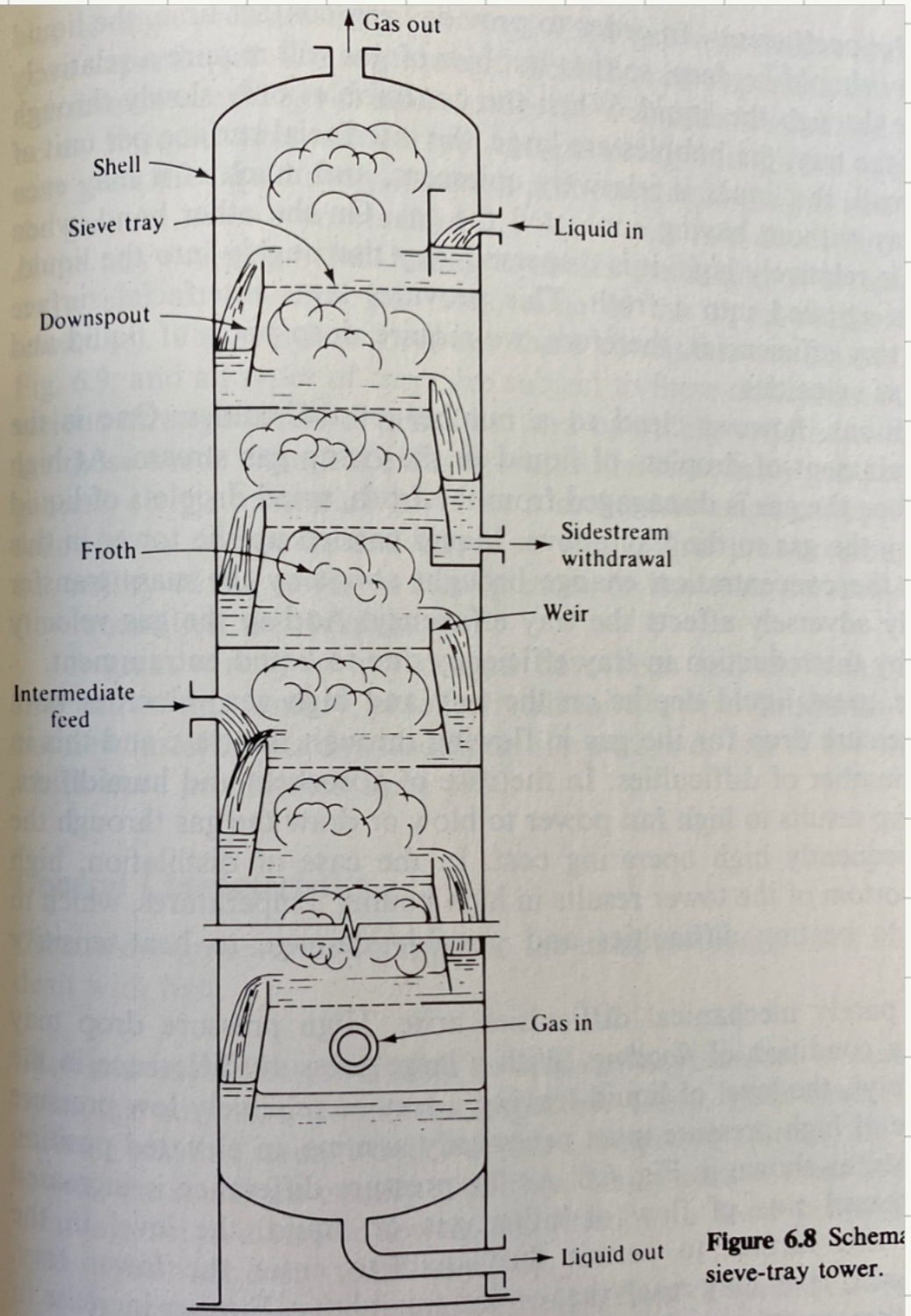
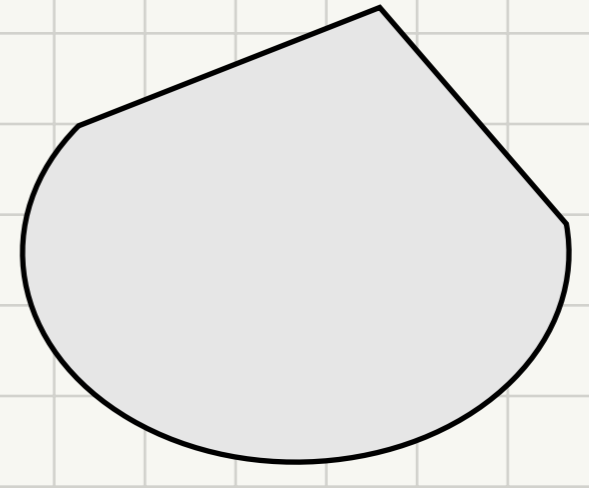


Figure 6.8 Schematic sieve-tray tower.

the mechanical design used and the conditions of operation. The tower, on the other hand, depends upon the quantities of liquid through the tray. Once the number of equilib

# FLOWS WITHIN A COLUMN



# SIEVE TRAY

# BOILING MIXTURE

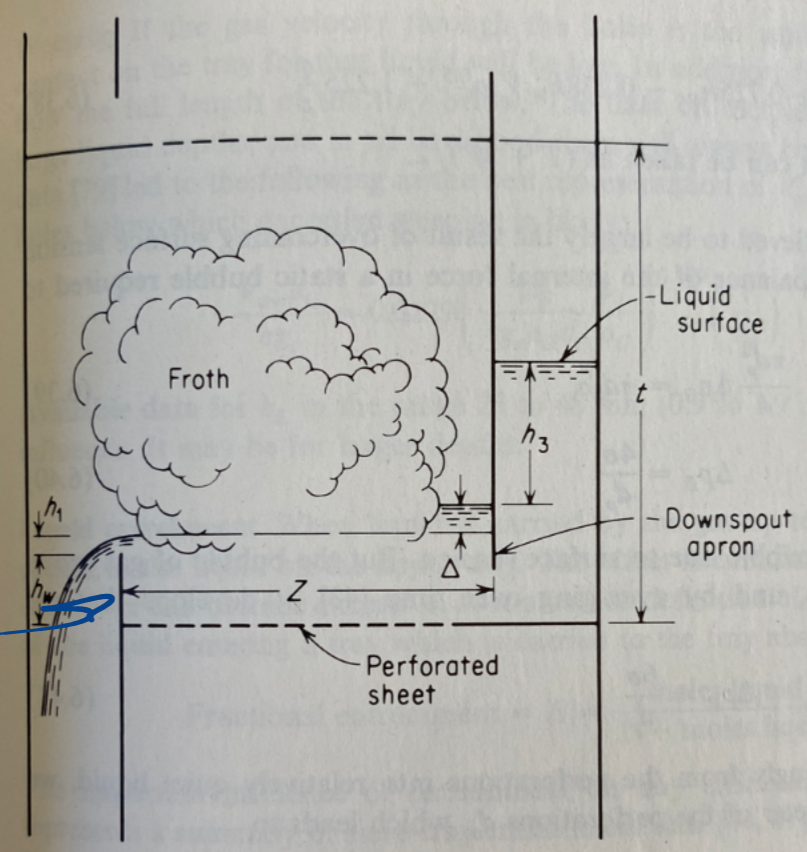


Figure cross-f

thickness, and an exit loss [64]

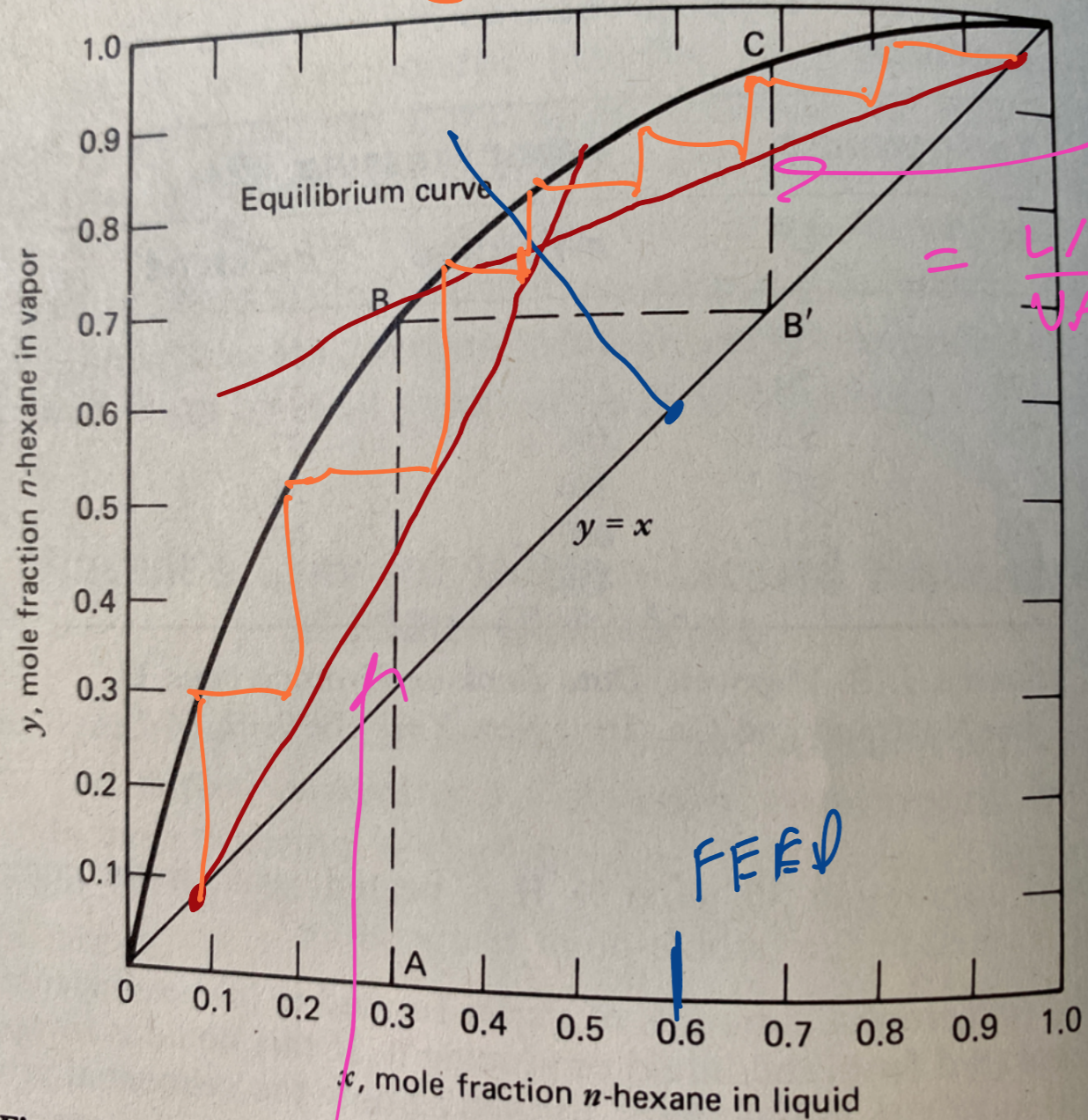
$$\frac{2h_D g \rho_L}{V_o^2 \rho_G} = C_o \left[ 0.40 \left( 1.25 - \frac{A_o}{A_n} \right) + \frac{4lf}{d_o} + \left( 1 - \right. \right.$$

The Fanning friction factor  $f$  is taken from a standard chart [15].  $C_o$  depends upon the ratio of plate thickness to hole diameter [82]. Over

$$C_o = 1.09 \left( \frac{d_o}{t} \right)^{0.25}$$

# Thermodynamic Equilibrium Diagrams

8-TRAYS



FROM THIS  
y-x DIAGRAM  
AND MASS  
BALANCES

SLOPE  
= LIQUID FLOW  
VAPOR FLOW

FEED

McCABE-THIELE

METHOD

WE TOOK A  
FEED OF

$$x_H = .6$$

AND SEPARATED  
IT INTO

$$x_H = .95$$

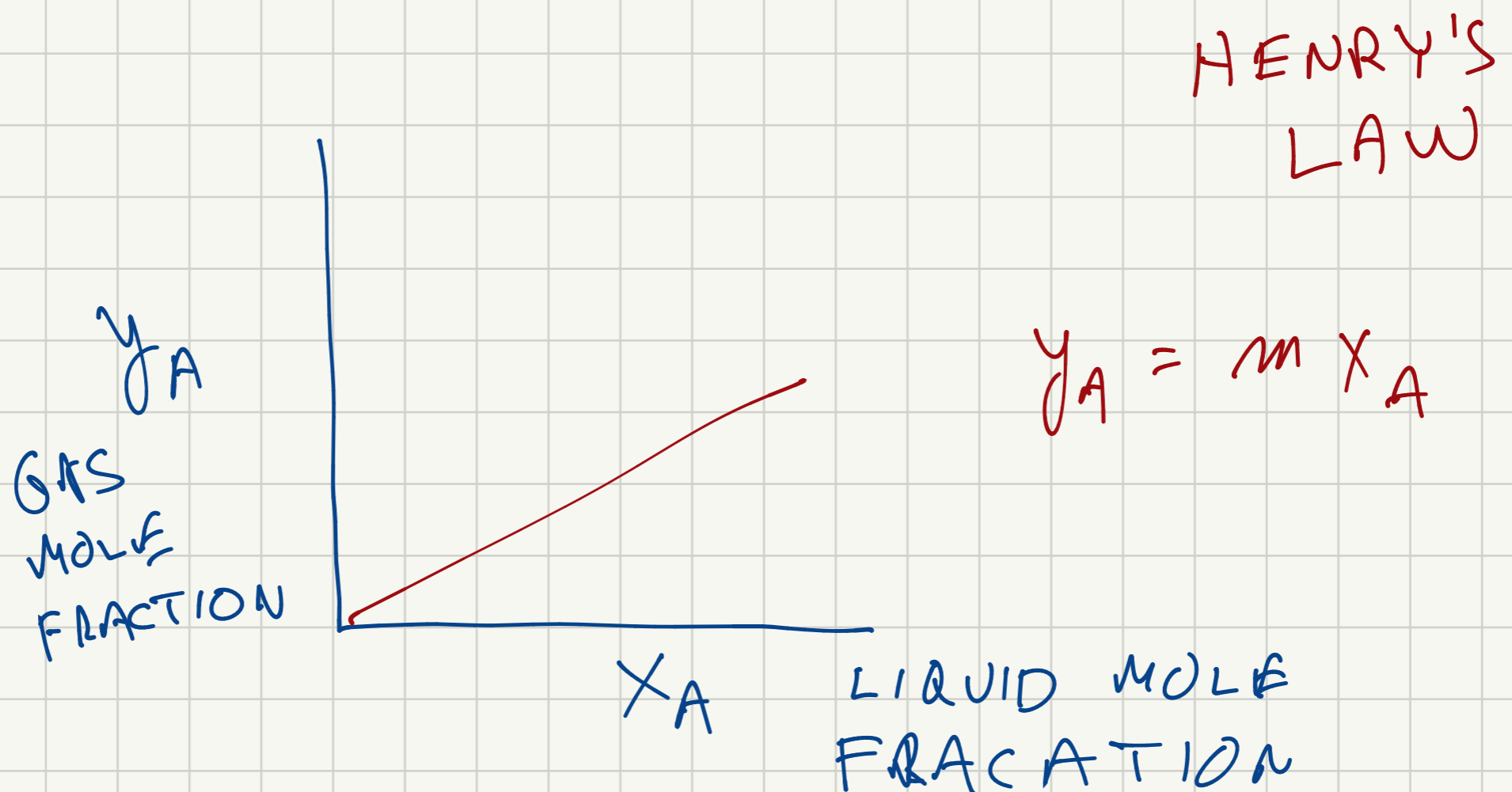
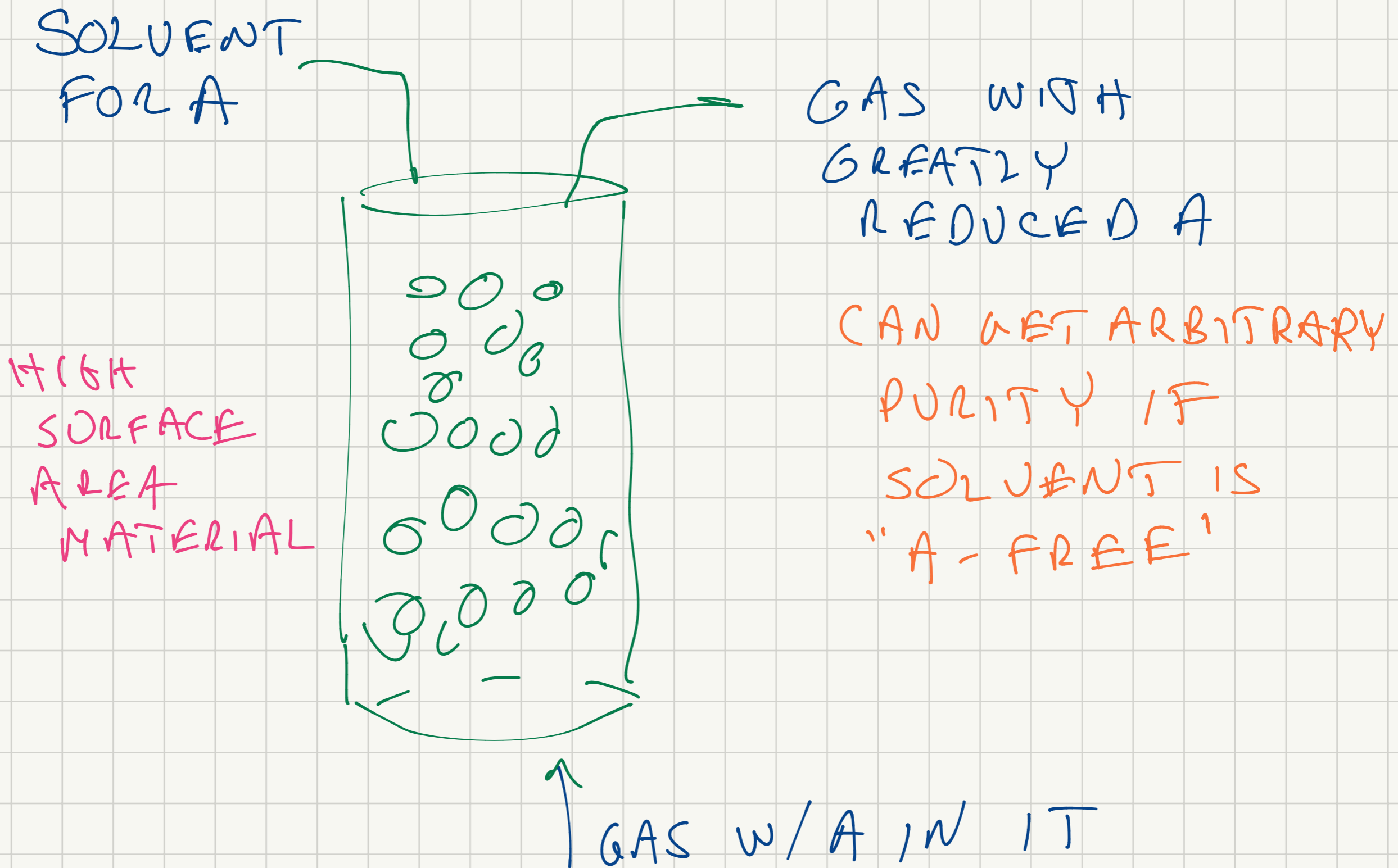
$$x_H = .1$$

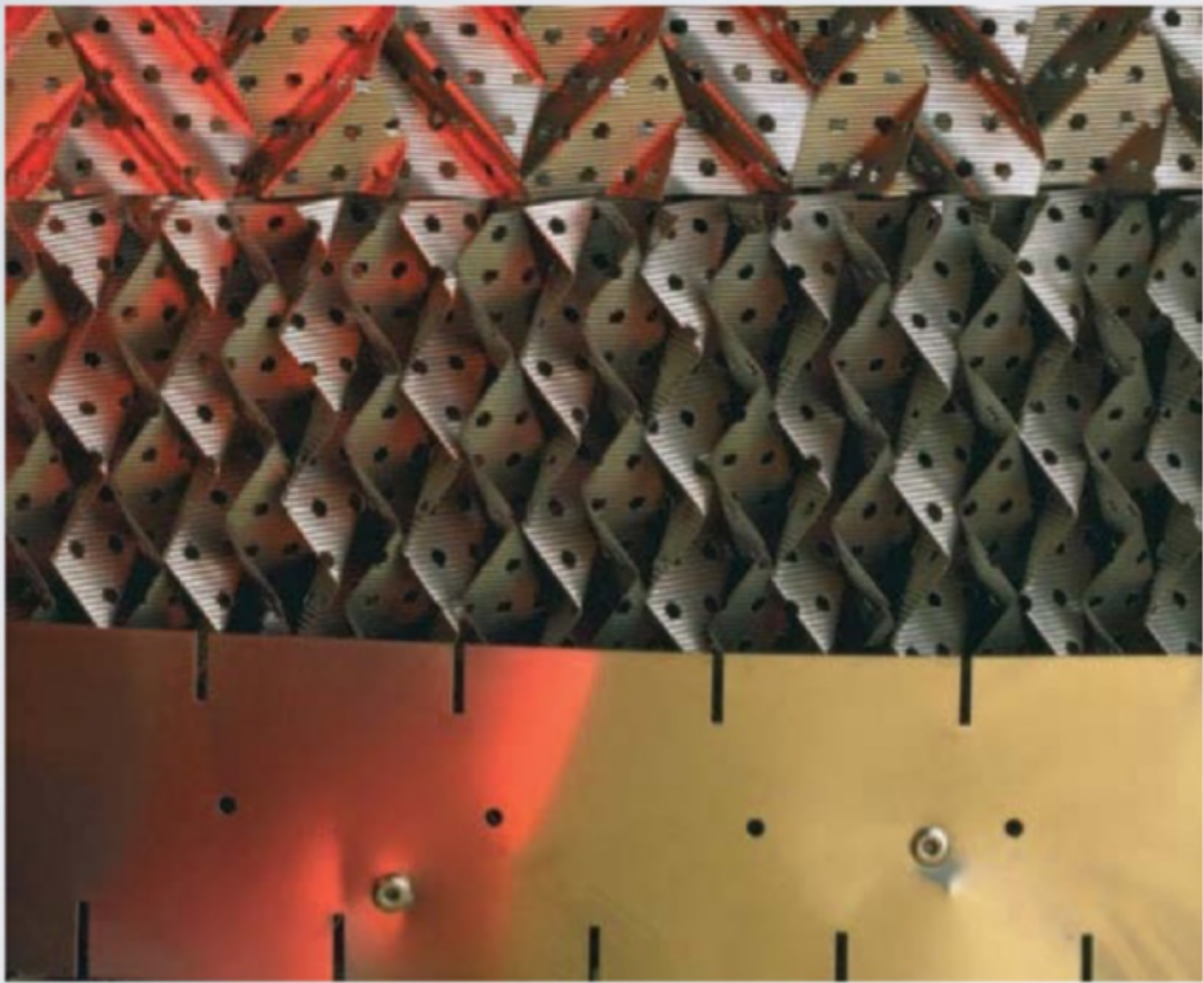
USING 8  
EQUILIBRIUM  
STAGES

Figure 3.3. The x-y diagram for n-hexane-n-octane, at 101 kPa. (E. J. Henley and E. M. Rosen, *Material and Energy Balance Computations*, John Wiley & Sons, New York, © 1969.)

COMPONENT MASS BALANCE  
GIVES "OPERATING" LINE

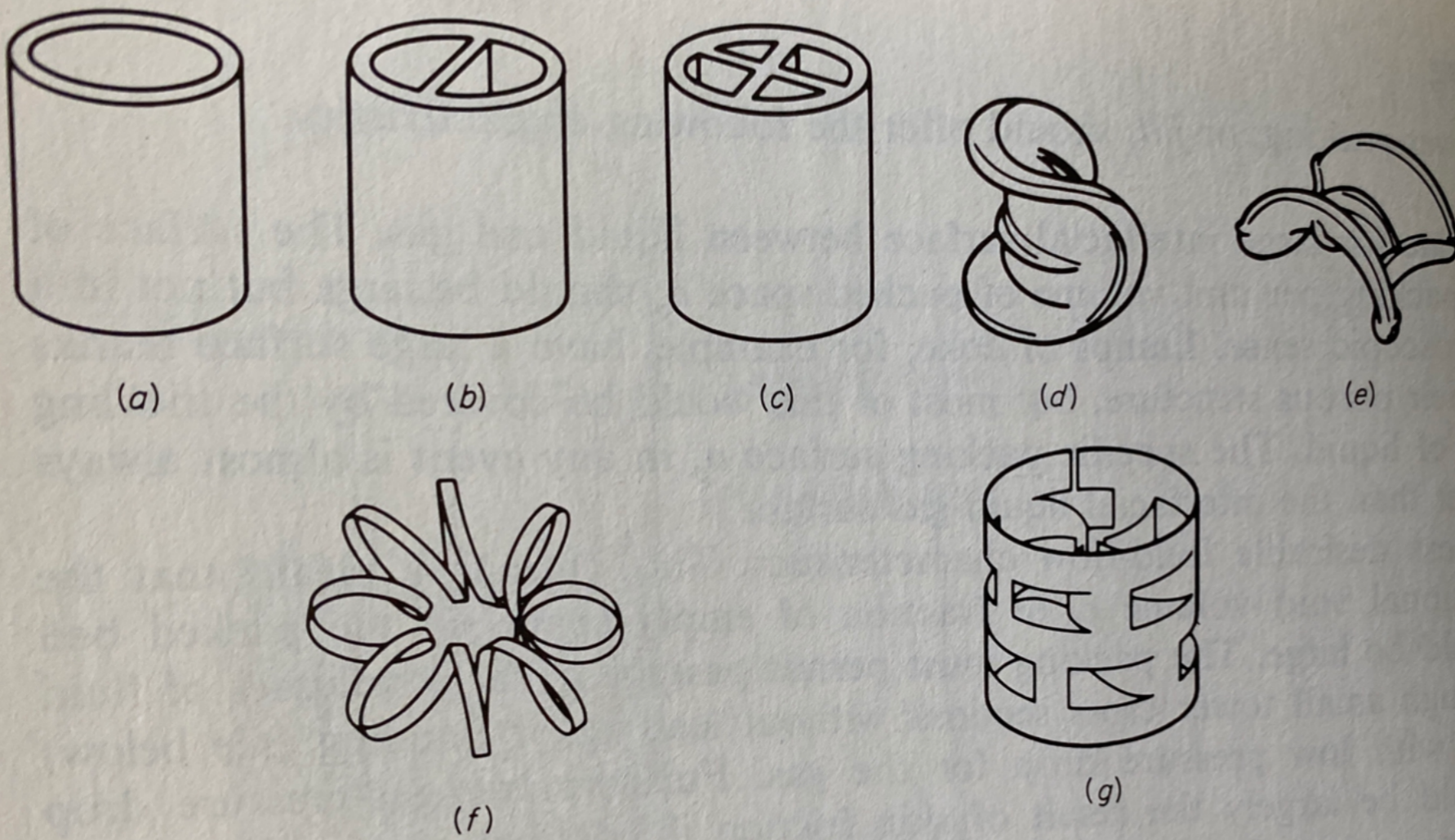
AS IT TURNS OUT, YOU  
DON'T ACTUALLY HAVE TO  
USE EQUILIBRIUM STAGES.





Structured

"DUMPED" PACKING



**Figure 6.28** Some random tower packings: (a) Raschig rings, (b) Lessing ring, (c) partition ring, (d) Berl saddle (courtesy of Maurice A. Knight), (e) Intalox saddle (Chemical Processing Products Division, Norton Co.), (f) Tellerette (Ceilcote Company, Inc.), and (g) pall ring (Chemical Processing Products Division, Norton Co.).

ings offer larger specific surface (and

A IS KEY DIMENSIONLESS  
 PARAMETER  $A \equiv \frac{L}{mG}$

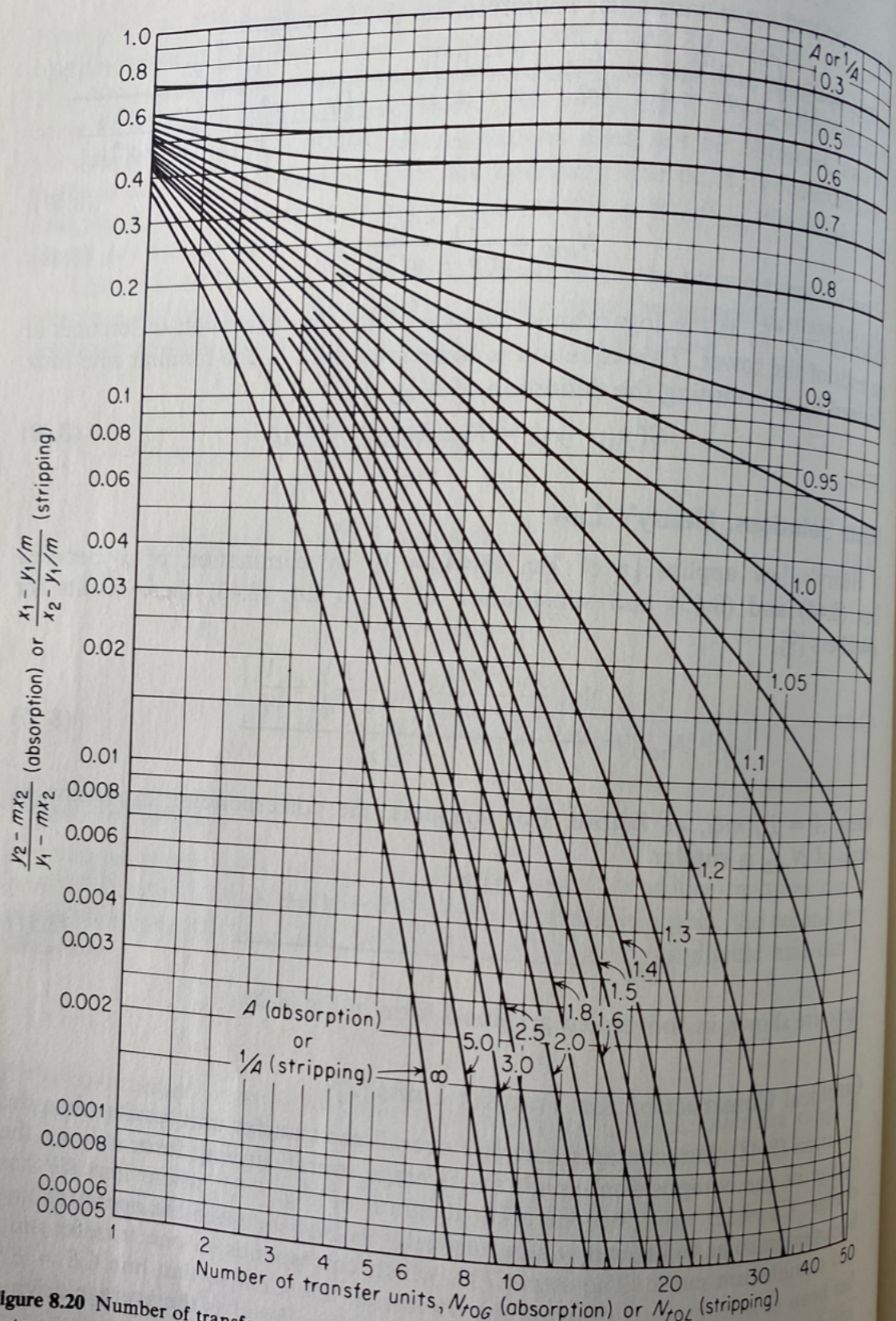


Figure 8.20 Number of transfer units for absorbers or strippers with constant absorption or stripping factor.

$N_{TOG}$

$$Z = N_{TOG} H_{OG}$$

$$H_{OG} = \frac{G}{\text{RATE OF MASS TRANSFER}}$$



# UNIT OPERATIONS

## GAS ABSORBER

THE GAS ABSORBER IN THE IMPERIAL COLLEGE PILOT USES AN MEA IN WATER LIQUID TO ABSORB  $\text{CO}_2$  FROM A MIXTURE IN  $\text{N}_2$

## ABSORBER AND STRIPPER



Structured



Both give: Random

- high surface area between liquid and gas ( $350 \text{ m}^2/\text{m}^3$ )
- continuous mixing of liquid and gas and they flow through column
- high fraction of "void" space so that the pressure drop is low